

# Growth mechanism of single-walled carbon nanotube from catalytic reaction inside carbon nanotube template

*Yoshifumi Izu<sup>1</sup>, Junichiro Shiomi<sup>1,\*</sup>, Yoshiteru Takagi<sup>2,3</sup>, Susumu Okada<sup>2,3</sup>, Shigeo Maruyama<sup>1,\*</sup>*

<sup>1</sup>Department of Mechanical Engineering, The University of Tokyo, Tokyo 113-8656, Japan

<sup>2</sup>Institute of Physics and Center for Computational Sciences, University of Tsukuba, 1-1-1 Tennodai, Tsukuba 305-8577, Japan

<sup>3</sup>Japan Science and Technology Agency, CREST, 5 Sanbancho, Chiyoda-ku, Tokyo 102-0075, Japan

shiomi@photon.t.u-tokyo.ac.jp, maruyama@photon.t.u-tokyo.ac.jp

**RECEIVED DATE (to be automatically inserted after your manuscript is accepted if required according to the journal that you are submitting your paper to)**

**ABSTRACT** We report a numerical investigation on the catalytic growth mechanism of a single-walled carbon nanotube (SWNT) inside a template SWNT, i.e. formation of a double-walled carbon nanotube (DWNT). The molecular dynamics simulations together with complementally ab initio calculations suggest that the DWNT formation from thermally annealed metallocene-encapsulating SWNT goes through formation of metal catalyst cluster, followed by SWNT precipitation at the root. The diameter of the inner SWNT is determined by the carbon/metal layered structure of the catalyst cluster, which gives rise to a DWNT interlayer distance significantly different from the van der Waals distance.

Carbon nanotubes (CNTs) have been celebrated for their novel electrical, optical, thermal, and mechanical properties arising from the quasi-one-dimensional structure with seamless covalent bond networks<sup>1</sup>. One direct application of the unique geometry, among many, is the nanoscale reactor to realize chemical reactions in the quasi-one-dimensional interior. Such chemical reactors are promising platforms for invention of new materials with restricted structures and low dimensional properties.<sup>2-9</sup> Interiors of CNTs also offer chemically and thermally stable environments for subtle chemical reactions. In addition, high reaction efficiency can be achieved by the directional molecular diffusion and high molecular collision rate under the confinement. Furthermore, CNTs serve as an ideal support for single molecule observation under transmission electron microscope.<sup>10</sup> With this multifunctional feature, CNT could be thought as a “nanoscale laboratory”, a foundation for future nanomaterial innovations.

A successful demonstration of the above concept can be found in formation of a CNT inside a template CNT.<sup>2-7</sup> An ultimate case is when the CNTs are single-walled carbon nanotubes (SWNTs), which results in a formation of a double-walled carbon nanotube (DWNT). It has been well known that DWNTs can be formed by thermalizing peapods (SWNTs filled with fullerenes).<sup>2-4</sup> More recently, it was shown that DWNTs can also be synthesized by thermally annealing SWNTs encapsulating ferrocene.<sup>5,7,8</sup> A key finding in these works is that the diameter of the inner SWNT depends on the synthesis method. Shiozawa et al<sup>8</sup> showed by using detailed resonant Raman spectroscopy that DWNTs formed from the ferrocene-encapsulating SWNTs exhibit considerably larger interlayer distance (i.e. smaller inner tube diameter for the same outer tube) than that from peapods. The finding opens up a possibility for tailoring the interlayer distance and thus the properties of DWNTs, complementing other well-explored growth methods such as the arc discharge<sup>11-13</sup> and chemical vapor deposition<sup>14-17</sup>. This is impacting since DWNTs are expected to possess similar low dimensional transport properties as SWNTs with even better mechanical strength, and hence, are attractive building blocks for various nanodevices. However, the cause of the different interlayer distances is not understood yet, and it is of a primary task to identify the growth mechanism of the inner SWNT inside the nanotube templates.

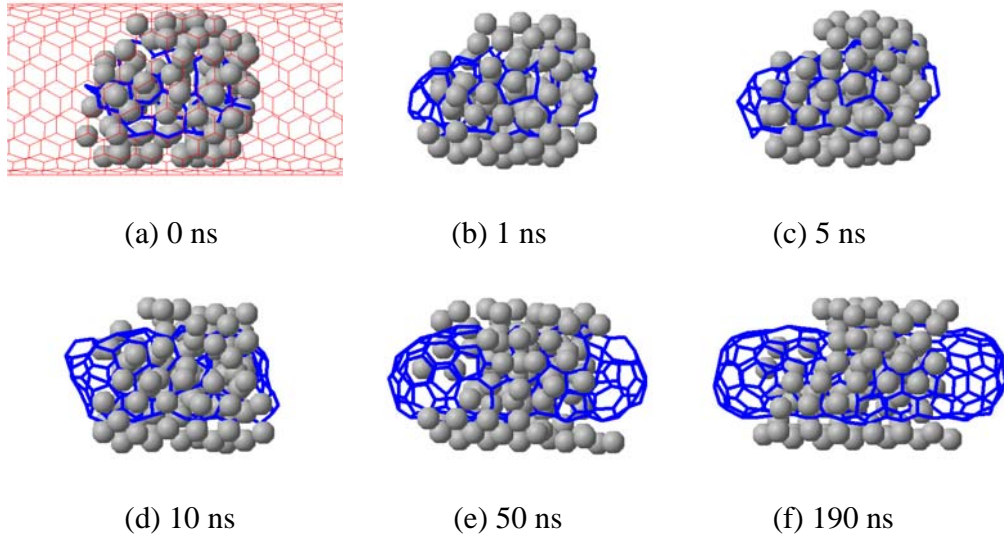
The DWNT formation from thermally annealed peapods can be pictured as fullerenes fusing and relaxing into an SWNT. The experiments have shown that the interlayer distance differs from the typical van der Waals distance of graphite and multi-walled CNT, though the sign of the difference depends on the report.<sup>4,8</sup> Nevertheless, the interlayer distance is expected to depend on the kinetic path of the polymerization of fullerene precursors as shown by the molecular dynamics simulations.<sup>18,19</sup> On the other hand, the understanding of the formation process of DWNTs from metallocene-encapsulating CNTs is much more limited. Although the experiments have probed signatures of catalytic growth from metal carbide clusters<sup>8</sup>, no temporally resolved microscopic analysis is available to this date. Therefore, in this work, we study the growth process of an inner SWNT from catalytic reaction inside a template SWNT by using molecular dynamics (MD) simulations. By choosing nickel as the representative transition metal, the catalytic reaction of the feedstock carbon atoms and metal carbide inside a template SWNT was modeled by adopting the set of potential functions that has been successful in simulating the nucleation of metallofullerenes<sup>20</sup> and SWNTs<sup>21</sup> from floating catalysts. Based on the general growth mechanism obtained from the MD simulations, we further quantify the interlayer distances of the DWNT by using an ab initio calculation, which allows us to compare the numerical simulations with the experiments and to validate the growth model.

In the MD simulations, catalytic growth was simulated by feeding carbon source to a stable metal cluster inside a template SWNT. The model assumes a formation of stable metal carbide cluster prior to the SWNT growth. The model is further simplified by expressing the catalytic reaction between the metal cluster and the carbon source with the reaction of the cluster and individual carbon atoms (feedstock carbon atoms). For sake of computational time, the simulations were given quasi-deterministic initial conditions based on the knowledge learnt from the previous simulations on SWNT growth from floating catalysts.<sup>21</sup> The previous work found that the efficiency of the cap nucleation depends on the contents of the graphitic network embedded in the metal carbide cluster. Therefore, in this study, we have tailored the initial nickel carbide cluster with high content of graphene networks (see supporting information for the methodology).

The growth simulations were performed for template SWNTs with various chiralities and metal carbide clusters with various sizes. The temperature was set at 2500 K, much higher than in the actual experiments<sup>8</sup>, in order to accelerate the simulation and also by considering the relatively high equilibrium binding energies of the current potential functions. The feedstock carbon atoms were fed at random locations inside the template SWNT by keeping the density of the isolated carbon atoms constant, i.e. a new carbon atom was added for every carbon atom adsorbed onto the metal carbide cluster. An exception was made when no absorption took place for 10 ns, then the density was increased to speed up the process. The feedstock carbon atoms were not allowed to react with each other before they reach the metal carbide cluster. During the growth simulation, the 3-D periodic boundary conditions were adopted and the carbon atoms of the template SWNT were fixed at the equilibrium positions (adiabatic condition). All of the above simplifications were adopted in the MD model in order to simulate the entire process from nucleation to growth of inner SWNTs. While the literature offers various molecular dynamics approach with different levels of accuracy and concepts<sup>21-28</sup>, they all needed to compromise between the simulation time and the model accuracy. Our strategy here is to identify a qualitative growth mechanism using simple classical molecular dynamics simulation, and complement it with the ab initio calculation when quantification is necessary.

The trajectories obtained from the simulations clearly show the growth of the inner SWNT from the catalyst cluster. Figure 1 depicts a case simulated until  $t=190$  ns, starting from an initial condition with Ni<sub>97</sub> carbide cluster encapsulated in a (10, 10) SWNT. At the early stage, the feedstock carbon atoms cover the cluster surface except for the part in contact with the outer SWNT. Once all the open sites are occupied, the carbon atoms precipitate to form a cap structure and then an SWNT. The general trend was the same for other cases with different outer SWNT chiralities and initial cluster sizes. In order to gain insight into the dynamics of the cluster during the SWNT growth, the Lindemann index<sup>29</sup> of the carbon atoms in the cluster was calculated. As a result, the index was found to always remain well below 0.1, the threshold value below which the system can be considered to be solid<sup>30</sup>. This indicates

that the carbon structure inside the metal carbide cluster is stable and additional carbon atoms from the feedstock hardly diffuse into the cluster throughout the growth process.

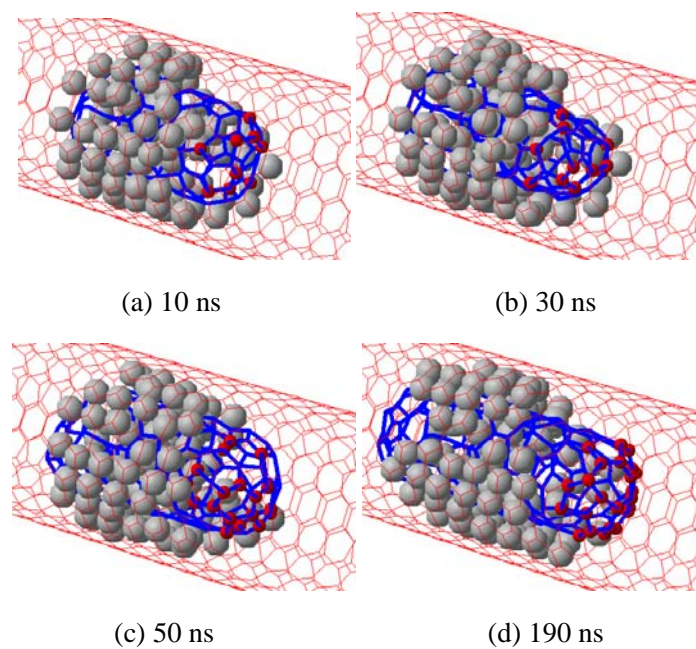


**Figure 1.** Growth process of an SWNT (blue) inside a template (10, 10) SWNT (red). Covalent bonds of the inner and outer SWNTs are denoted with blue and red lines. The outer SWNT is omitted for (b-f) for visual clarity.

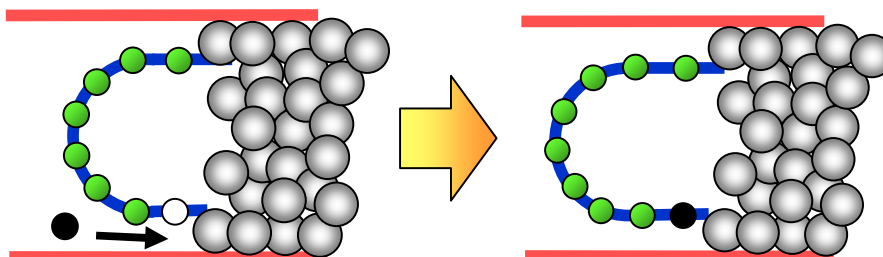
More details of the carbon supply process was studied by marking (with red spheres) the carbon atoms that formed the tip of the cap at  $t=190$  ns, and monitoring their trajectories during the growth process (Fig. 2). The visualized trajectories reveal that the feedstock carbon atoms mainly adsorb onto the open sites of the outermost metal layer of the cluster, and then are carried away from the cluster as more carbon atoms are fed and precipitate. This suggests the growth mechanism shown in Fig. 3 for the catalytic reaction inside a template SWNT; once the cap is formed, carbon atoms are fed from the root of the cap to realize continuous growth of the inner SWNT.

The growth simulations for template SWNTs with various chiralities reveal the influence of the template geometry on the resulting structure of the inner SWNT. A general and most important characteristic is that the inner SWNT diameter is well-correlated with the outer SWNT diameter keeping the interlayer distance at a constant value, which will be discussed later. For now, let us briefly

discuss the structural details; if the chiral angel has noticeable influence on the structure of the inner SWNT. The result shows that the outermost nickel layer is aligned with the outer SWNT structure, with the nickel atoms locating near the hollow site of the graphitic network of the outer SWNT (Fig. S2). However, we could not observe a clear evidence of the metal alignment affecting the carbon structure precipitated from the catalyst cluster, partially due to lack of statistics. The dependence on the cluster size was also investigated by varying the number of nickel atoms in the metal carbide cluster as 108, 128, and 158, which showed no deterministic influence on the resulting inner SWNT.



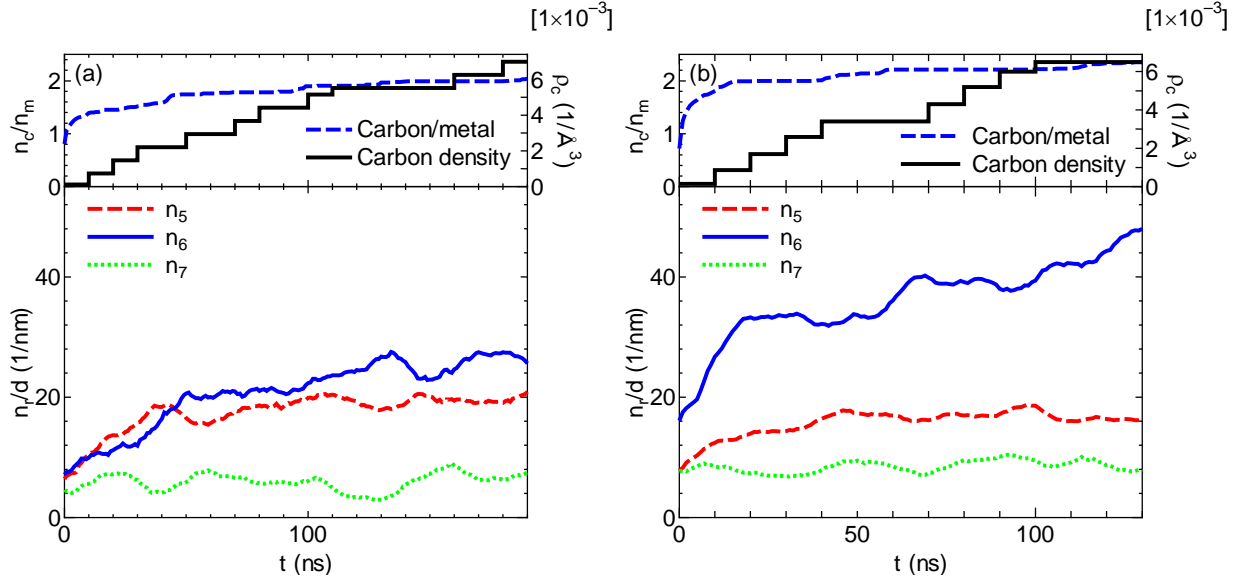
**Figure 2.** Trajectories of carbon atoms. The carbon atoms forming the cap at  $t=190$  ns is denoted with red spheres.



**Figure 3.** Schematics of inner SWNT growth process.

One useful way to characterize the formation of SWNT is to measure the number of 5-7 membered rings<sup>21</sup>. This also allows us to monitor the time evolution of the growth process, i.e. the growth rate. Figure 4 (a, b) shows time histories of the number ratio of carbon to metal in the catalyst cluster ( $n_c/n_m$ ), the number density of the feedstock carbon atoms ( $\rho_c$ ), and the number of 5-7 membered rings ( $n_5-n_7$ ), for outer SWNTs with chiralities (10, 10) and (15, 6). Note that, in order to achieve monotonic growth, the number density of the feedstock carbon was increased with time. Although the time histories of  $\rho_c$  are not the same for the two cases reflecting the different growth rate, the difference is minor and should not affect the following discussions. For both cases, the  $n_6$  profiles exhibit two regimes; an initial faster growth and the following slower growth, despite the gradual increase in the feedstock density. An insight into this can be gained from the  $n_5$  profiles, which increase in the beginning and gradually saturate before  $t=50$  ns at a constant value. This corresponds to the formation of the cap structure which needs 5 membered rings to form the 3-d curvature. Once the cap is formed,  $n_5$  saturates at around a value of  $n_5/d$  ( $=20 \text{ nm}^{-1}$ ) independent of the outer SWNT diameter ( $d$ ). Therefore, the above behavior of the  $n_6$  profiles corresponds to the relatively fast nucleation of the cap and the slow growth of the side walls.

This agrees with the pictures shown in Fig. 1, where the cap formation is completed before  $t=50$  ns. The growth deceleration can be understood from the growth mechanism described in Fig. 3, where the feedstock needs to overcome the potential barrier to diffuse through the channel between inner and outer SWNTs, which becomes larger as the cap forms and the side wall grows. This also results in a much slower growth speed compared with the SWNT nucleation from floating catalyst cluster in the previous molecular dynamics study<sup>21</sup>. While the general trend of the growth curves was the same for the two cases, the distinct difference in the magnitude of  $n_5/d$  suggests that the growth rate of the inner SWNTs sensitively depends on the outer diameter. Note that the magnitude of  $n_7$  indicates the extent of defects, which is similar and relatively low in both cases.

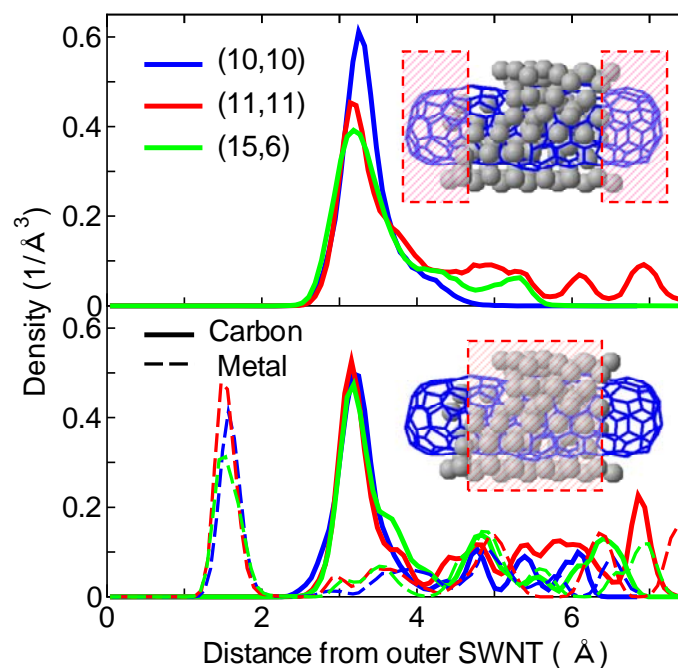


**Figure 4.** Structural properties of the inner SWNT growth for (a) (10, 10) and (b) (15, 6) outer SWNTs. In the bottom figures, the time histories of the number of 5, 6, and 7 membered rings ( $n_5$ ,  $n_6$ ,  $n_7$ ) are denoted with dashed, solid, and dotted lines, respectively. Here,  $d$  is the diameter of the outer SWNT. The top figure denotes the ratio of number of carbon atoms ( $n_c$ ) to that of metal atoms ( $n_m$ ) in the metal carbide cluster with the dotted lines, and the feedstock carbon density ( $\rho_c$ ) with the solid lines.

Let us now investigate the interlayer distance of the DWNT. Taking the cases where highly crystallized DWNT growth was observed, the density distribution function (DDF) of the carbon atoms of the inner SWNT was calculated as a function of the radial distance from the outer SWNT (Fig. 5). The interlayer distance was about  $3.2 \text{ \AA}$  independently of the outer SWNT diameter, which is significantly different from the van der Waals distance ( $3.4 \text{ \AA}$ ). The cause of the interlayer deviation can be understood by comparing the carbon DDFs of the inner SWNT and the catalyst cluster. The good match between the peak positions indicates that the diameter of the inner SWNT is determined by the carbon structures inside the catalyst cluster. The primary role of the metal carbide structure over the interlayer van der Waals interaction was also checked by performing the simulations for two different models with and without van der Waals interactions between the inner and outer SWNTs (Fig. S3). Figure 5 also shows that the largest metal DDF peak is located right in between the largest carbon DDF peak and the outer SWNT, therefore the metal carbide cluster takes a distinct layered structure with



outer metal and inner carbon layers. The above adds up to the following mechanism; equilibration of metal carbide cluster inside a template SWNT gives rise to a layered structure, where a metal layer is sandwiched between the template SWNT and the internal carbon layer. This structure guides the inner SWNT to grow preserving the interlayer distance between the carbon structure and the outer SWNT. Since the inner SWNT grows from the root, the structure is strongly influenced by the metal carbide structure at the SWNT/cluster interface, and thus inherits the diameter of the carbon layer in the catalyst cluster.



**Figure 5.** Density distribution function of carbon/metal atoms in (top) the precipitated SWNT, and (bottom) the metal carbide cluster, for three different outer SWNT chiralities.

The MD simulations so far suggest that the diameter of the inner SWNT grown from the catalyst cluster inside a template SWNT is determined by the distance between the concentric carbon layers separated by the metal layer in between. This means that the inner SWNT diameter can be predicted by knowing the bond length of the intercalating structure. Then the next step is to check if this mechanism agrees with the available experiments. Since the quantitative comparison with the experiments on such a structure requires charge transfer effects, which cannot be taken into account in the current MD

potential model, we have separately performed ab initio calculations based on the density functional theory (DFT)<sup>31</sup>. For this, we have reduced the system to a metal atom intercalating two graphitic layers. Furthermore, by ignoring the curvature of SWNT for simplicity, the system can be considered as the conventional graphite intercalation compound (GIC). Iron (Fe) was chosen as the metal to compare the results with the experiment of DWNT formation by thermally annealing ferrocene encapsulating SWNTs<sup>8</sup>. For the DFT calculation, the generalized gradient approximation (GGA)<sup>32</sup> was adopted for the electron exchange-correlation potential, and electron-ion interaction was expressed using the ultrasoft pseudopotential. The valence electron wave-functions were expanded using a plane wave basis with a kinetic cutoff energy of 36 Ry. The ab initio calculations of the Fe-GIC system with stable structure resulted in interlayer distance of 3.53 Å, which agrees well with the experiment<sup>8</sup>. The agreement supports the validity of the above growth mechanism obtained from the MD simulations; the inner SWNT grows through formation of the metal cluster and the interlayer distance is determined by the layered structure of the heterogeneous catalyst cluster.

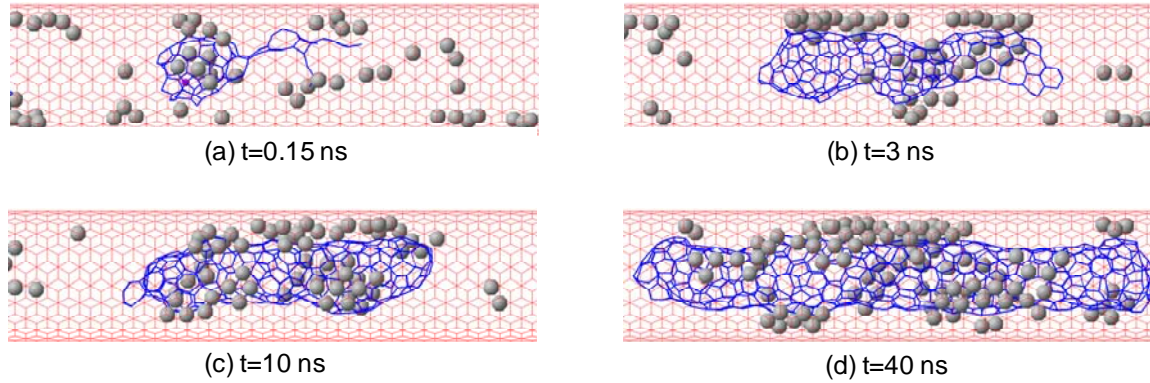
The above molecular simulations assumed that the inner SWNT is grown from a metal cluster, based on the reported experimental observation<sup>8</sup>. However, especially at high temperature, the thermally decomposed species may start reacting and nucleating before forming a stable metal cluster. In order to validate this possibility and also to seek for alternative reaction pathway, we have performed additional simulations in the other extreme case; SWNT growth from catalytic reaction of fully thermally decomposed precursors. For sake of simplicity and practicability in the molecular dynamics framework, we rephrase this as “catalytic reaction starting from individual carbon and metal atoms randomly placed inside a template SWNT”. This was done using the same MD model as the previous simulation for a cluster, except for a modification on the metal-metal and metal-carbon binding energies. On beginning the simulation from initial conditions with isolated metal atoms, the surface diffusion length of the metal atoms on the template SWNT and the grown inner SWNT becomes considerably larger than that of the previous initial conduction with a cluster, and hence, plays an important role on determining the resulting inner SWNT growth. Therefore, magnitude of the binding energy in the graphitic/metal

layering structure becomes important even for qualitative characterization unlike the previous simulation with minute diffusion of the cluster. For these reasons, we have incorporated the metal-graphite binding energy obtained from the above DFT calculation of the Fe-GIC system. As a result, the metal-carbon binding energy is approximately half of the value in the previous simulations for nickel carbide system. Correspondingly, the metal-metal binding energy was scaled by half to maintain the consistency.

The simulation begins by gradually feeding metal and carbon atoms inside the template SWNT with number ratio of initially 1:2 and then 1:10 corresponding to that of metallocene. The temperature was kept same as the previous simulations (2500 K). The number density of the carbon gas was kept constant. Note that carbon atoms are allowed to react only through catalyst metal atoms. As a consequence, this model realized highly efficient growth of the inner SWNT as seen in Fig. 6, which shows the growth process inside a (11, 11) template SWNT until  $t=40$  ns. The figure clearly shows the initial formation of a patch of graphite network [Fig. 6(a)] and then a cap structure [Fig. 6(b-c)] due to the catalytic activity of the metal in form of a small cluster with several atoms. The metal particles are adsorbed onto the outer SWNT and act as a reaction site to further growth of inner SWNTs. The individual metal atoms or small cluster here exhibits a longer diffusion length and are more volatile than the previous case with nanoscale metal cluster. Therefore, in this case, the growth site is not fixed, but varies with time. The same growth process was observed for other kinds of outer SWNT chiralities. To the authors' knowledge, among many reported molecular dynamics simulations with non-ad hoc and ad hoc MD models, the SWNT grown in the current simulation is one of the longest ones.

As in the previous case for growth from catalyst cluster, density distribution function was calculated (Fig. S4), and the interlayer distances was obtained to be 3.4 Å corresponding with the van der Waals distance, independently of the outer SWNT diameter. This is because there are less metal particles around the growth site due to the relatively large growth site and high mobility of the metal atoms. Therefore, the results does not agree with the DWNT growth experiment from ferrocene encapsulating SWNTs<sup>8</sup>, and rather supports, though does not prove, the validity of the previous catalyst cluster model.

On the other hand, it suggests there may be other possible growth path that might be more efficient than the growth from the catalytic cluster.



**Figure 6.** Growth process of an SWNT inside a (11, 11) SWNT from randomly placed individual carbon and metal atoms. Covalent bonds of the inner and outer SWNTs are denoted with blue and red lines.

In summary, formation process of DWNT from metallocene-encapsulating SWNT was investigated by combining MD simulations and DFT calculations. Firstly, by assuming the formation of catalyst nanocluster prior to the growth of inner SWNT, the growth process was clearly identified by the MD simulations. The detailed observation of the molecular trajectories reveals the root growth of the inner SWNT. Here, the carbon atoms access the catalyst through the potential barrier between the inner and outer SWNT, which increases as the inner SWNT grows, and thus slows down the growth for constant feedstock density. The DDF of constituent atoms reveals that the DWNT interlayer distance significantly differs from the van der Waals distance for graphite and multi-walled CNT. The good correlation between the DDFs of the precipitated SWNT and the layered metal carbide cluster suggests that the interlayer distance is determined by the carbon/metal layered structure of the metal carbide cluster. Based on the general mechanism obtained from the molecular dynamics simulations, interlayer distance of the layered structure was quantified by performing ab-initio calculations for Fe-GIC system. By taking iron as the metal, the good agreement was obtained with the experiments on DWNT

formation from ferrocene encapsulating SWNT. Further insight into the validity of the catalyst cluster model is gained by examining the other extreme growth scenario; growth of inner SWNT from randomly placed the individual carbon and metal atoms. This resulted in highly efficient growth, where the interlayer distance was equal to the van der Waals distance. Although this may suggest a possibility for more efficient pathways, the good agreement between the catalyst cluster model with the experiments suggests that the DWNT formation from ferrocene-encapsulating SWNT goes through a formation of metal cluster.

**Acknowledgment.** This work is supported in part by Grants-in-Aid for Scientific Research 19051016 and 19054003.

**Supporting Information Available.** Molecular dynamics potential, method of tailoring initial metal carbide cluster, data of Lindemann index calculations, and more details on outer-tube chirality dependence and density distribution functions. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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