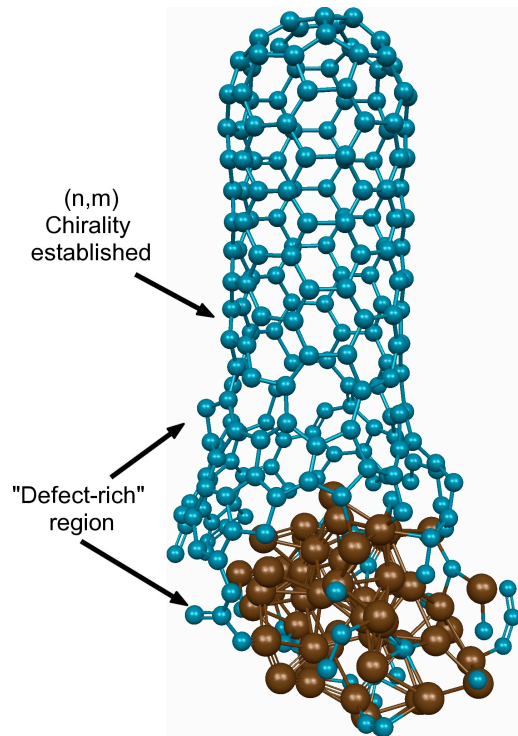




# What Can We Learn from Current Molecular Dynamics Simulations of Nanotube Growth?

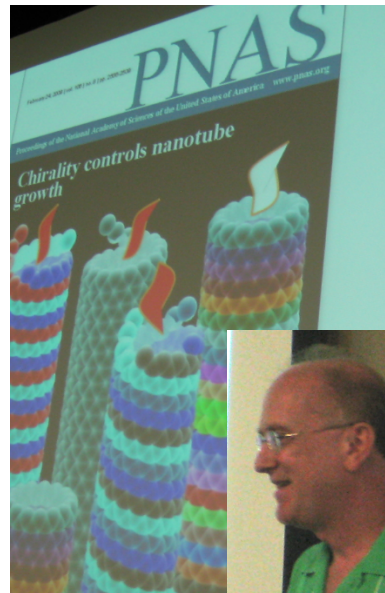
Stephan Irle



Molecular Dynamics

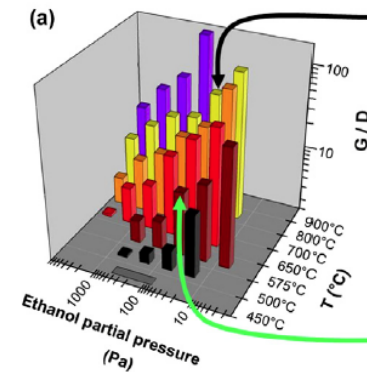
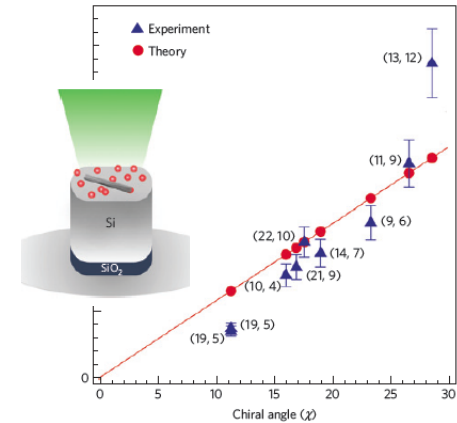


VS



Thermodynamics

VS



Experiments



# Acknowledgements



Prof. Keiji Morokuma



Dr. Yasuhito Ohta<sup>a</sup>

<sup>a</sup>now: Professor, Nara Women's University



Dr. Hai-Bei Li



Dr. Yoshiko Okamoto



Dr. Ying Wang<sup>c</sup>

<sup>c</sup>now: Professor, Changchun Institute for Applied Chemistry (CHINA)



Dr. Alister J. Page<sup>b</sup>

<sup>b</sup>now: Lecturer, University of Newcastle (AUS)



Dr. Joonghan Kim

# Acknowledgements

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-  *Japan Science and Technology Agency* CREST grant 2006-2012 (KM, SI) and AFOSR (to KM)
- MEXT Tenure Track program (SI)



## Computer resources :

- Research Center for Computational Science (RCCS), Okazaki Research Facilities, National Institutes for Natural Sciences.
- Academic Center for Computing and Media Studies (ACCMS), Kyoto University

## ADVERTISEMENT #1

[Download \(.pdf\)](#)

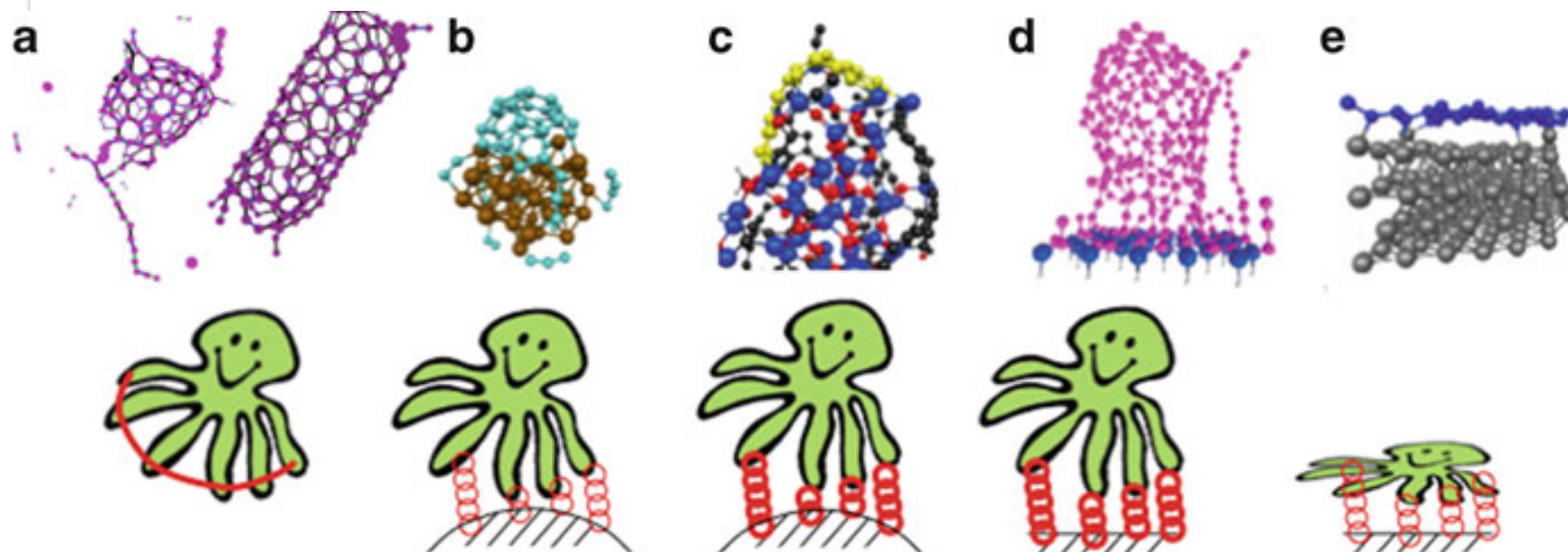
• 479



A contribution to “Practical Aspects of Computational Chemistry II: An Overview of the Last Two Decades and Current Trends”, eds. J. Leszczynski and M. K. Shukla, Springer-European Academy of Sciences (publication scheduled for April 2, 2012), <http://www.springer.com/chemistry/book/978-94-007-0922-5>

**Atomistic mechanism of carbon nanostructure self-assembly  
as predicted by nonequilibrium QM/MD simulations**

Stephan Irle,<sup>1</sup> Alister J. Page,<sup>2</sup> Biswajit Saha,<sup>2</sup> Ying Wang,<sup>1</sup> K. R. S. Chandrakumar,<sup>2</sup> Yoshio Nishimoto,<sup>1</sup> Hu-Jun Qian,<sup>1</sup> and Keiji Morokuma<sup>2,3</sup>



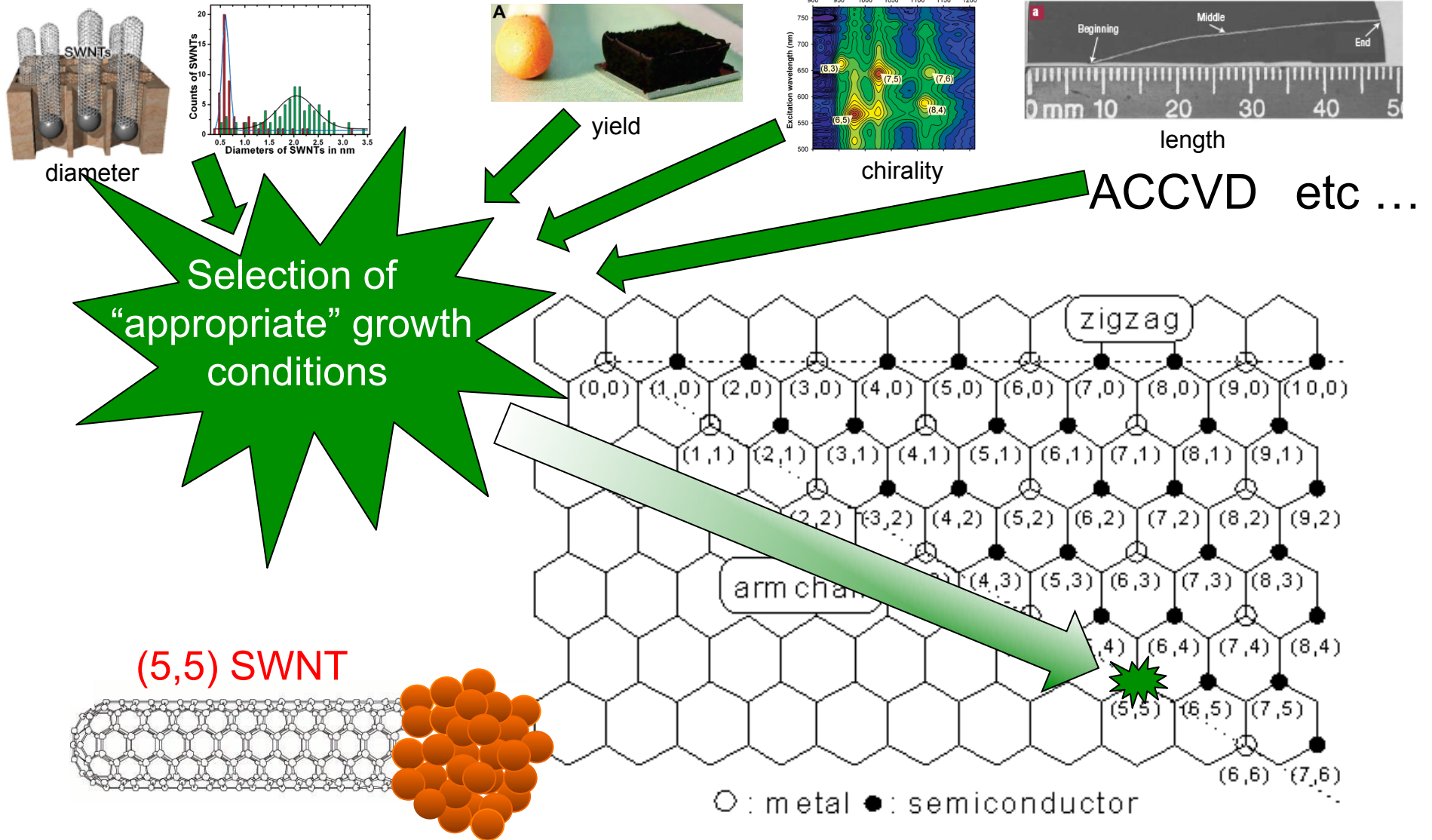
# Overview

- **Overview: What are MD simulations up against?**
- **Density-functional tight-binding (DFTB)-based MD**
- **DFTB/MD Simulations: Acetylene feedstock, carbon-only feedstock, catalytic CVD, catalyst-free CVD**
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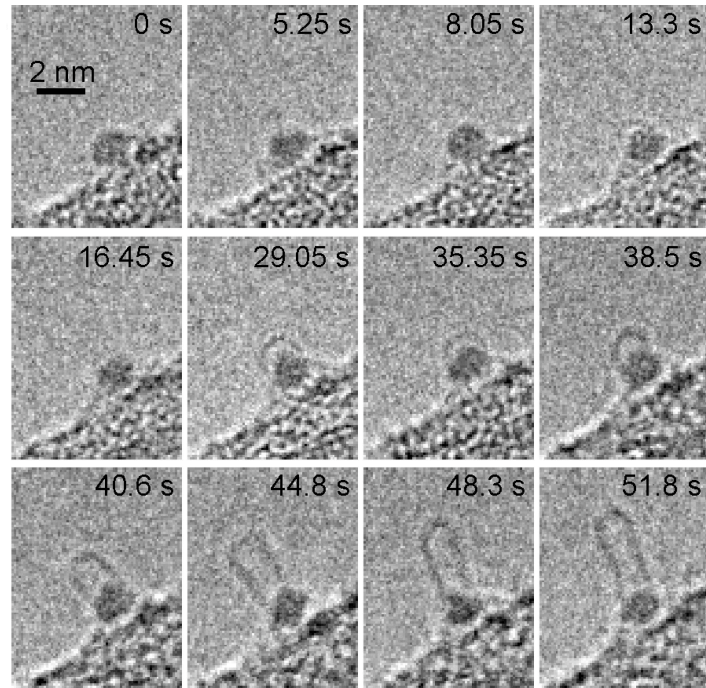
# The ultimate goal: (n,m)-specific SWNT Growth



high yield, desired length, defect-free, eventually catalyst-free

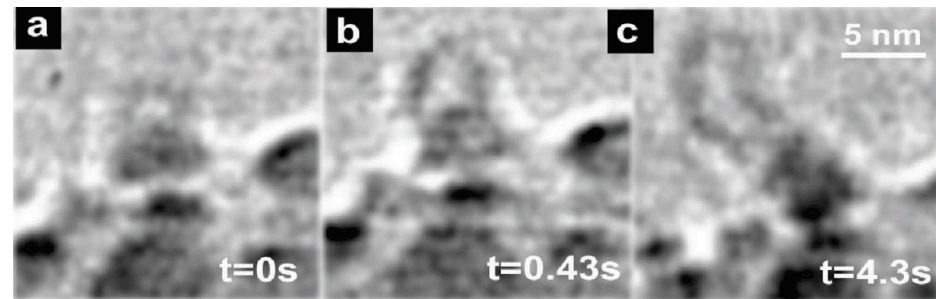
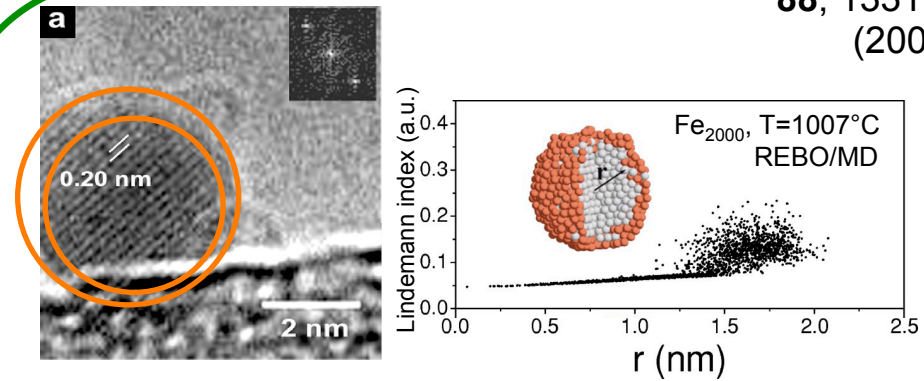
# Look here ... *in situ* environmental TEM studies of SWNT nucleation and growth

F. Ding, *et al.*  
*Appl. Phys. Lett.*  
**88**, 133110  
 (2006)



Fe/SiO<sub>2</sub> C<sub>2</sub>H<sub>2</sub>:H<sub>2</sub> T=600°C  
**Fluctuating solid Fe<sub>3</sub>C**

H. Yoshida, *et al.* Atomic-Scale In-situ Observation of Carbon Nanotube Growth from Solid State Carbide Nanoparticles, *Nano Lett.* **8**, 2082 (2008)

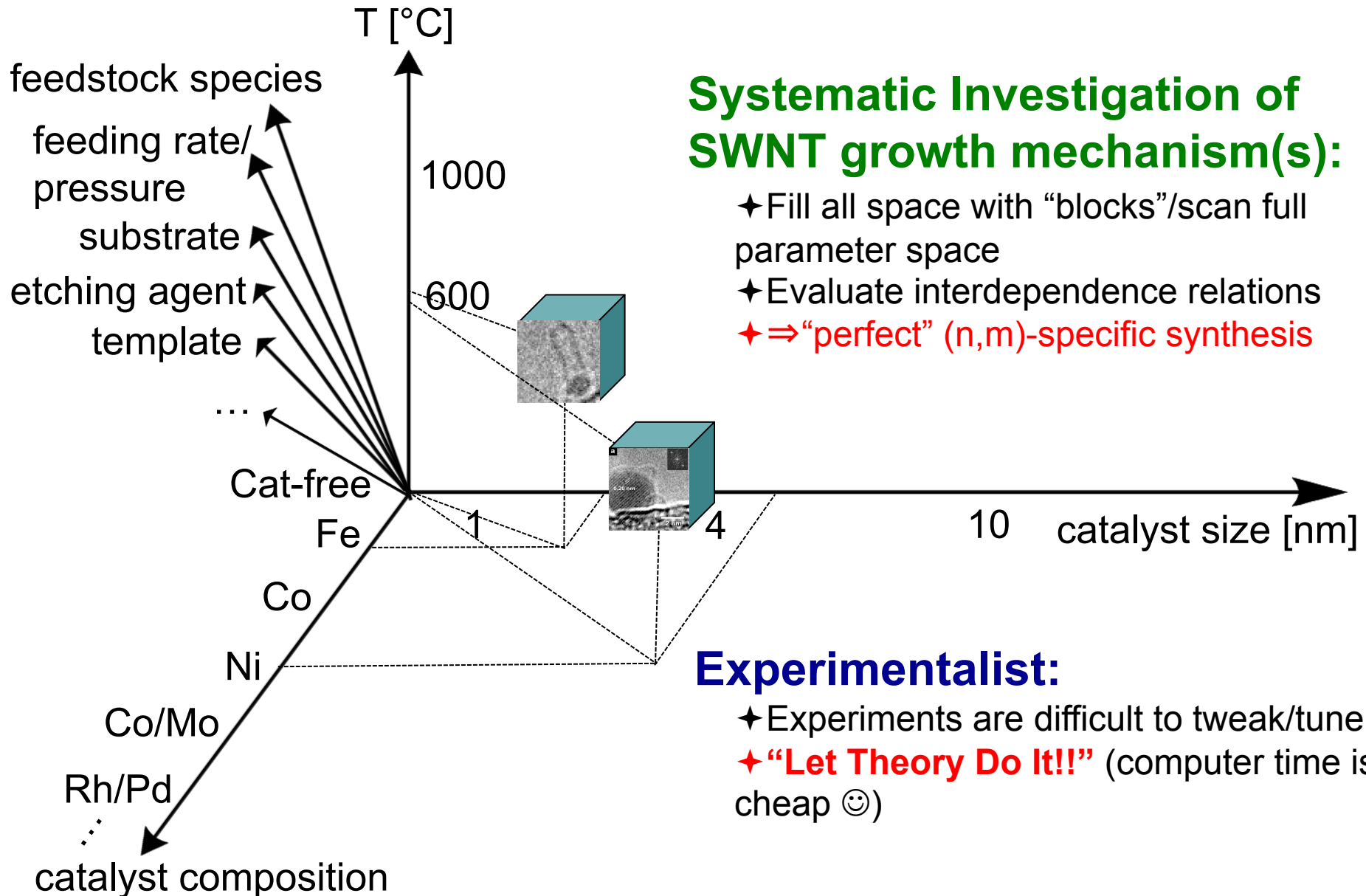


Ni/SiO<sub>2</sub> C<sub>2</sub>H<sub>2</sub>:NH<sub>3</sub> T=480 to 700°C  
**Fluctuating solid pure nickel**

S. Hofmann, *et al.* In-situ Observations of Catalyst Dynamics during Surface-Bound Carbon Nanotube Nucleation, *Nano Lett.* **7**, 602 (2007)

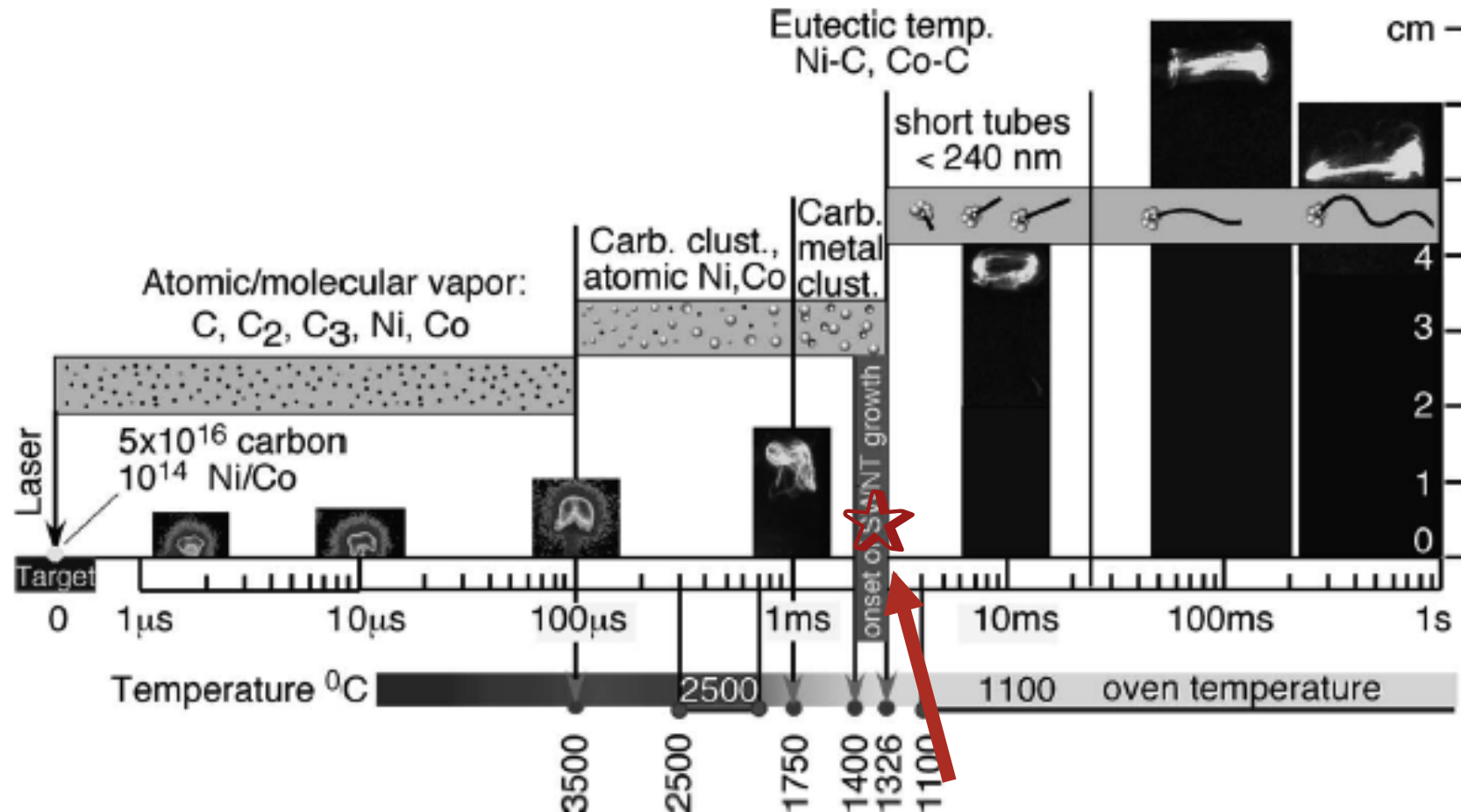


# SWNT Growth Hyperdimensional “Parameter Space”



# Long Timescale of SWNT Formation Mechanism! Example: Laser Vaporization Methods

**Assumption:** Direct correlation between time ~ temperature and growth



**SWNT Nucleation and Growth: We are here, but *ms* may determine (n,m)!**

## What MD method should be used?

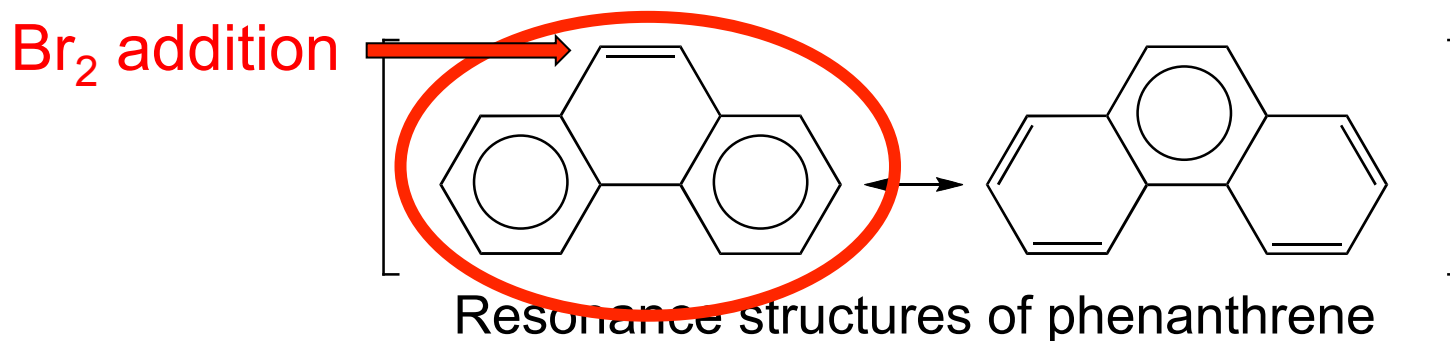
- SiC:  $sp^3$  hybridization, **localized single bonds**
- Graphene:  $sp^2$  hybridization, **delocalized  $\pi$  bonds**

## Graphenes and the Clar Rule

E. Clar, *Polycyclic Hydrocarbons*, Academic Press: London (1964)

Polyaromatic hydrocarbons (PAHs): aromatic compounds

Degree of aromaticity can be different for each ring segment!

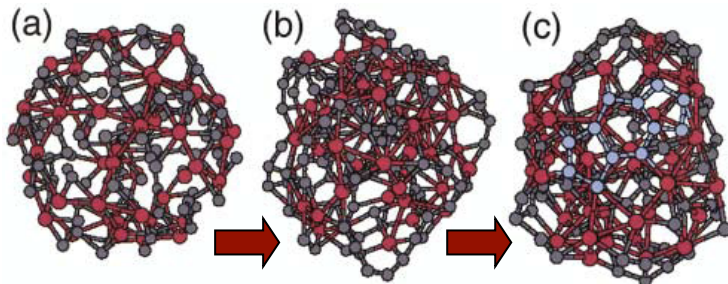


Clar's Rule: "Resonance structure with **most disjoint aromatic  $\pi$ -sextets** is most important for characterization of ring properties"

# Previous Car-Parrinello Molecular Dynamics (CPMD)

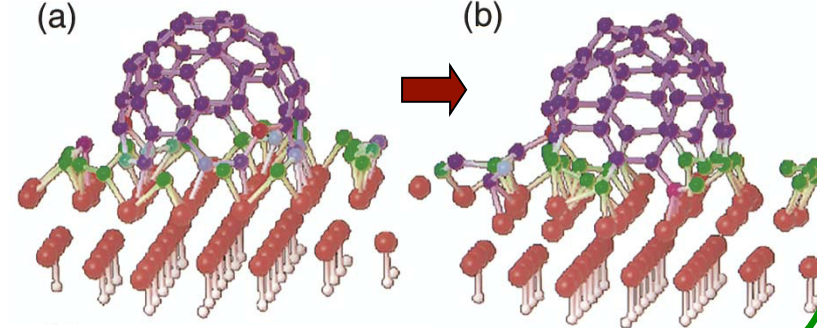
**Heroic efforts on supercomputers, one-shot simulations!**

J. Gavillet *et al*, Root-Growth Mechanism for SWNTs, *Phys. Rev. Lett.* **87**, 275504 (2001)

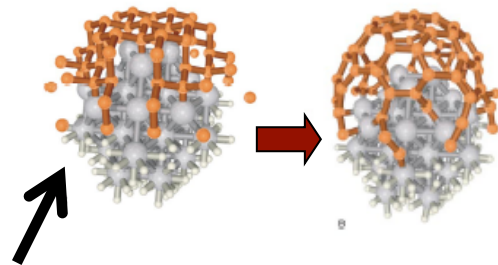


Carbon precipitation on Co carbide particle, 51 Co & 102 C atoms, 25 ps  $\Rightarrow$  **1 hexagon, 2 pentagons**

$C_{30} + 44C$  on Co surface at 1500 K, 15 ps  $\Rightarrow$  **5 carbon atoms diffused to cap**



J.-Y. Raty *et al*, Growth of Carbon Nanotubes on Metal Nanoparticles: A Microscopic Mechanism from *Ab Initio* Molecular Dynamics Simulations, *Phys. Rev. Lett.* **95**, 096103 (2005)



Change from diamond structure ( $sp^3$ ) to fullerene cap ( $sp^2$ ) immediately!

Nano-diamond: **Inappropriate model!**

simulation time  $\sim$  10 ps  
**Too short** to demonstrate self-assembly

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## Tight Binding as Approximate DFT Method

**Density-Functional Tight-Binding:** Method using atomic parameters from DFT (PBE, GGA-type), diatomic repulsive potential

- Seifert, Eschrig (1980-86): minimum STO-LCAO; 2-center approximation
- Porezag, Frauenheim: efficient parameterization

**DFTB**

• **FT**

•

**1000 X FASTER THAN DFT!**



Frauenheim

$$E^{S(\text{pin-polarized})DFTB} = E^{(SCC-)DFTB} + \frac{1}{2} \sum_{A \neq B}^{atoms} \gamma_{AB} \Delta q_A \Delta q_B$$

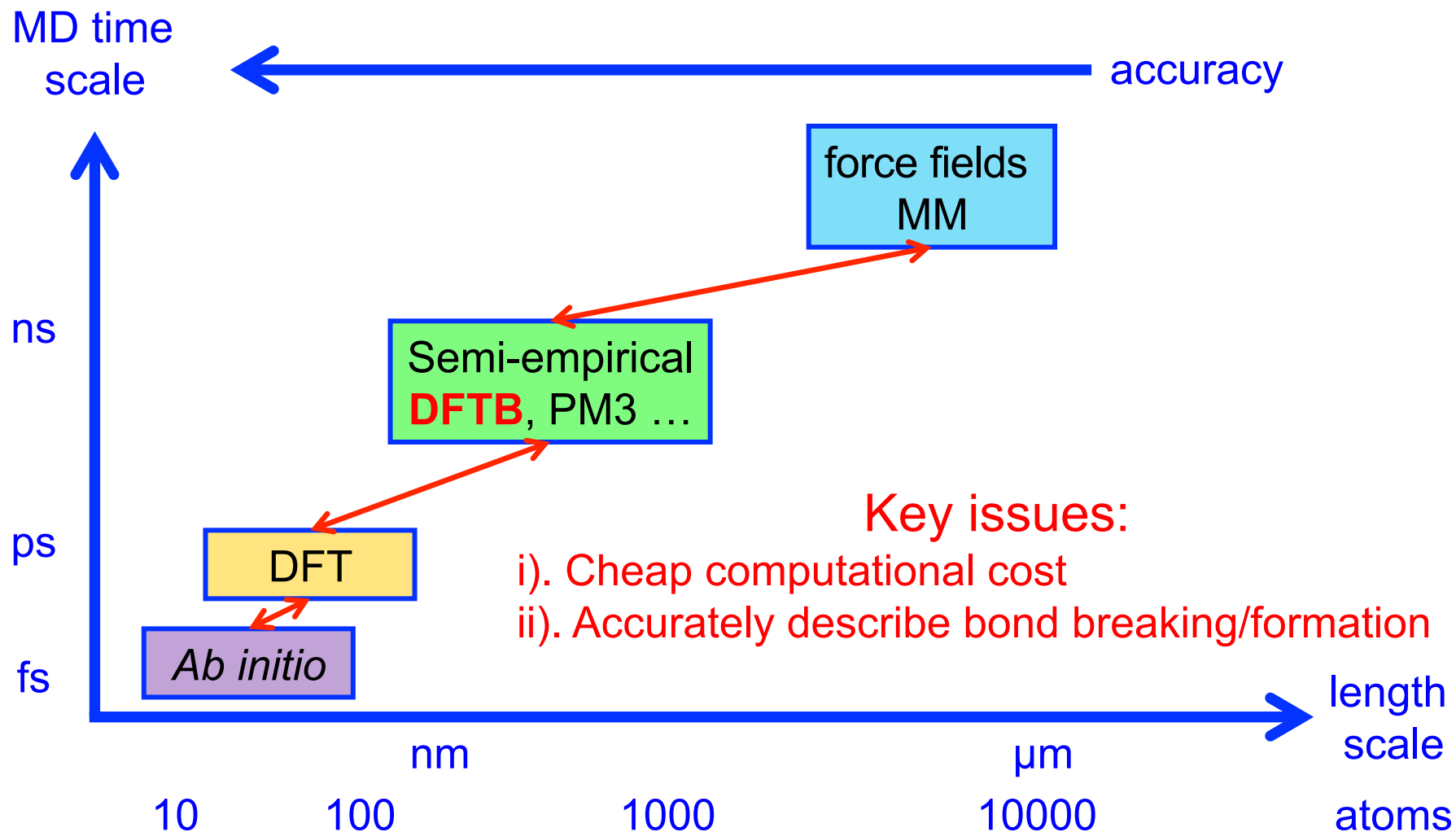


Marcus Elstner

$$E^{S(\text{pin-polarized})DFTB} = E^{(SCC-)DFTB} + \frac{1}{2} \sum_A^{atoms} \sum_{l \in A} \sum_{l' \in A} p_{Al} p_{Al'} W_{All'}$$



Christof Köhler



➤ **DFTB** (density-functional tight-binding) is a well established **approximate DFT method**, but diatomic *parameters* are required. Therefore, we started to develop X-Y parameters for all elements.

Optimized elemental electronic DFTB parameters  
now available for  $Z=1-109$ !



Chien-Pin Chou

Yoshifumi Nishimura, Chien-Pin Chou  
Henryk A. Witek, Stephan Irle



Yoshifumi  
Nishimura



Nagoya University



National Chiao Tung  
University, Taiwan



Henryk A. Witek



# Example: DFTB Si bandstructures, parameters optimized @ bcc only

— DFT  
— DFTB

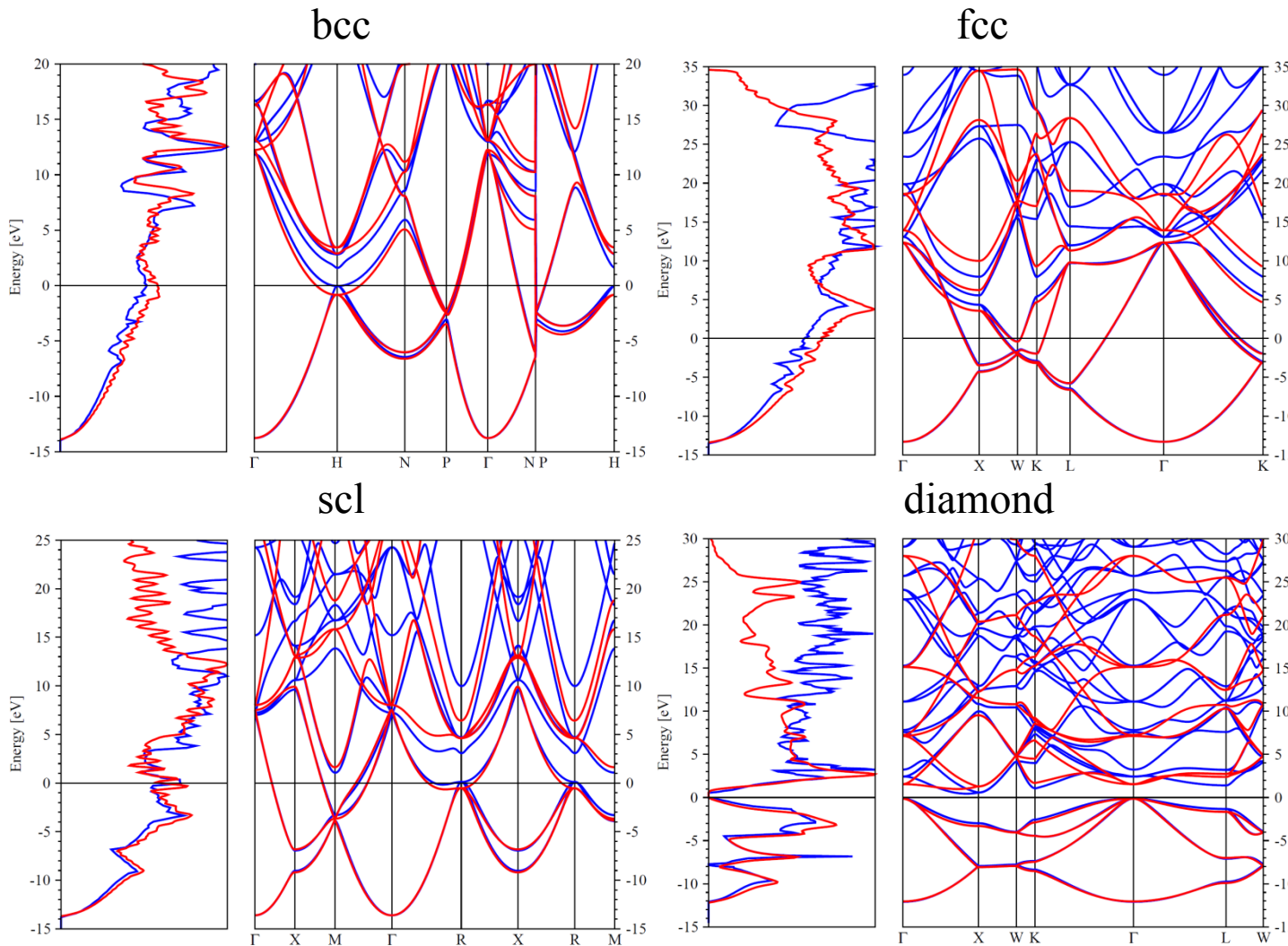
$3s^23p^23d^0$

Lattice constants:

Expt	
· bcc	3.081
fcc	3.868
scl	2.532
diamond	5.431

Parameter sets:

$W$ (orb)	3.33938
$a$ (orb)	4.52314
$r$ (orb)	4.22512
$W$ (dens)	1.68162
$a$ (dens)	2.55174
$r$ (dens)	9.96376
$\epsilon_s$	-0.39735
$\epsilon_p$	-0.14998
$\epsilon_d$	0.21210



➤ Artificial crystal structures can be reproduced well

## SCC-DFTB: general comparison with experiment

### *Performance for small **organic** molecules (mean absolut deviations)*

- Reaction energies:  $\sim 5$  kcal/mol
- Bond lengths:  $\sim 0.014$  Å
- Bond angles:  $\sim 2^\circ$
- Vibrational frequencies:  $\sim 6-7$  %

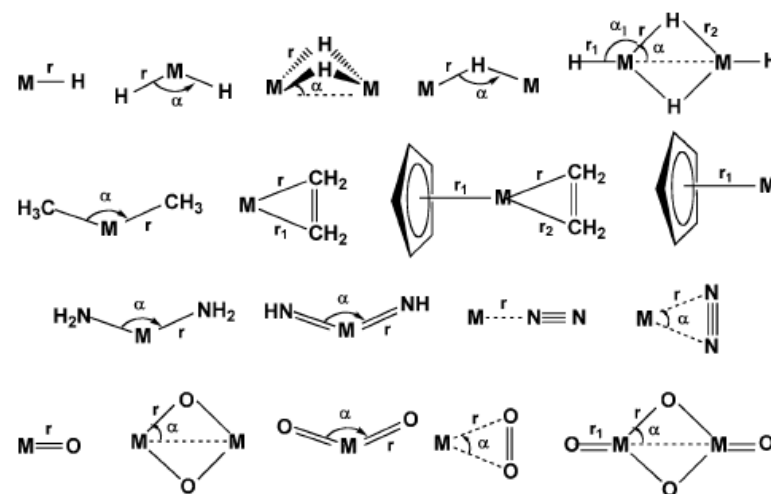
# SCC-DFTB: Transition metals

G. Zheng *et al.* *J. Chem. Theor. Comput.* **3** 1349 (2007)

**Table 2.** List of Molecules and Their Spin States Used in the Parametrization Procedure<sup>a</sup>

	M-M	M-H	M-C	M-N	M-O
M = Sc					
tier 1	<sup>1</sup> Sc <sub>2</sub>	<sup>1</sup> ScH <sub>3</sub>	<sup>1</sup> HScCH <sub>2</sub> <sup>1</sup> H <sub>2</sub> ScCH <sub>3</sub>	<sup>1</sup> ScN <sup>1</sup> H <sub>2</sub> ScN <sub>2</sub>	<sup>1</sup> HScO <sup>1</sup> H <sub>2</sub> ScOH
M = Ti					
tier 1	<sup>1</sup> Ti <sub>2</sub>	<sup>1</sup> TiH <sub>2</sub>	<sup>1</sup> TiCH <sup>1</sup> H <sub>2</sub> TiCH <sub>2</sub> <sup>1</sup> H <sub>3</sub> TiCH <sub>3</sub>	<sup>1</sup> TiN <sup>1</sup> H <sub>2</sub> TiNH <sup>1</sup> H <sub>3</sub> TiNH <sub>2</sub>	<sup>1</sup> H <sub>2</sub> TiO <sup>1</sup> H <sub>3</sub> TiOH
tier 2			<sup>1</sup> Ti(CO) <sub>2</sub> <sup>+4</sup> <sup>1</sup> Ti(CO) <sub>3</sub> <sup>+4</sup> <sup>1</sup> Ti(CO) <sub>4</sub> <sup>+4</sup> <sup>1</sup> Ti(CO) <sub>5</sub> <sup>+4</sup> <sup>1</sup> Ti(CO) <sub>6</sub> <sup>+4</sup>	<sup>1</sup> Ti(NH <sub>3</sub> ) <sub>2</sub> <sup>+4</sup> <sup>1</sup> Ti(NH <sub>3</sub> ) <sub>3</sub> <sup>+4</sup> <sup>1</sup> Ti(NH <sub>3</sub> ) <sub>4</sub> <sup>+4</sup> <sup>1</sup> Ti(NH <sub>3</sub> ) <sub>5</sub> <sup>+4</sup> <sup>1</sup> Ti(NH <sub>3</sub> ) <sub>6</sub> <sup>+4</sup>	<sup>1</sup> Ti(H <sub>2</sub> O) <sub>2</sub> <sup>+4</sup> <sup>1</sup> Ti(H <sub>2</sub> O) <sub>3</sub> <sup>+4</sup> <sup>1</sup> Ti(H <sub>2</sub> O) <sub>4</sub> <sup>+4</sup> <sup>1</sup> Ti(H <sub>2</sub> O) <sub>5</sub> <sup>+4</sup> <sup>1</sup> Ti(H <sub>2</sub> O) <sub>6</sub> <sup>+4</sup>
M = Fe					
tier 1	<sup>1</sup> Fe <sub>2</sub>	<sup>1</sup> FeH <sub>2</sub>	<sup>1</sup> FeCH <sub>2</sub> <sup>1</sup> FeCH <sub>3</sub> <sup>+</sup> <sup>1</sup> HFeCO	<sup>1</sup> FeNH <sup>1</sup> HFeNH <sub>2</sub> <sup>1</sup> FeNH <sub>3</sub> <sup>+2</sup>	<sup>1</sup> FeO <sup>1</sup> HFeOH <sup>1</sup> FeOH <sub>2</sub> <sup>+2</sup>
tier 2			<sup>6</sup> Fe(CO) <sub>2</sub> <sup>+3</sup> <sup>6</sup> Fe(CO) <sub>3</sub> <sup>+3</sup> <sup>6</sup> Fe(CO) <sub>4</sub> <sup>+3</sup> <sup>6</sup> Fe(CO) <sub>5</sub> <sup>+3</sup> <sup>6</sup> Fe(CO) <sub>6</sub> <sup>+3</sup>	<sup>6</sup> Fe(NH <sub>3</sub> ) <sub>2</sub> <sup>+3</sup> <sup>6</sup> Fe(NH <sub>3</sub> ) <sub>3</sub> <sup>+3</sup> <sup>6</sup> Fe(NH <sub>3</sub> ) <sub>4</sub> <sup>+3</sup> <sup>6</sup> Fe(NH <sub>3</sub> ) <sub>5</sub> <sup>+3</sup> <sup>6</sup> Fe(NH <sub>3</sub> ) <sub>6</sub> <sup>+3</sup>	<sup>6</sup> Fe(H <sub>2</sub> O) <sub>2</sub> <sup>+3</sup> <sup>6</sup> Fe(H <sub>2</sub> O) <sub>3</sub> <sup>+3</sup> <sup>6</sup> Fe(H <sub>2</sub> O) <sub>4</sub> <sup>+3</sup> <sup>6</sup> Fe(H <sub>2</sub> O) <sub>5</sub> <sup>+3</sup> <sup>6</sup> Fe(H <sub>2</sub> O) <sub>6</sub> <sup>+3</sup>

**Scheme 1.** Schematic Representation of the Geometrical Parameters of the Set of Tier 3 Molecules for M = Ti, Fe, Co, and Ni<sup>a</sup>



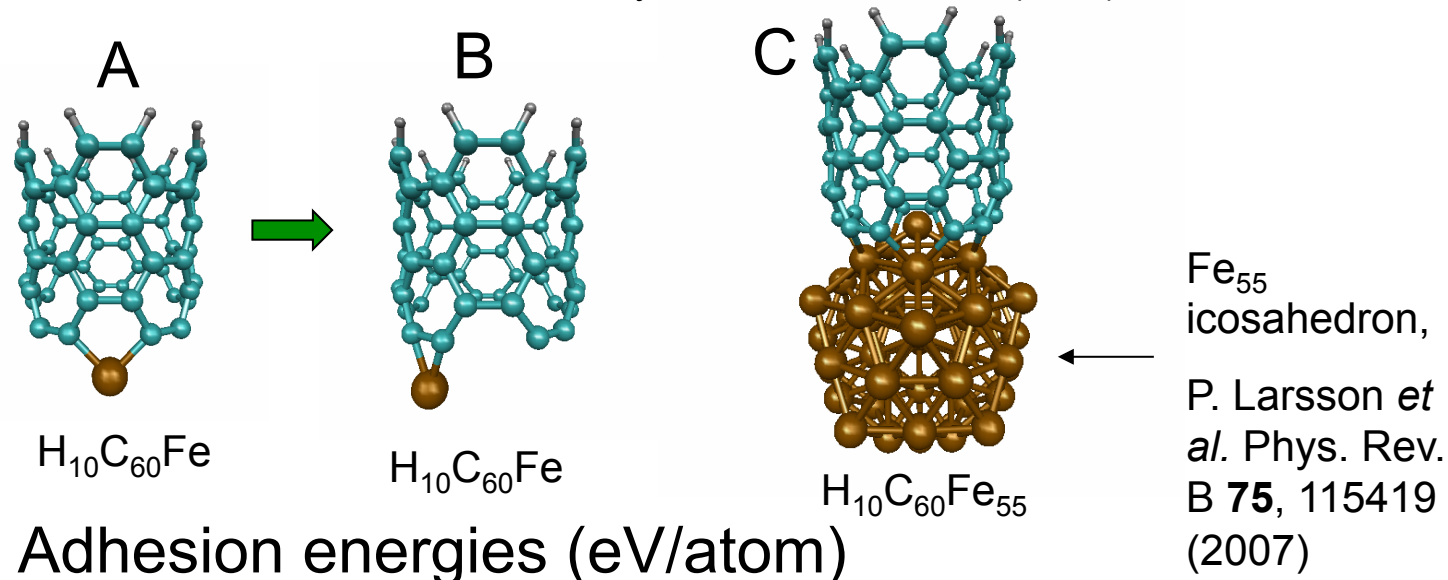
Bond lengths:  $\sim 0.1 \text{ \AA}$

Bond angles:  $\sim 10^\circ$

Relative energies:  $\sim 20 \text{ kcal/mol}$

## (5,5) armchair SWNT (H<sub>10</sub>C<sub>60</sub>) + Fe / Fe<sub>55</sub>

Y. Ohta, Y. Okamoto, SI, K. Morokuma, Phys. Rev. B **79**, 195415 (2009)



	A	B	C
DFT:PW91 <sup>[1]</sup>	-6.24	-5.63	-1.82
SCC-DFTB <sup>[2]</sup>	-5.17	-4.68	-1.86

Relative  
energies often  
OK!

[1] Phys. Rev. B **75**, 115419 (2007)    [2] Fermi broadening=0.13 eV

[1]: PW91: An ultrasoft pseudopotential with a plane-wave cutoff of 290 eV for the single metal and the projector augmented wave method with a plane-wave cutoff of 400 eV for the metal cluster    20

{2} Fe-Fe and Fe-C DFTB parameters from: G. Zheng *et al.*, *J. Chem. Theor. Comput.* **3**, 1349 (2007)

## MD for Chemical Reactions

Newton's equations of motion for the  $N$ -particle system:

$$\mathbf{F}_i = m_i \ddot{\mathbf{r}}_i$$

$E$  is a potential energy function  
In our case: DFTB total electronic energy

$\mathbf{F}_i$  can be calculated as  $-\partial E / \partial \mathbf{r}_i$ . There are several approximate methods to solve this system of equations. Some commonly used methods are:

Verlet's algorithm

Beeman's algorithm

Velocity Verlet algorithm:

$$\mathbf{r}_i(t + \delta t) = \mathbf{r}_i(t) + \delta t \mathbf{v}_i(t) + (\delta t)^2 \frac{\mathbf{F}_i(t)}{2m_i}$$

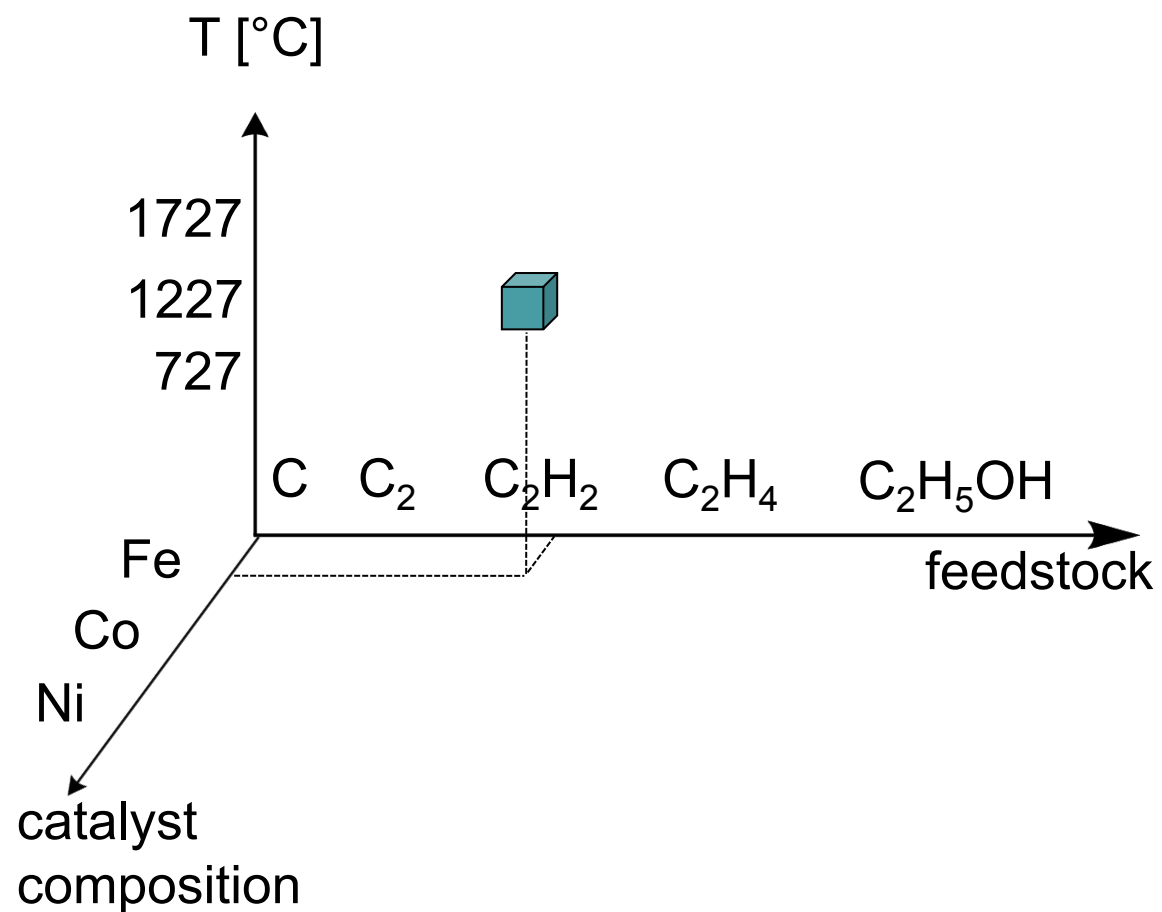
$$\mathbf{v}_i(t + \delta t) = \mathbf{v}_i(t) + \delta t \frac{\mathbf{F}_i(t + \delta t) + \mathbf{F}_i(t)}{2m_i}$$

Practical implementation requires discrete  $\Delta t$

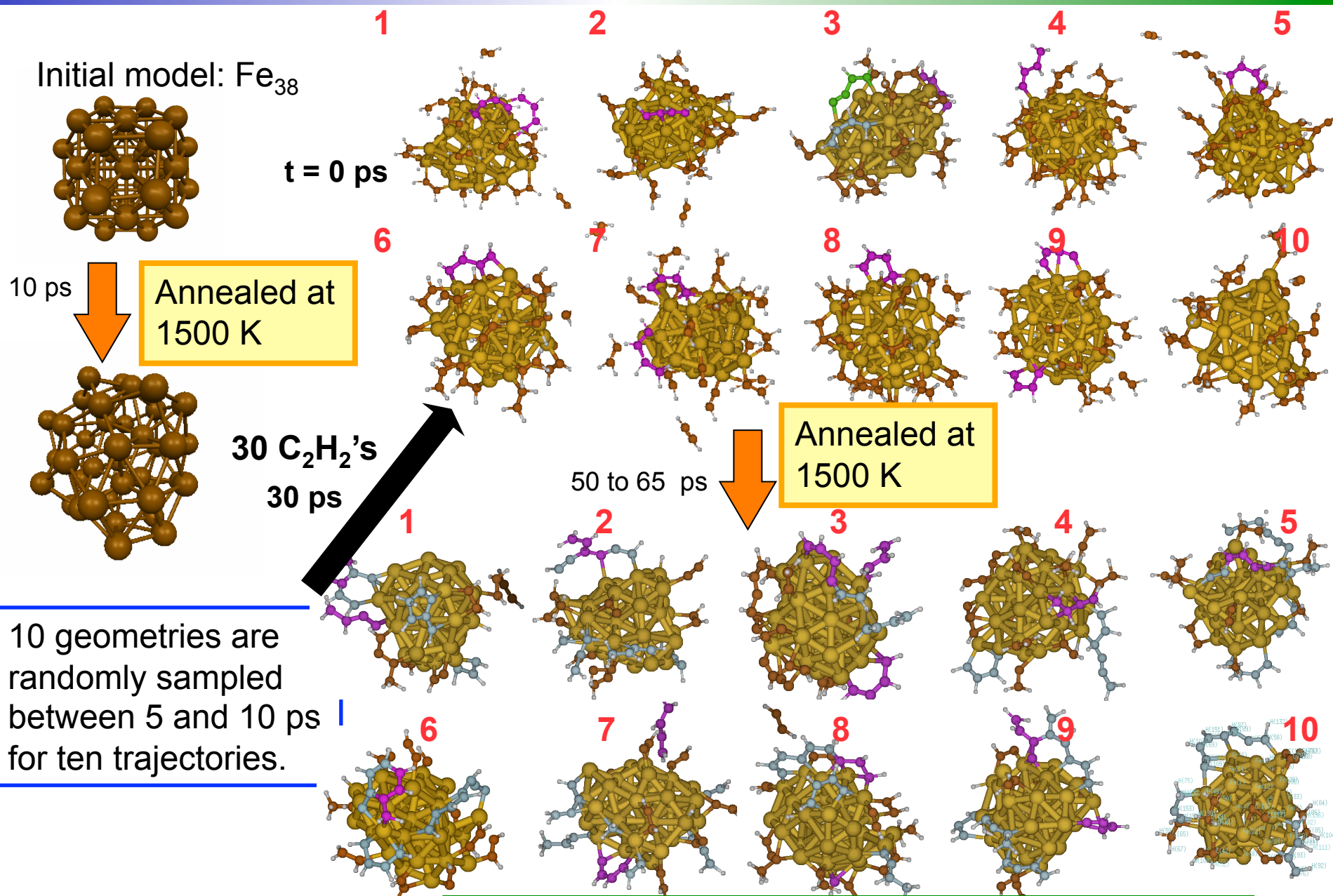


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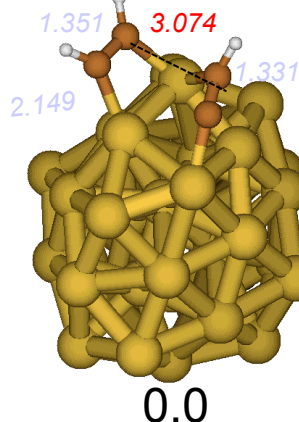
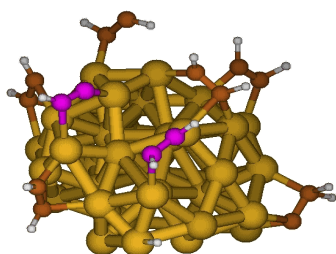
Dr. Ying Wang



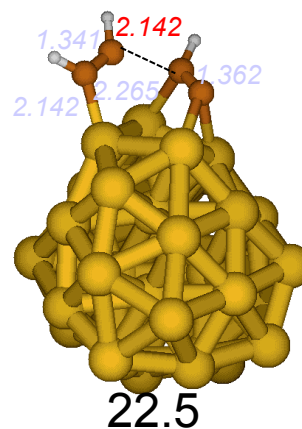
Polyacetylene formation, largest carbon cluster: C<sub>10</sub>H<sub>x</sub>



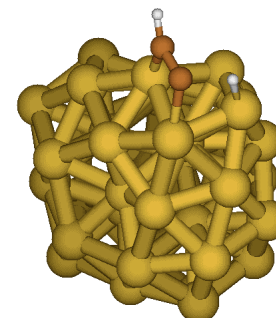
**C-C Bond formation:**



0.0  
NImag=0

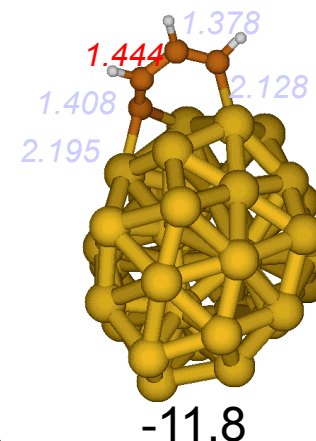


22.5  
NImag=1  
 $\nu_{imag} = 455i \text{ cm}^{-1}$

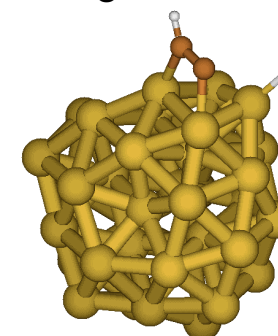


36.5

NImag=1  
 $\nu_{imag} = 1377i \text{ cm}^{-1}$



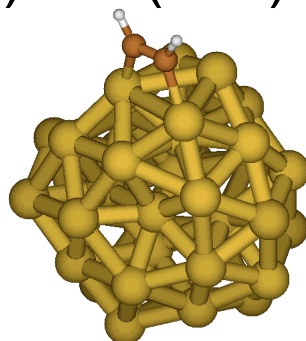
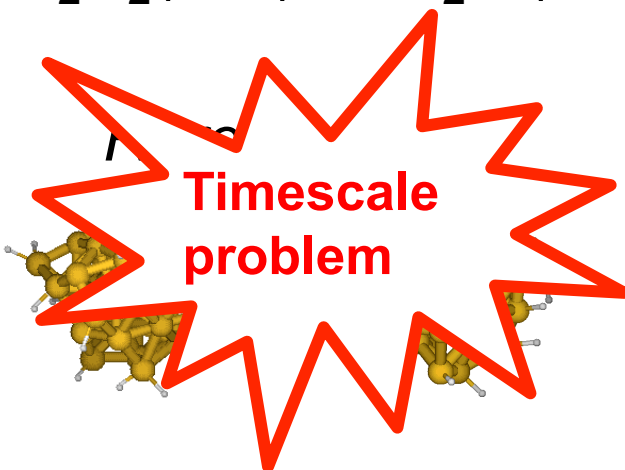
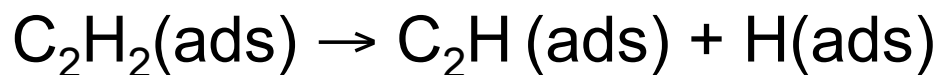
-11.8  
NImag=0



8.0  
NImag=0

Relative energies in [kcal/mol]  
including ZPE  
IRC verified

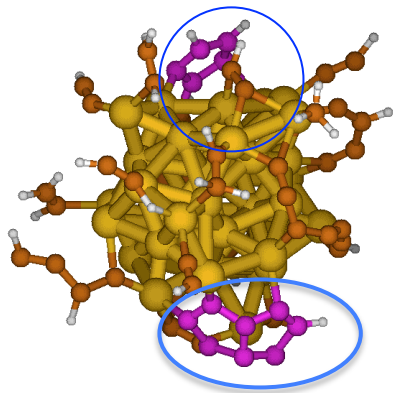
**H abstraction:**



0.0  
NImag=0

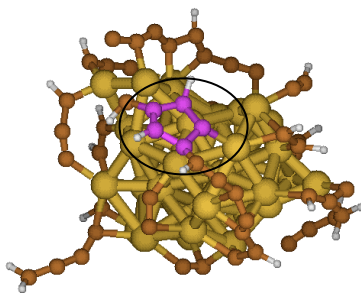
$C_2H_2$  supply/2H removal (every 5 ps until 60 carbon atoms attached)

A



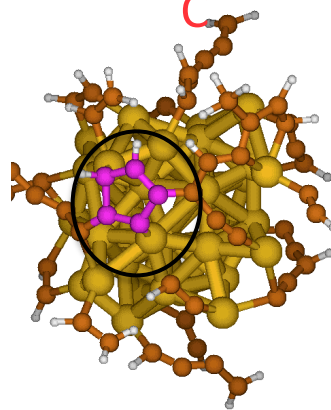
55ps

B



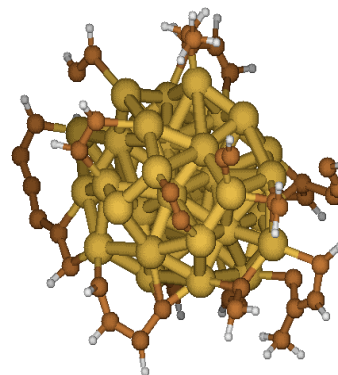
60ps

C



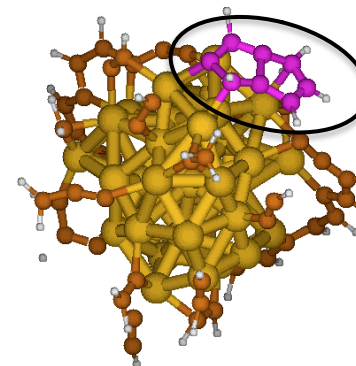
45ps

D



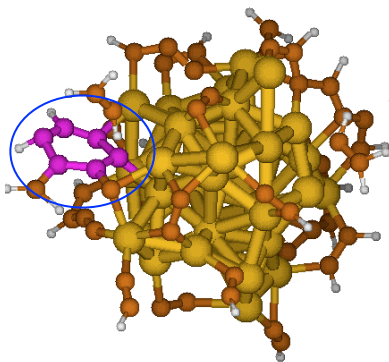
40ps

E



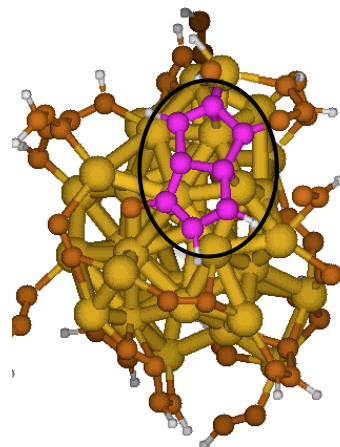
40ps

F



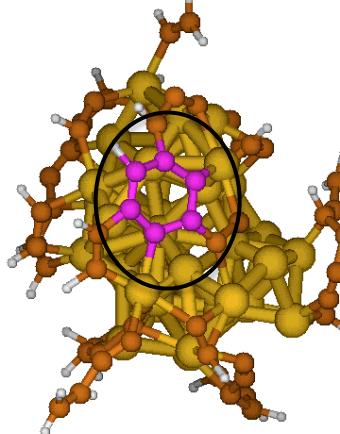
55ps

G



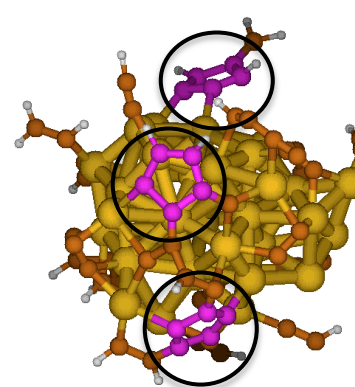
60ps (61 C)

H



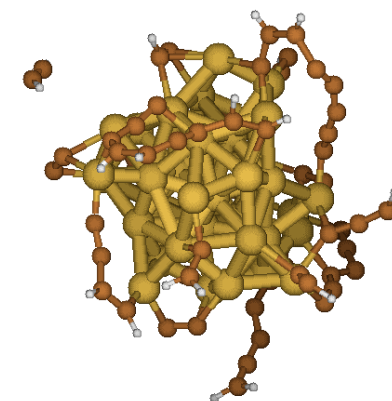
55ps

I



65ps

J

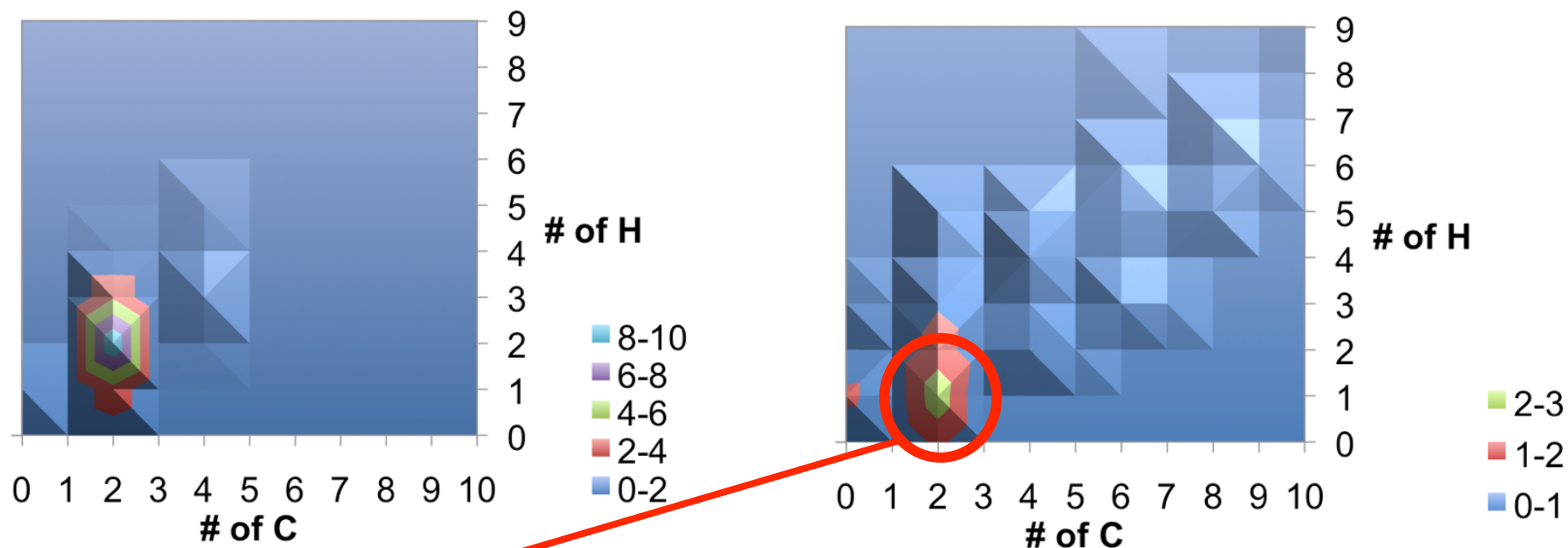
75ps  
(61 C)

## $C_xH_y$ composition on $Fe_{38}$ cluster

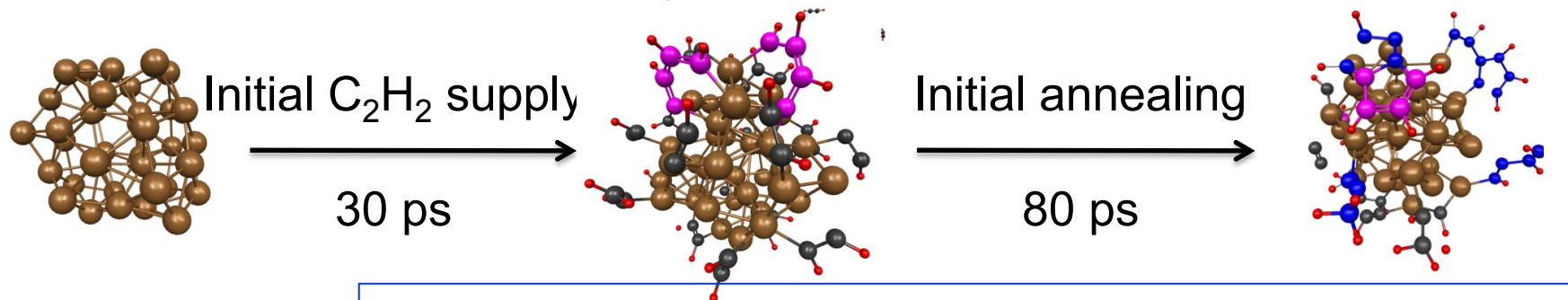
### BEFORE

### AFTER

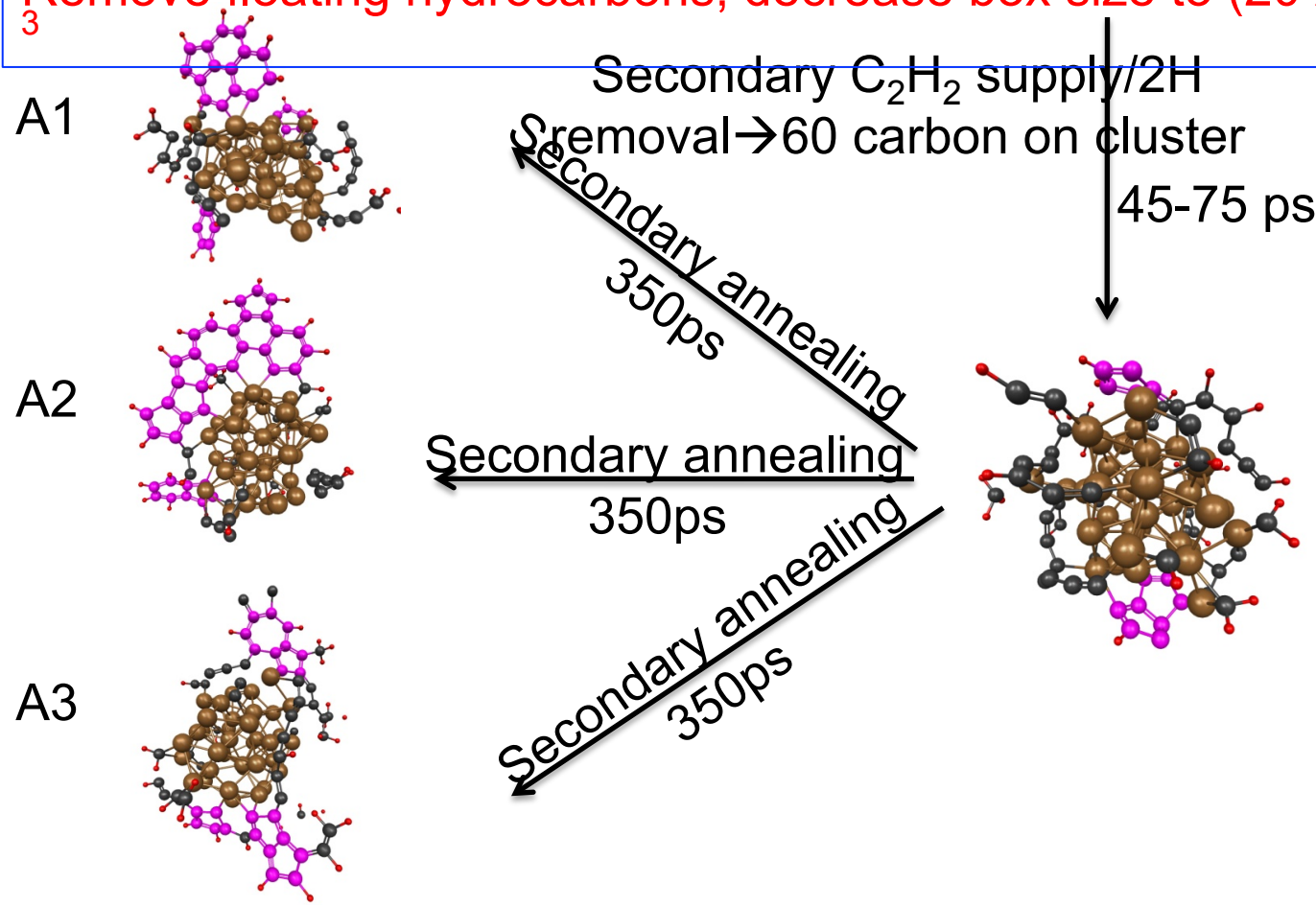
$C_2H_2$  supply/2H **removal** (every 5 ps until 60 carbon atoms attached)

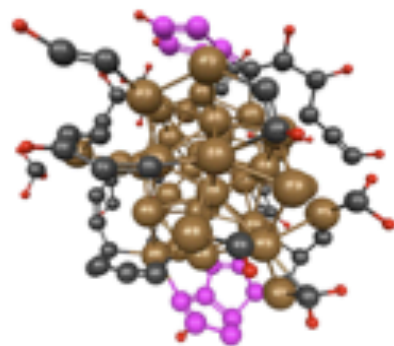
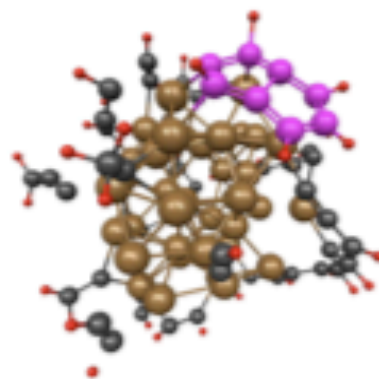
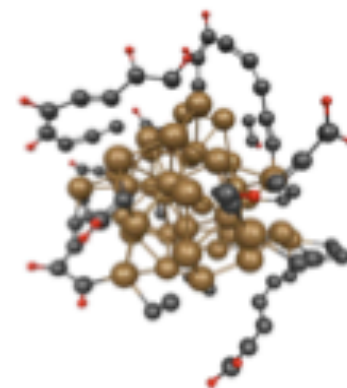


$\cdot C_2H$  radicals are consumed/re-generated!  
“dissipative small molecule organocatalyst”

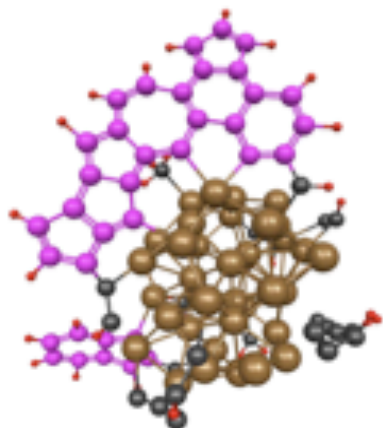


Remove floating hydrocarbons, decrease box size to (20 Å)<sup>3</sup>



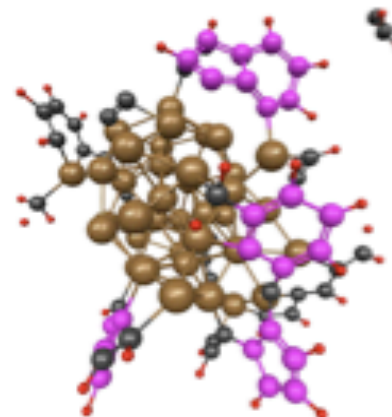
**“Final results” after secondary annealing**A  
 $\text{Fe}_{38}\text{C}_{60}\text{H}_{33}/55\text{ps}$ E  
 $\text{Fe}_{38}\text{C}_{60}\text{H}_{42}/40\text{ps}$ J  
 $\text{Fe}_{38}\text{C}_{61}\text{H}_{19}/75\text{ps}$ 

a)

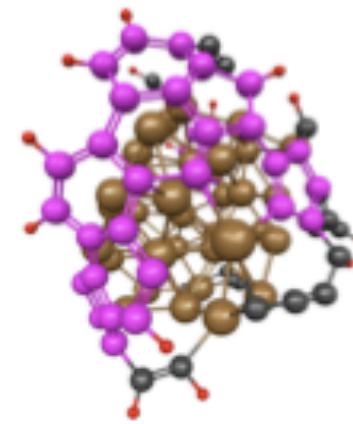
Annealed at  
1500 KA2  
 $\text{Fe}_{38}\text{C}_{60}\text{H}_{33}/515\text{ps}$ 

b)

“standing wall”

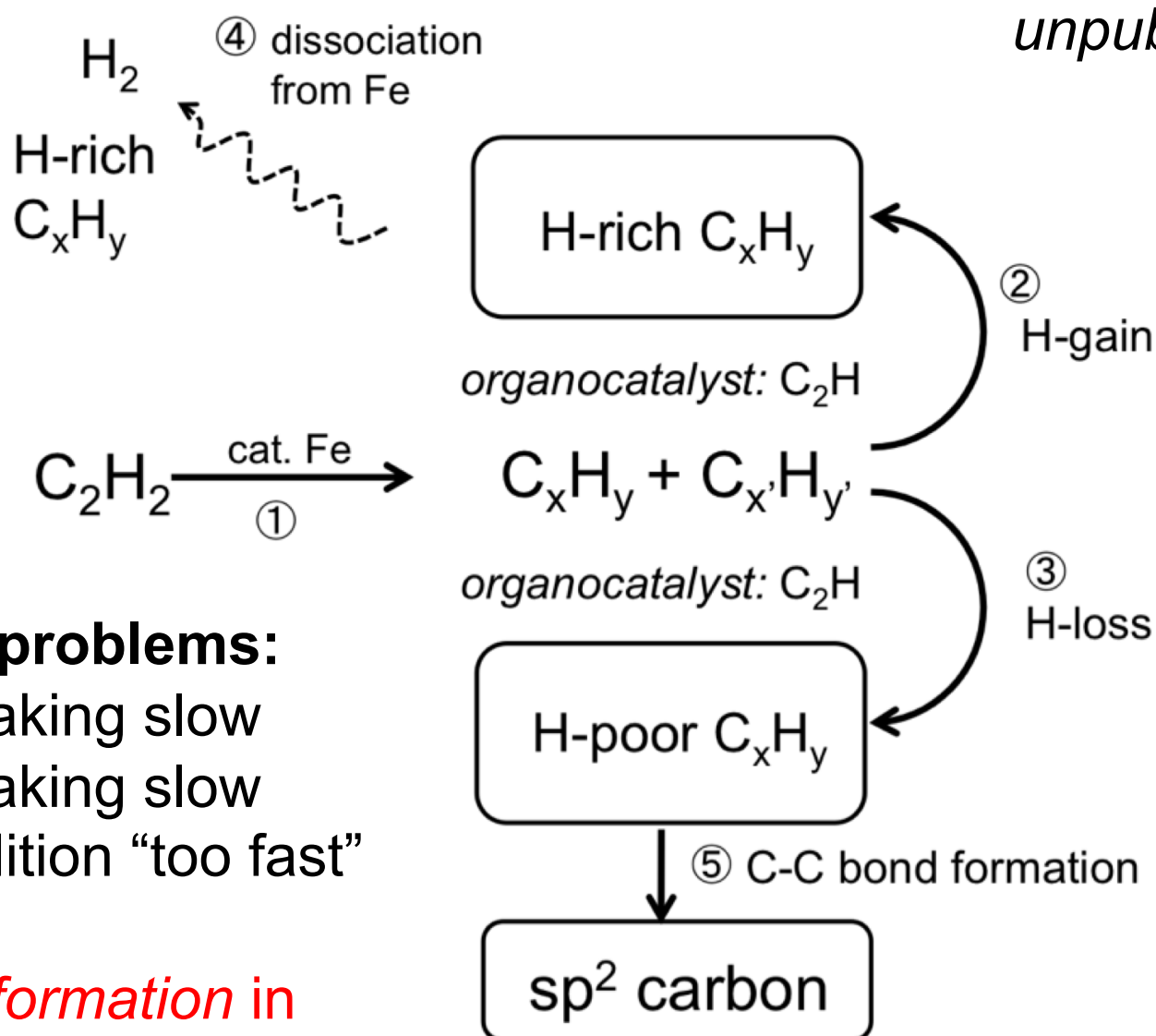
E2  
 $\text{Fe}_{38}\text{C}_{60}\text{H}_{42}/500\text{ps}$ 

“PAHs”

J1  
 $\text{Fe}_{38}\text{C}_{61}\text{H}_{19}/535\text{ps}$ 

“cap”

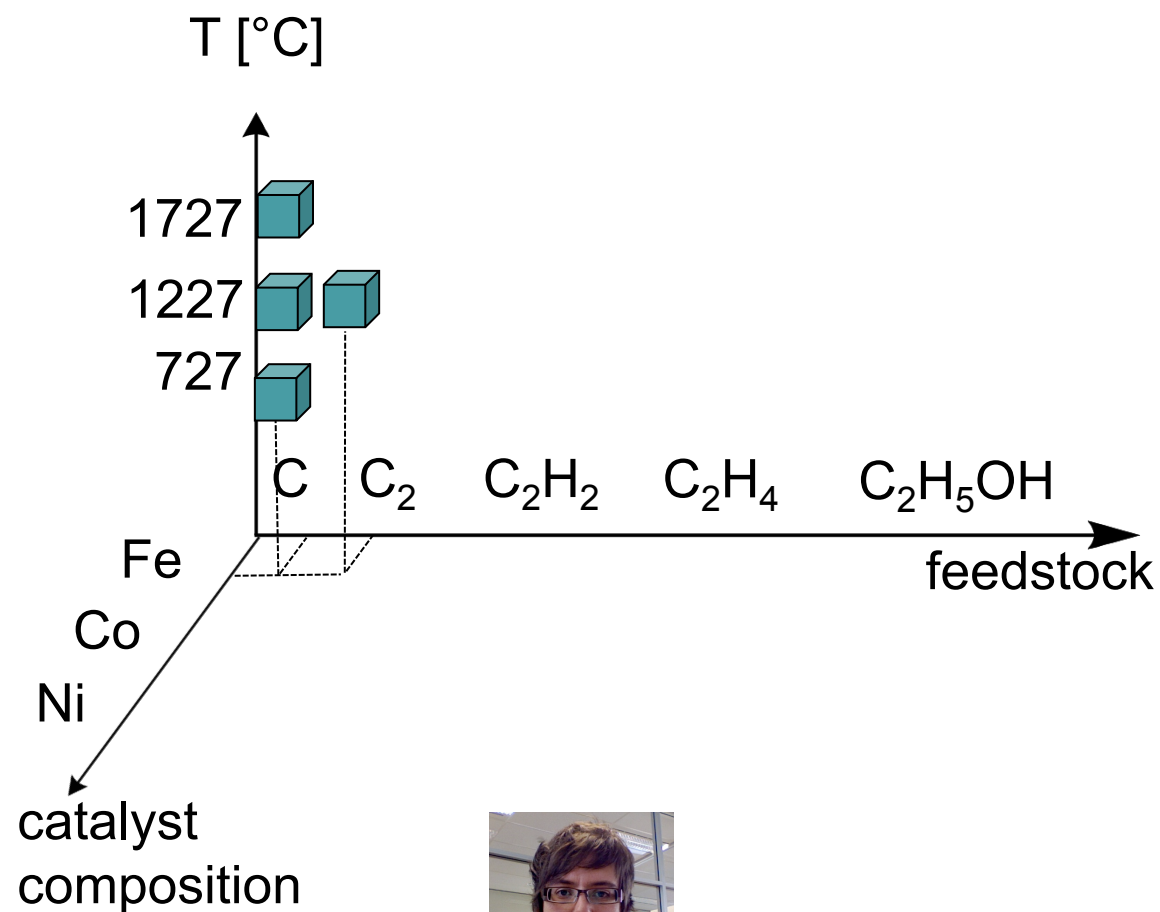
# “Disproportionation Mechanism” of Acetylene Decomposition



## Fundamental problems:

- C-C bond breaking slow
- C-H bond breaking slow
- Acetylene addition “too fast”

→ *No carbide formation in simulations*



Dr. Yasuhito Ohta



Dr. Alister J. Page



Dr. Yoshiko Okamoto

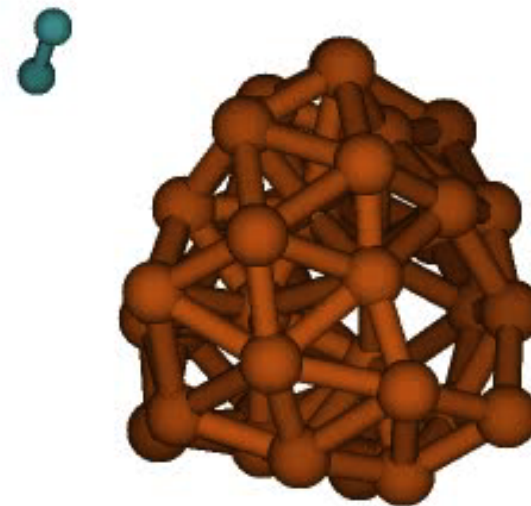


Dr. Joonghan Kim

## $C_2$ shooting and annealing on $Fe_{38}$ particle

Y. Ohta, Y. Okamoto, A. J. Page, SI, K. Morokuma, ACS Nano **3**, 3413 (2009)

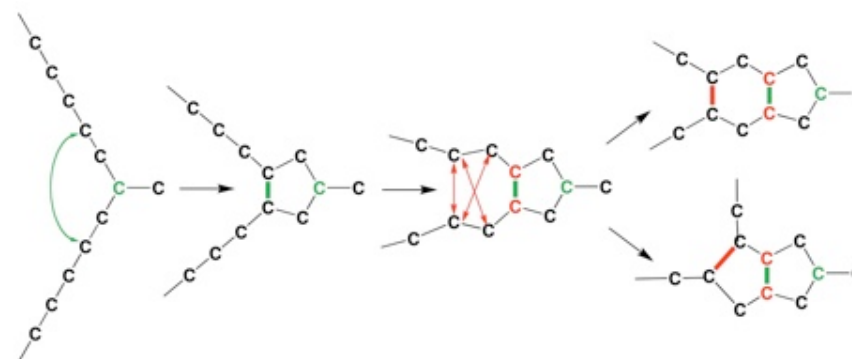
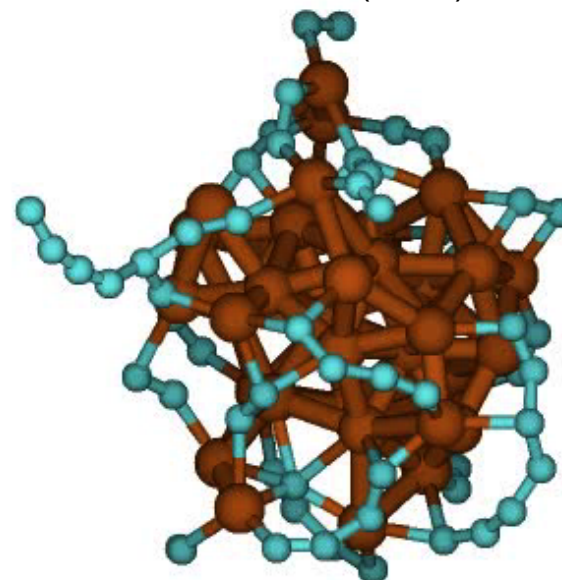
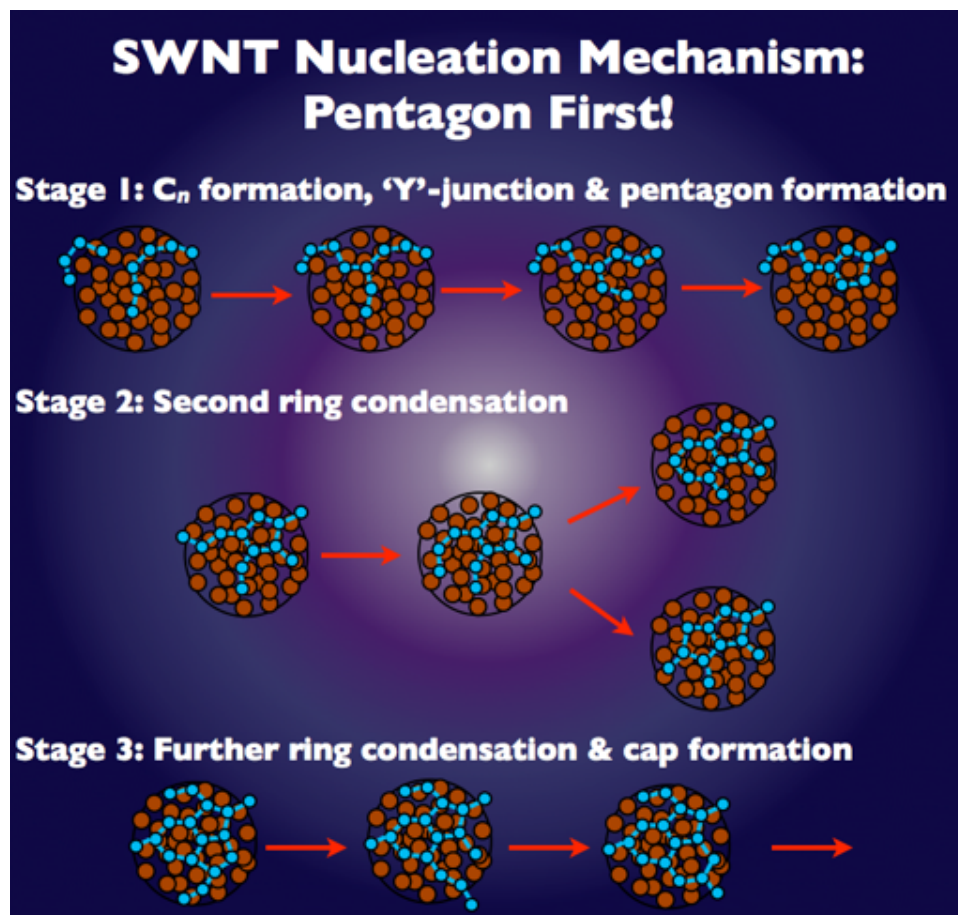
- SCC-DFTB;  $T_e = 10,000$  K.
- MD;  $\Delta t = 1$  fs.
- NVT ensemble;  $T_n = 1,500$  K.
- Nosé-Hoover-Chain thermostat.
- 30  $C_2$  deposited onto fcc- $Fe_{38}$  surface (1/ps).
- NVT thermal annealing for 400 ps.





# C<sub>2</sub> shooting and annealing on Fe<sub>38</sub> particle

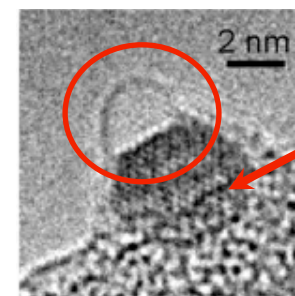
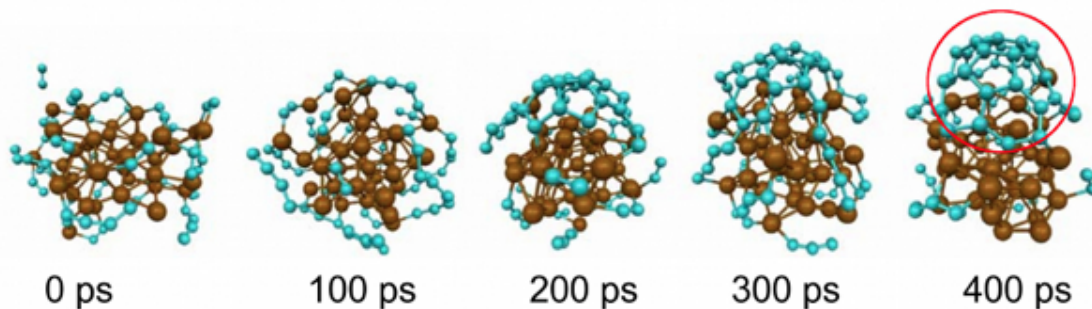
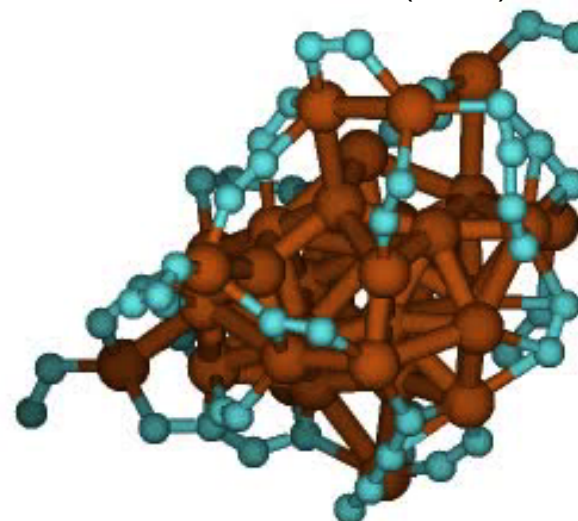
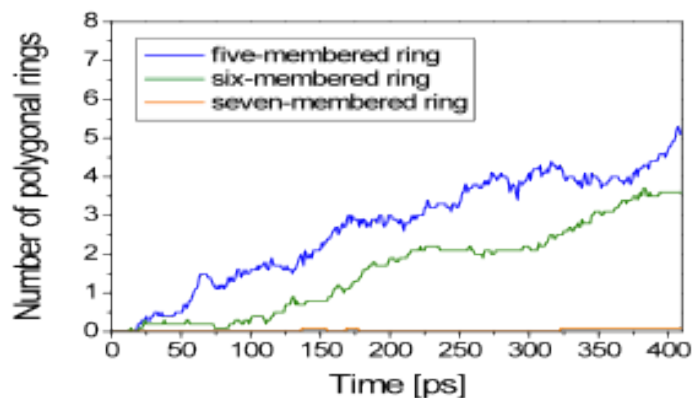
Y. Ohta, Y. Okamoto, A. J. Page, SI, K. Morokuma, ACS Nano 3, 3413 (2009)



# C<sub>2</sub> shooting and annealing on Fe<sub>38</sub> particle

Y. Ohta, Y. Okamoto, A. J. Page, SI, K. Morokuma, ACS Nano **3**, 3413 (2009)

SWNT nucleation:  
driven by 5-/6-membered ring formation



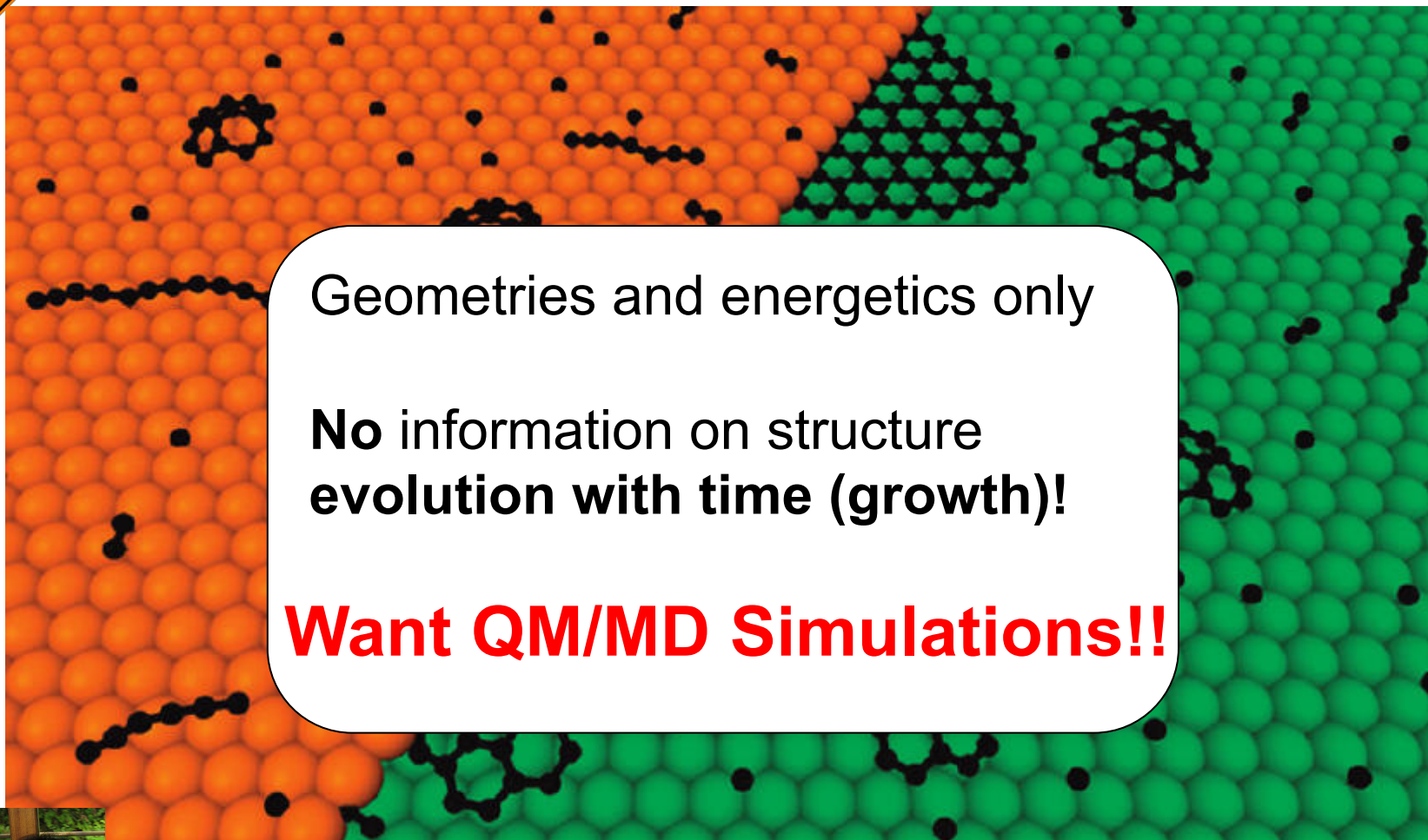
Fe<sub>3</sub>C nanoparticle

Yoshida *et al.*, *Nano. Lett.* (2008)

SWNT 'cap' formed **without** carbide phase... (again!)



## Detour: How Does Graphene Form on Ni(111)?



Geometries and energetics only

**No information on structure evolution with time (growth)!**

**Want QM/MD Simulations!!**

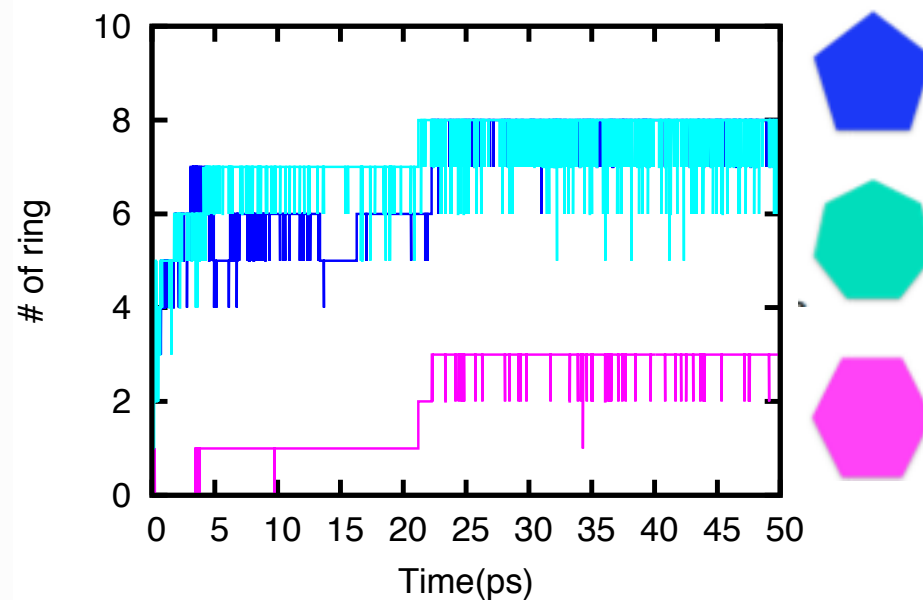
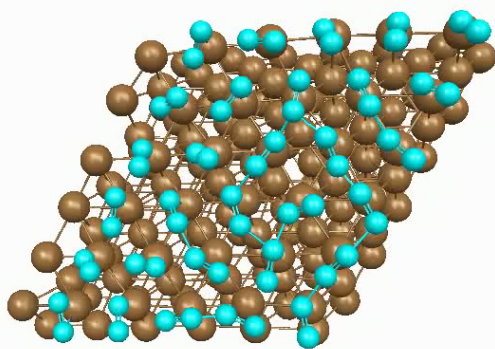
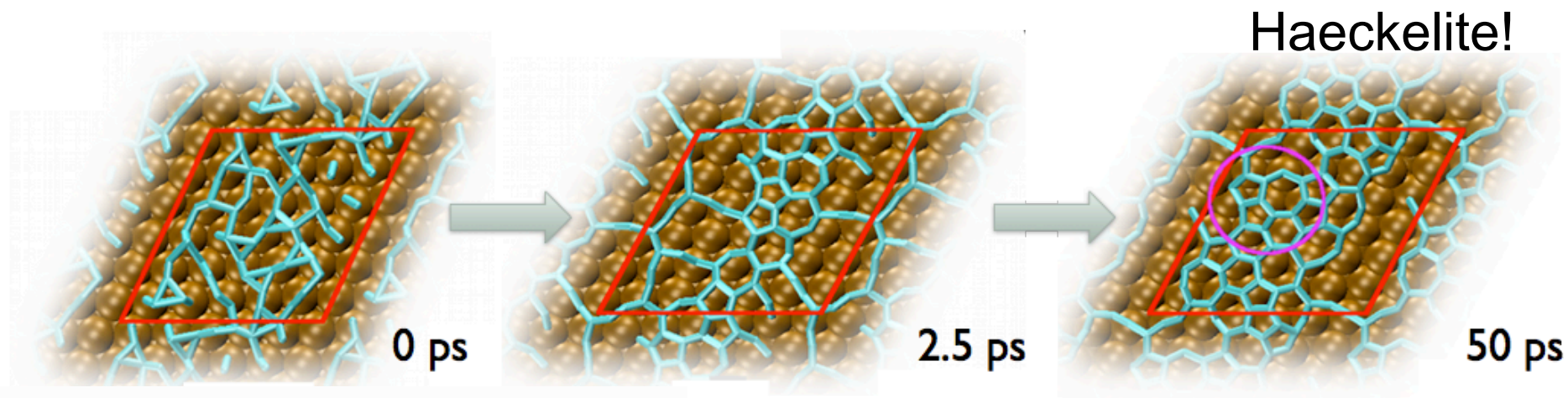


Dr. Ying Wang

Image source:  
Gao *et al.* J. Am. Chem. Soc. **133**, 5009 (2011), static DFT calculations

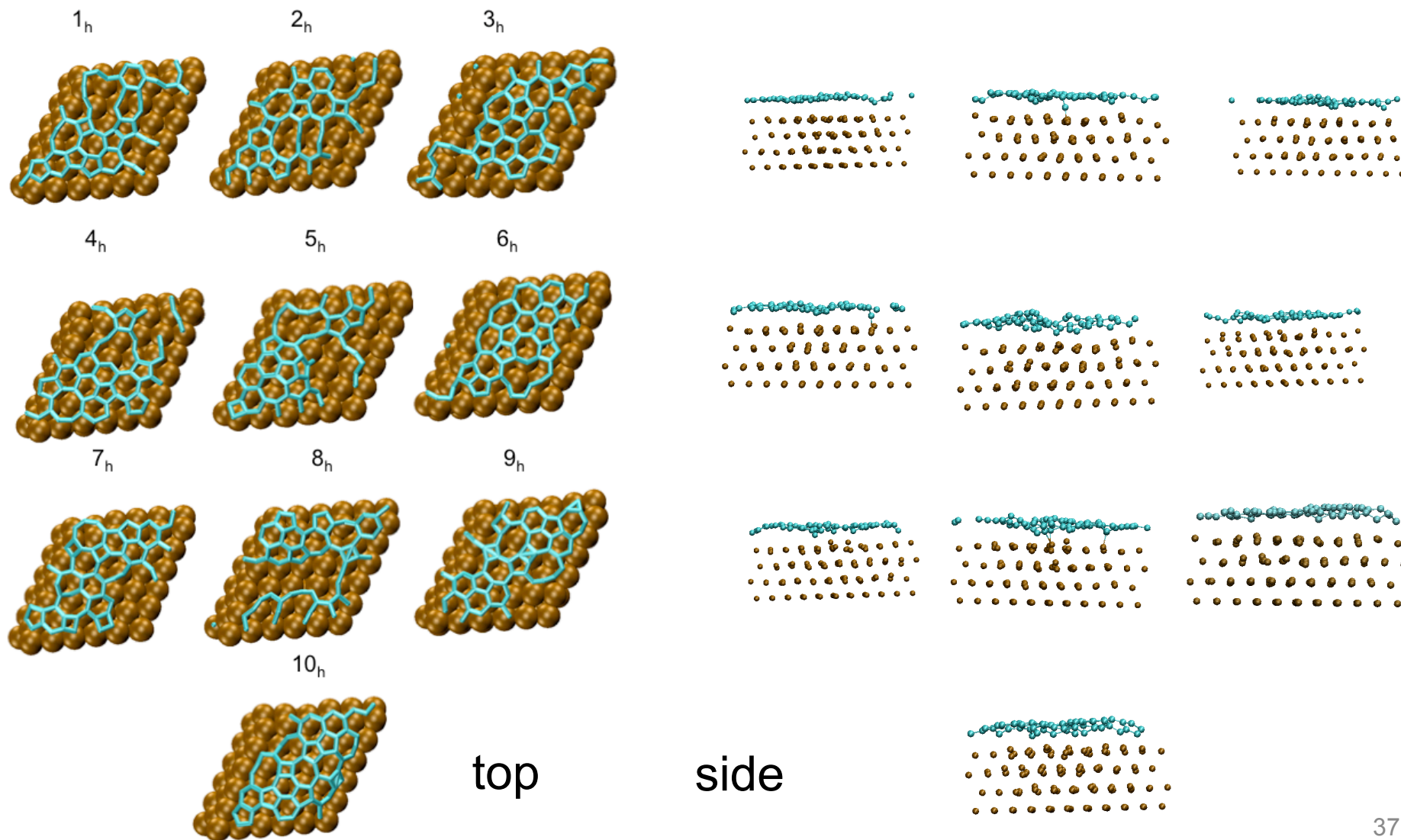
## QM/MD of 30 C<sub>2</sub> on Ni(111), 1180 K

Y. Wang, A. J. Page, Y. Nishimoto, H.-J. Qian, SI, K. Morokuma, *J. Am. Chem. Soc.* **133**, 18837 (2011)

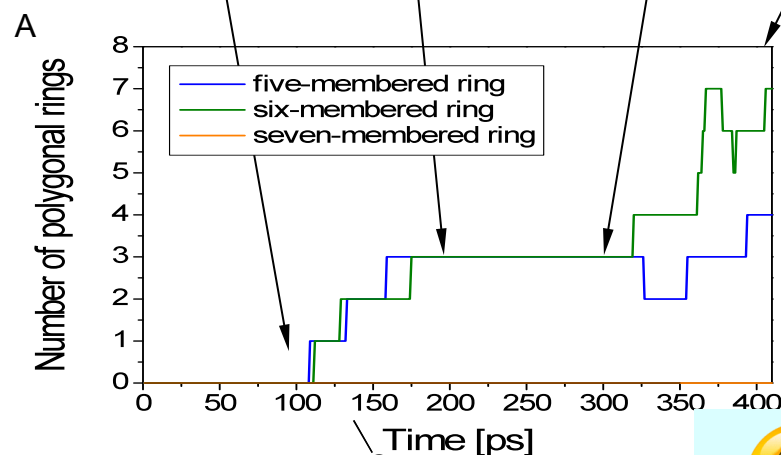
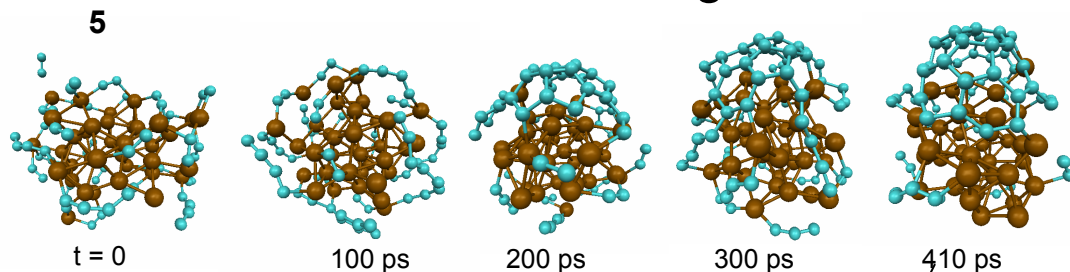


# QM/MD of 30 C<sub>2</sub> on Ni(111), 1180 K

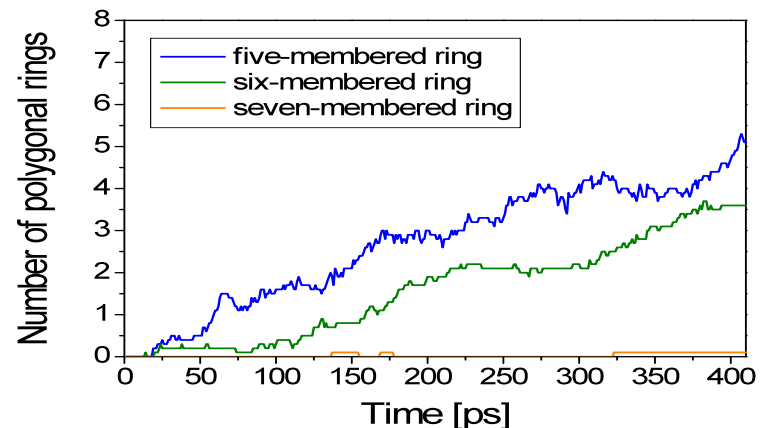
Y. Wang, A. J. Page, Y. Nishimoto, H.-J. Qian, SI, K. Morokuma, *J. Am. Chem. Soc.* **133**, 18837 (2011)



Y. Ohta, Y. Okamoto, A. J. Page, SI, K. Morokuma, ACS Nano **3**, 3413 (2009)

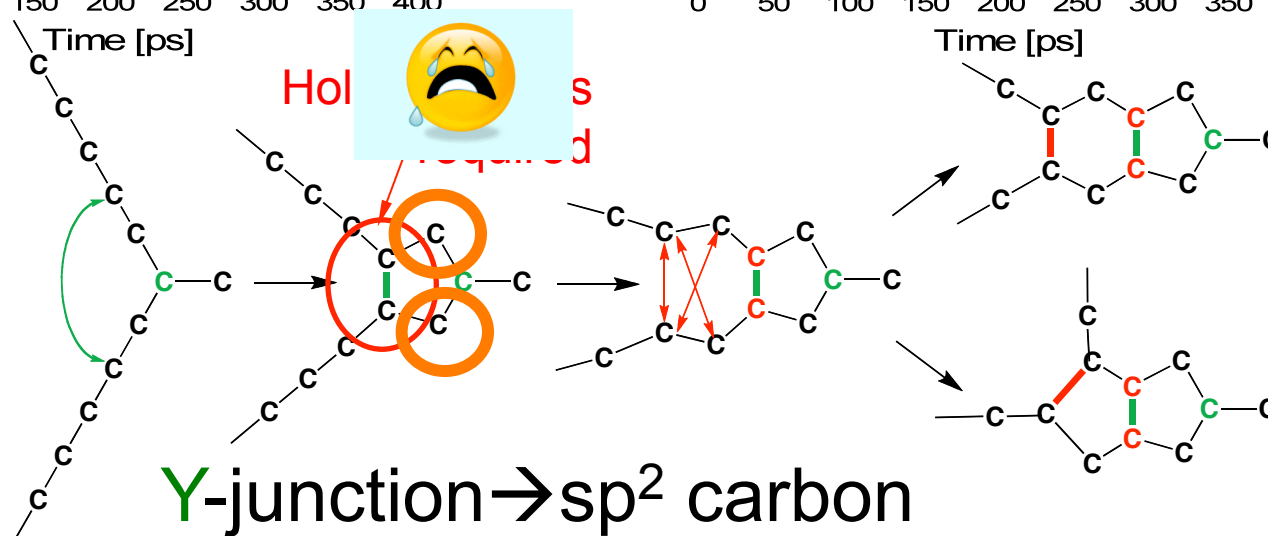


Average 5- and 6-ring counts over 10 annealing trajectories



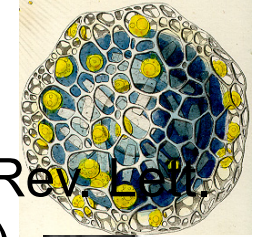
Formation of first condensed 2-ring system (5/5 or 5/6)

Always pentagon first!



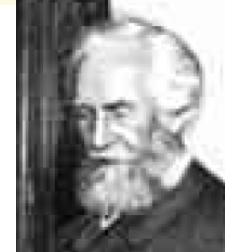
# Haeckelite

Radiolara

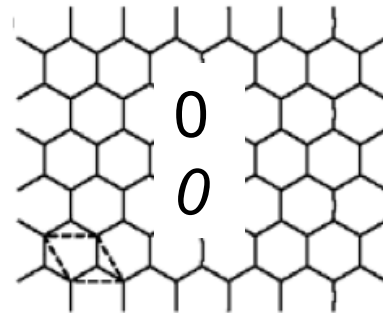


Crespi *et al.* Phys. Rev. B **53**, R13303 (1996); Terrones *et al.* Phys. Rev. B **62**, 1716 (2000); Rocquefelte *et al.* Nano Lett. **4**, 805 (2004)

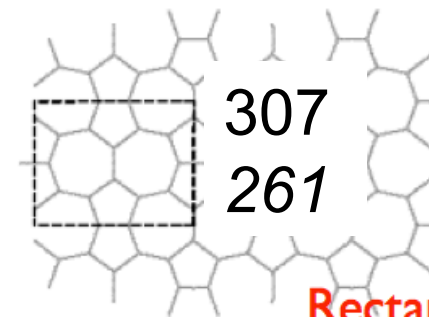
## Throner-Stone-Wales Transformation



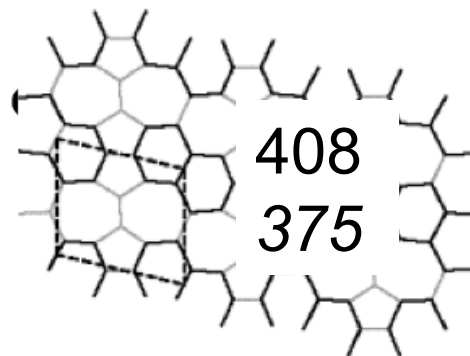
Ernst Haeckel (1834-1919)



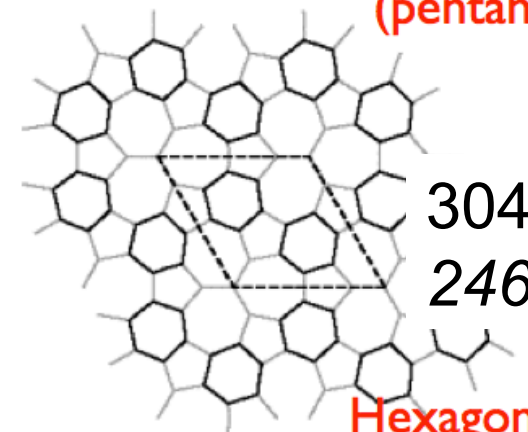
Graphene



Rectangular,  $R_{5,7}$  (pentaheptite)



Oblique,  $R_{5,6,7}$



Hexagonal,  $H_{5,6,7}$

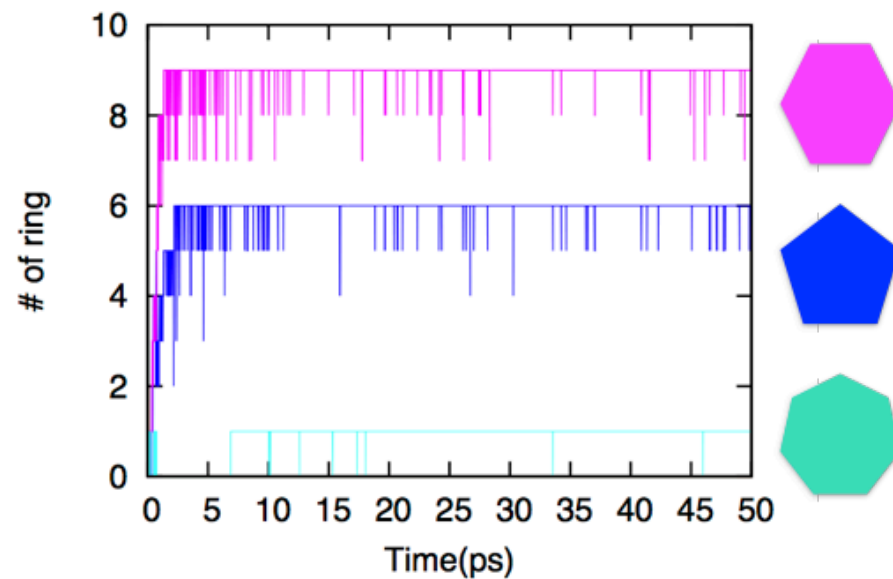
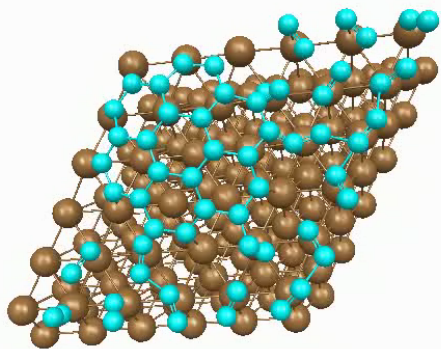
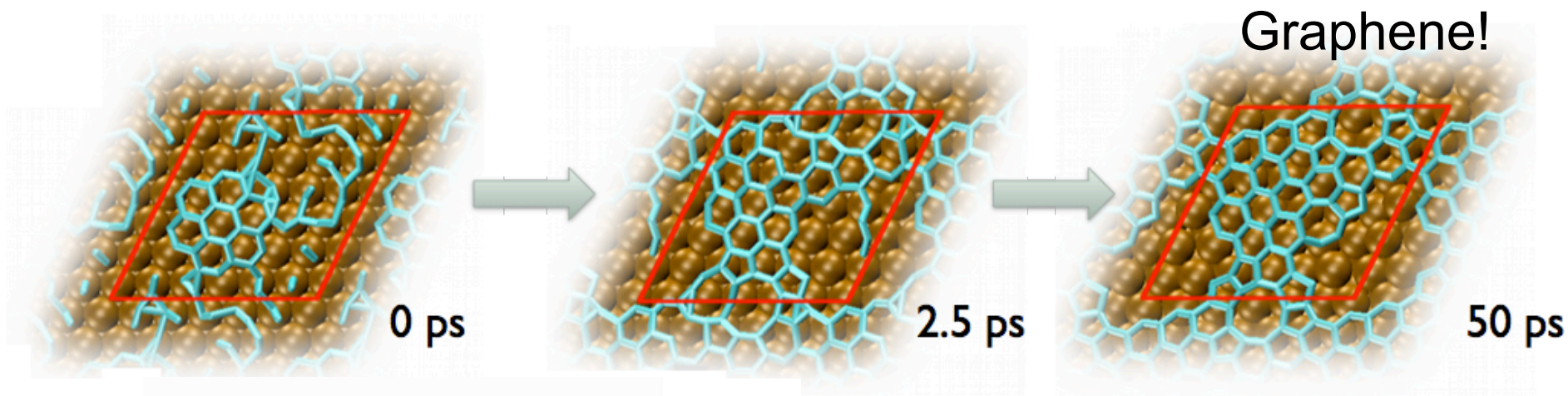
$\Delta E(TB)$  (meV/C atom)

$\Delta E(PBE)$  (meV/C atom)

$C_{60}$ : 419  
380

# QM/MD of 18 C<sub>2</sub> + C<sub>24</sub> on Ni(111), 1180 K

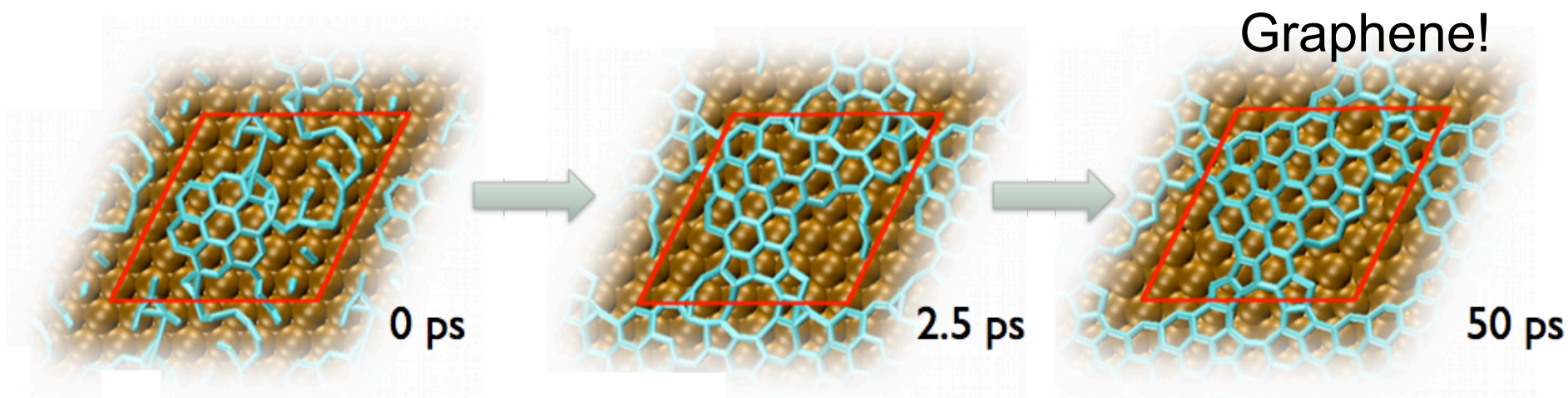
Y. Wang, A. J. Page, Y. Nishimoto, H.-J. Qian, S.I. K. Morokuma, *J. Am. Chem. Soc.* **133**, 18837 (2011)



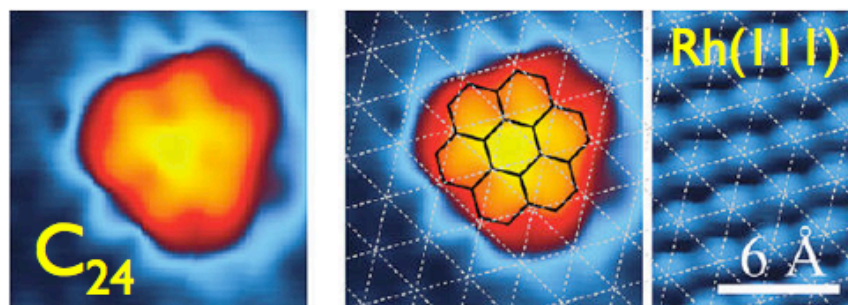


## QM/MD of 18 C<sub>2</sub> + C<sub>24</sub> on Ni(111), 1180 K

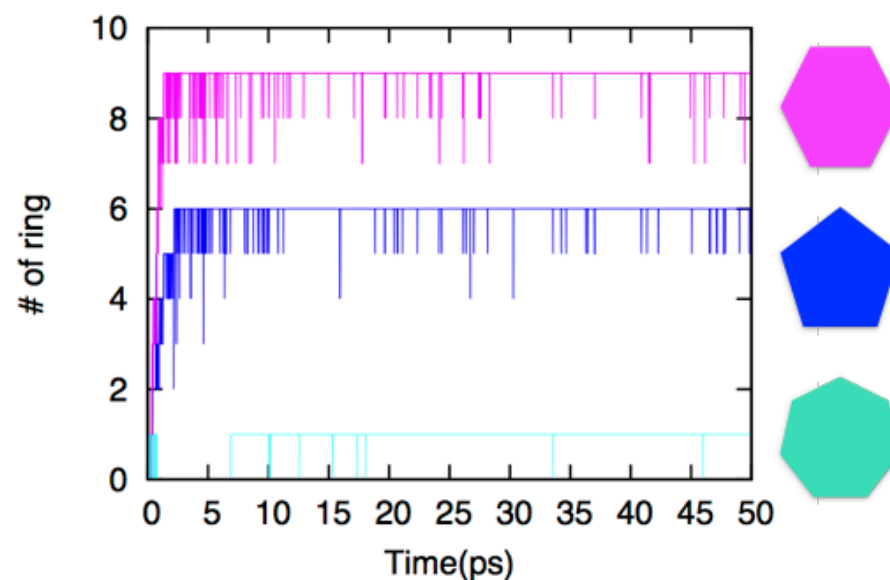
Y. Wang, A. J. Page, Y. Nishimoto, H.-J. Qian, S.I. K. Morokuma, *J. Am. Chem. Soc.* **133**, 18837 (2011)



- Pentagon-first vs. **template effect**.
- Suppression of heptagons and pentagons

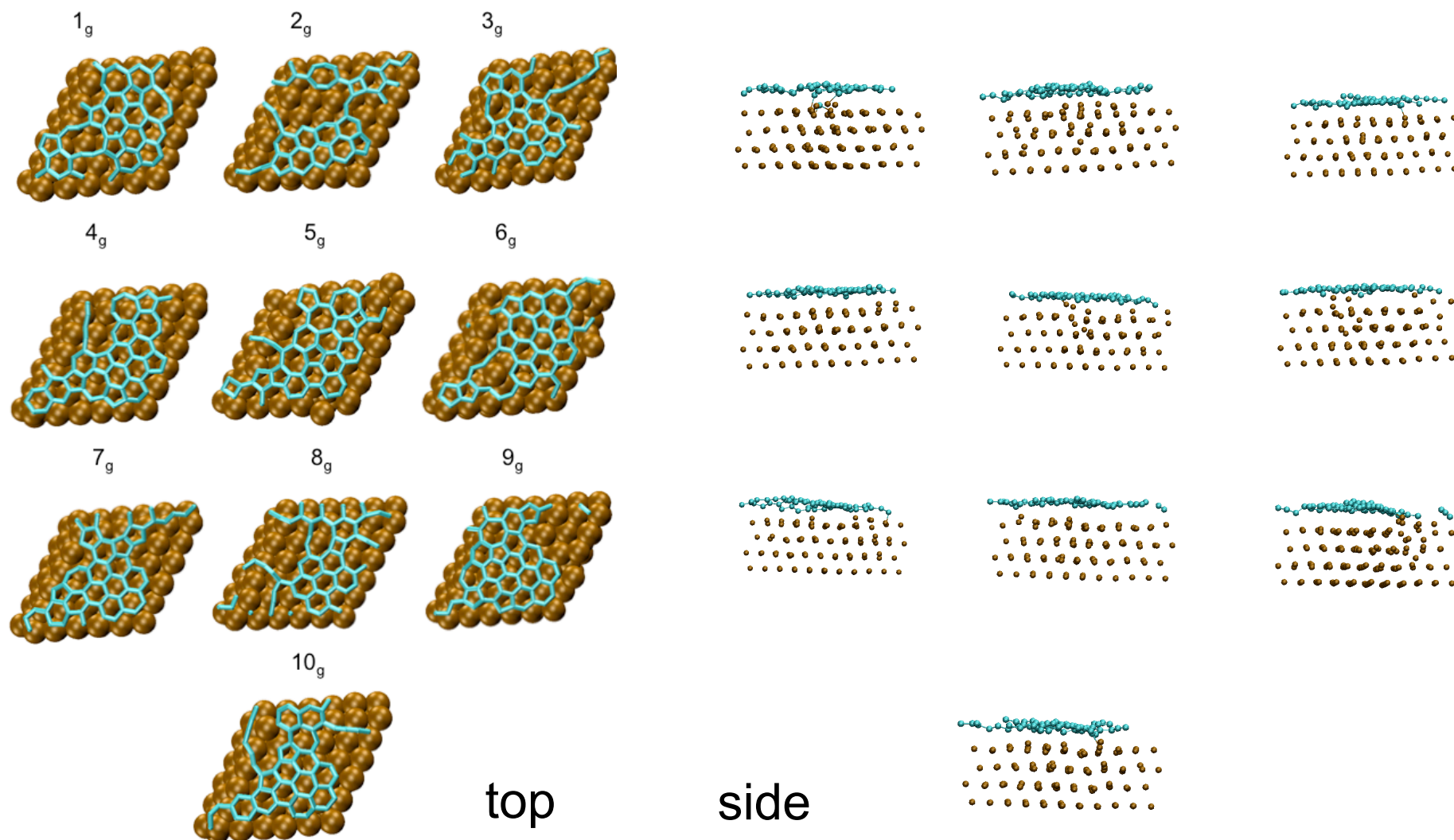


Wang *et al.*, *Nano Lett.*, (2011)

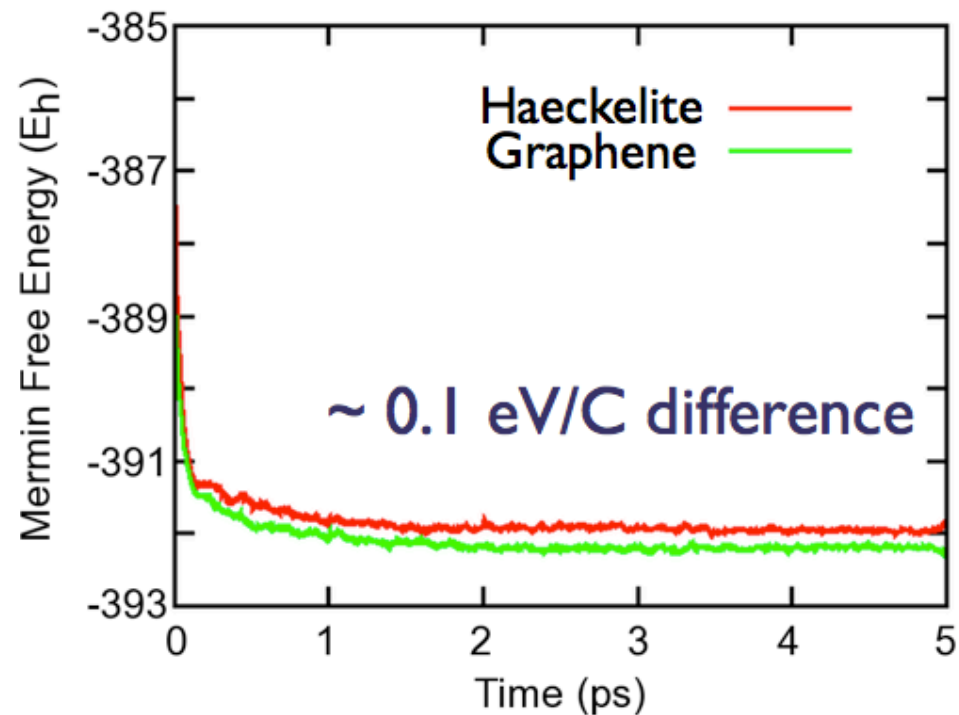
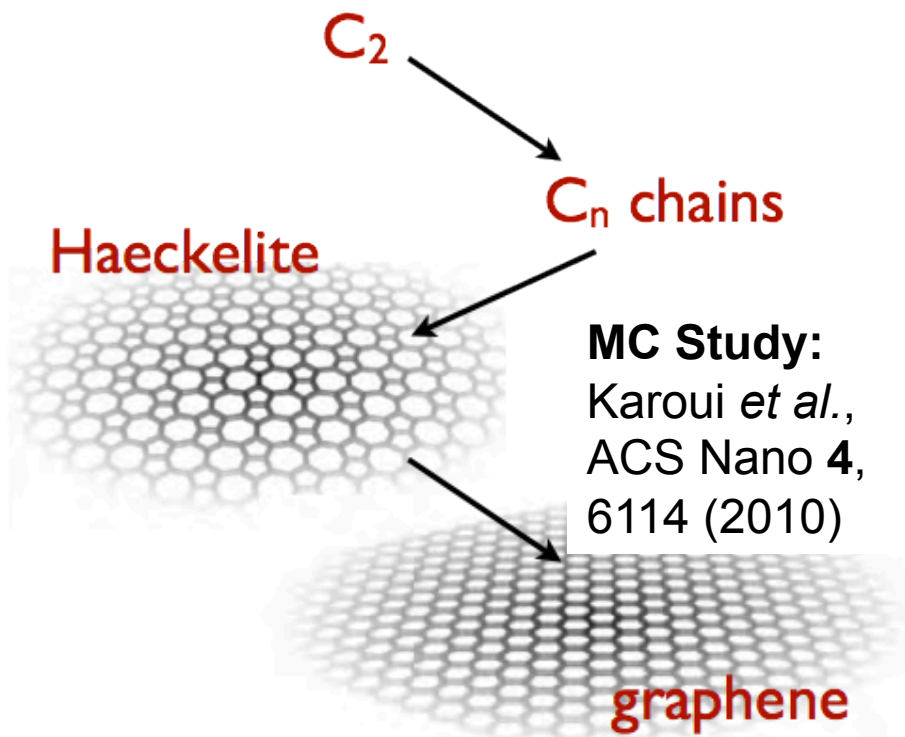


# QM/MD of 18 C<sub>2</sub> + C<sub>24</sub> on Ni(111), 1180 K

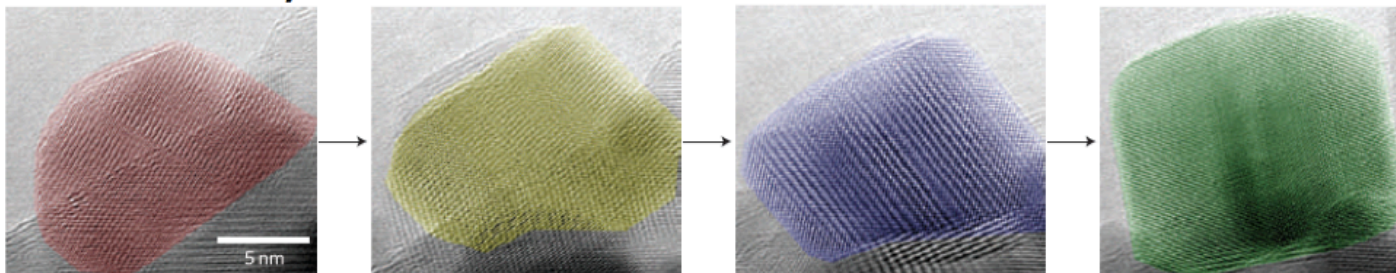
Y. Wang, A. J. Page, Y. Nishimoto, H.-J. Qian, S.I. K. Morokuma, *J. Am. Chem. Soc.* **133**, 18837 (2011)



# DFTB/MD: Haeckelite is a Metastable Phase



LiFePO<sub>4</sub> nanocrystal, 450 °C



Chung *et al.*, Nature Phys. (2008)

Ostwald's 'rule of stages'

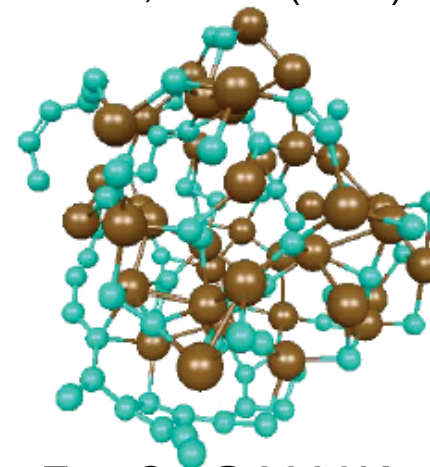


F. W. Ostwald,  
 Z. Phys. Chem.  
**22**, 289 (1897)<sup>43</sup>

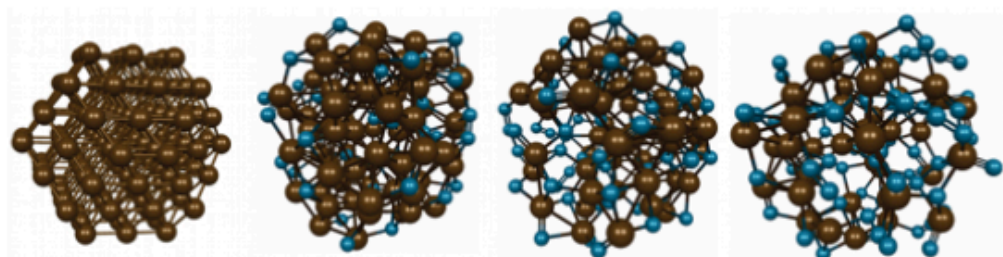
## Fe-Carbide Nanoparticle Precursor

A. J. Page, H. Yamane, Y. Ohta, SI, K. Morokuma, *J. Am. Chem. Soc.* **132**, 15699 (2010)

- SCC-DFTB;  $T_e = 10,000$  K.
- MD;  $\Delta t = 1$  fs.
- NVT ensemble;  $T_n = 800, 1,400$  &  $2,000$  K.
- Nosé-Hoover-Chain thermostat.
- fcc-Fe<sub>116</sub> nanoparticles.
- 'Random replacement' of 33, 50 and 66% Fe atoms.
- NVT thermal annealing for 300 ps.



Fe<sub>58</sub>C<sub>58</sub>@2000K-5

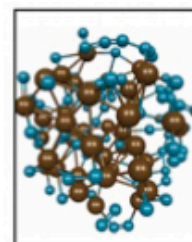


Fe<sub>116</sub>

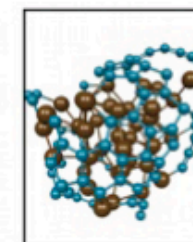
Fe<sub>77</sub>C<sub>39</sub>

Fe<sub>58</sub>C<sub>58</sub>

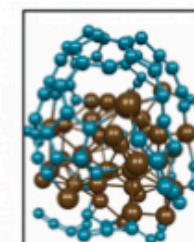
Fe<sub>39</sub>C<sub>77</sub>



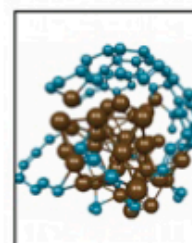
0 ps



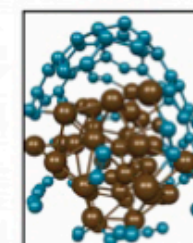
50.00 ps



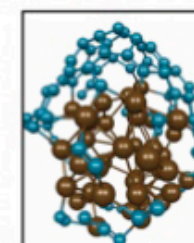
100.00 ps



150.00 ps



200.00 ps

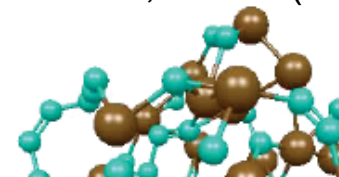


300.00 ps

Fe<sub>39</sub>C<sub>77</sub>@1400K-9

## Fe-Carbide Nanoparticle Precursor

A. J. Page, H. Yamane, Y. Ohta, SI, K. Morokuma, *J. Am. Chem. Soc.* **132**, 15699 (2010)



PRL **100**, 195502 (2008)

PHYSICAL REVIEW LETTERS

week ending  
16 MAY 2008

### Reduced Carbon Solubility in Fe Nanoclusters and Implications for the Growth of Single-Walled Carbon Nanotubes

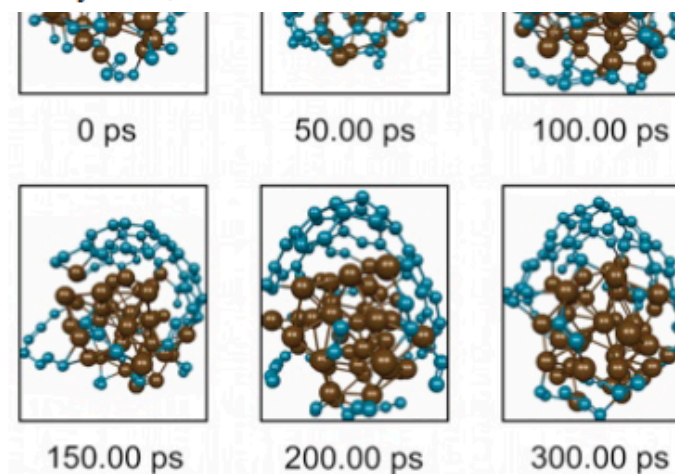
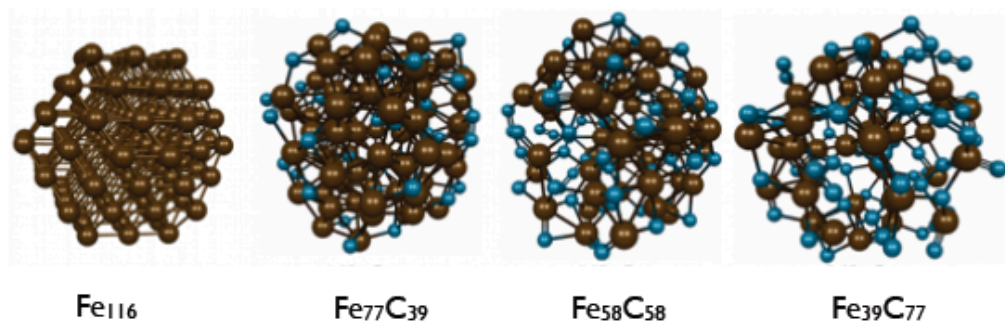
A. R. Harutyunyan,<sup>1,\*,\dagger</sup> N. Awasthi,<sup>2</sup> A. Jiang,<sup>2</sup> W. Setyawan,<sup>2</sup> E. Mora,<sup>1</sup> T. Tokune,<sup>1</sup> K. Bolton,<sup>3</sup> and S. Curtarolo<sup>2,\*,\ddagger</sup>

<sup>1</sup>*Honda Research Institute USA, Inc., 1381 Kinnear Road, Columbus, Ohio 43212, USA*

<sup>2</sup>*Department of Mechanical Engineering and Materials Science, Duke University, Durham, North Carolina 27708, USA*

<sup>3</sup>*University College of Borås, SE-501 90 Borås and Physics Department, Göteborg University, SE-412 96 Göteborg, Sweden*

(Received 26 October 2007; published 14 May 2008)

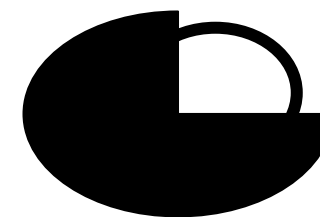
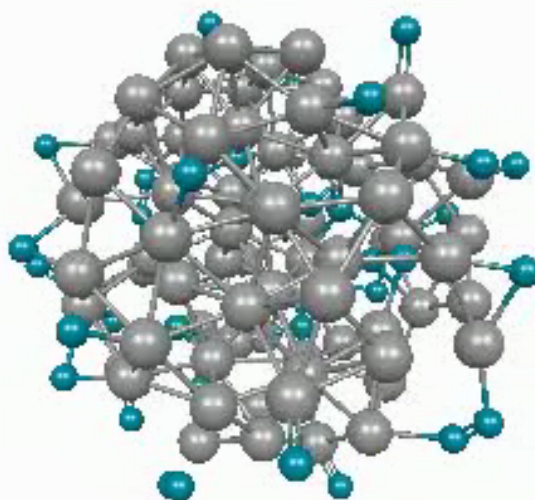


Fe<sub>39</sub>C<sub>77</sub>@1400K-9

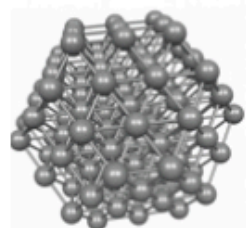
# Ni-Carbide Nanoparticle Precursor

A. J. Page, H. Yamane, Y. Ohta, SI, K. Morokuma, *J. Am. Chem. Soc.* **132**, 15699 (2010)

Metal-car  
Precipitatio  
S



Ni<sub>77</sub>C<sub>39</sub>@1400K-5

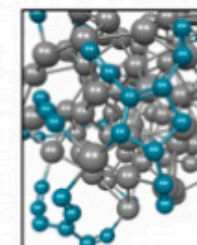
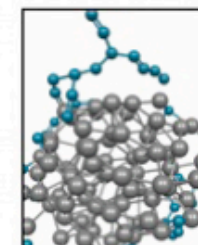


Ni<sub>116</sub>

Ni<sub>77</sub>C<sub>39</sub>

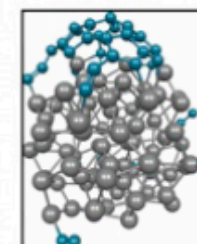
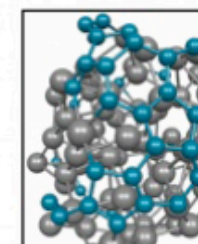
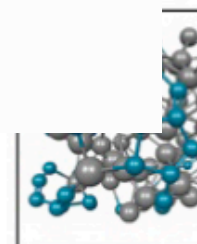
Ni<sub>58</sub>C<sub>58</sub>

Ni<sub>39</sub>C<sub>77</sub>



96.08 ps

116.84 ps



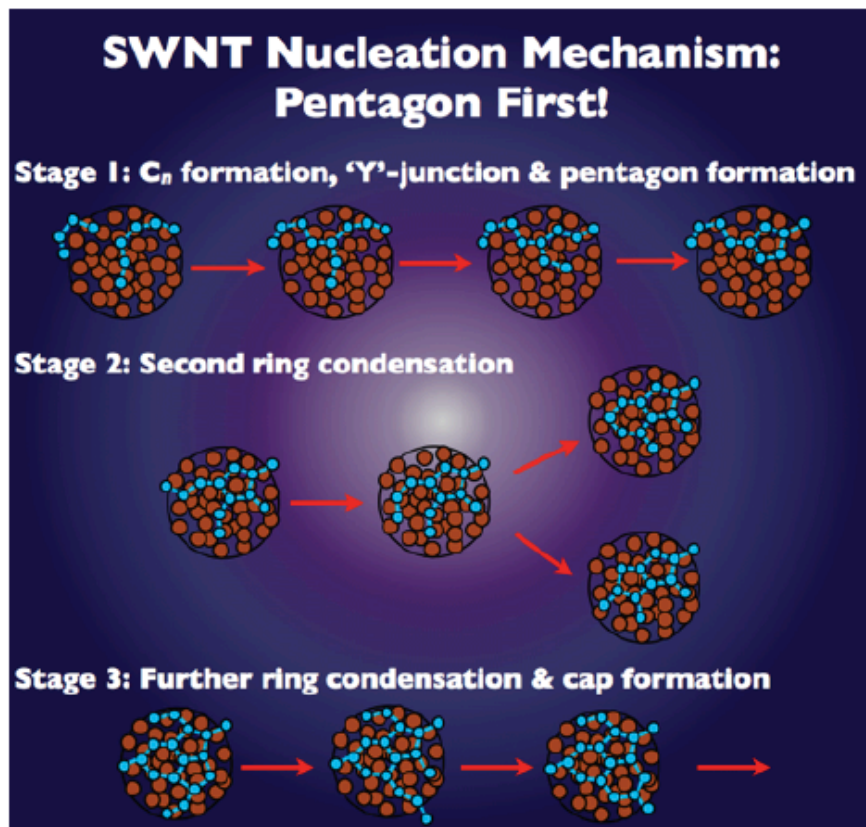
121.04 ps

139.08 ps

300.00 ps 46

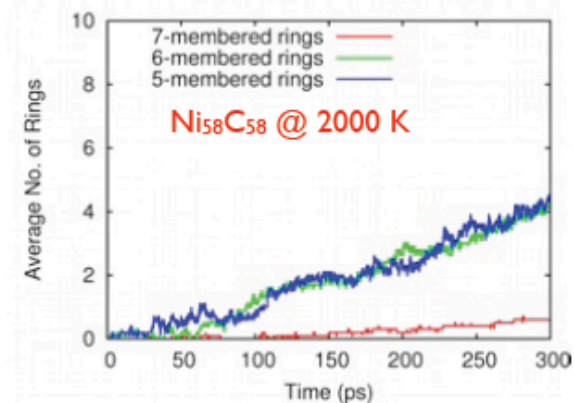
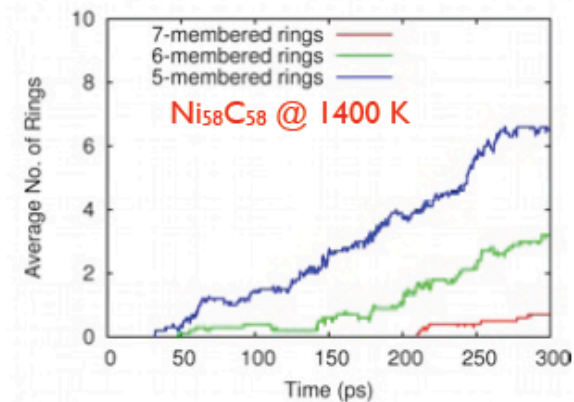
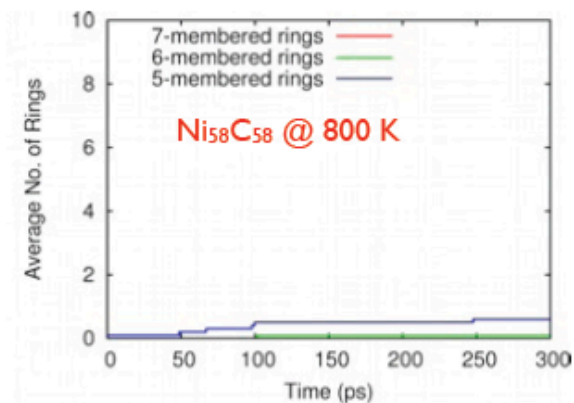
Ni<sub>77</sub>C<sub>39</sub>@1400K-5

A. J. Page, H. Yamane, Y. Ohta, SI, K. Morokuma, *J. Am. Chem. Soc.* **132**, 15699 (2010)



Carbide phase  $\rightarrow$  Catalyst/Cap structure in  $< 300$  ps!

Fe/Ni-carbide nanoparticles thermodynamically unstable at these conditions.



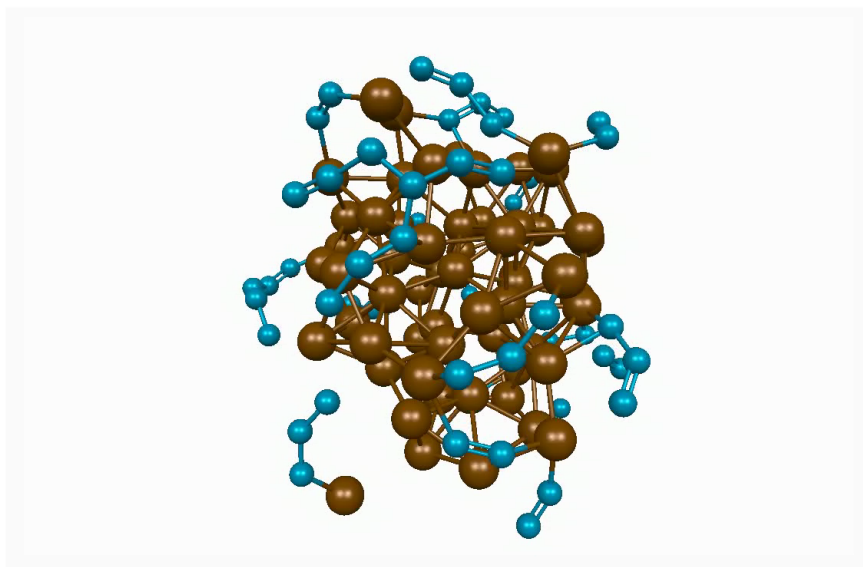
A. J. Page, H. Yamane, Y. Ohta, SI, K. Morokuma, *J. Am. Chem. Soc.* **132**, 15699 (2010)

Phase of Catalyst during Nucleation:

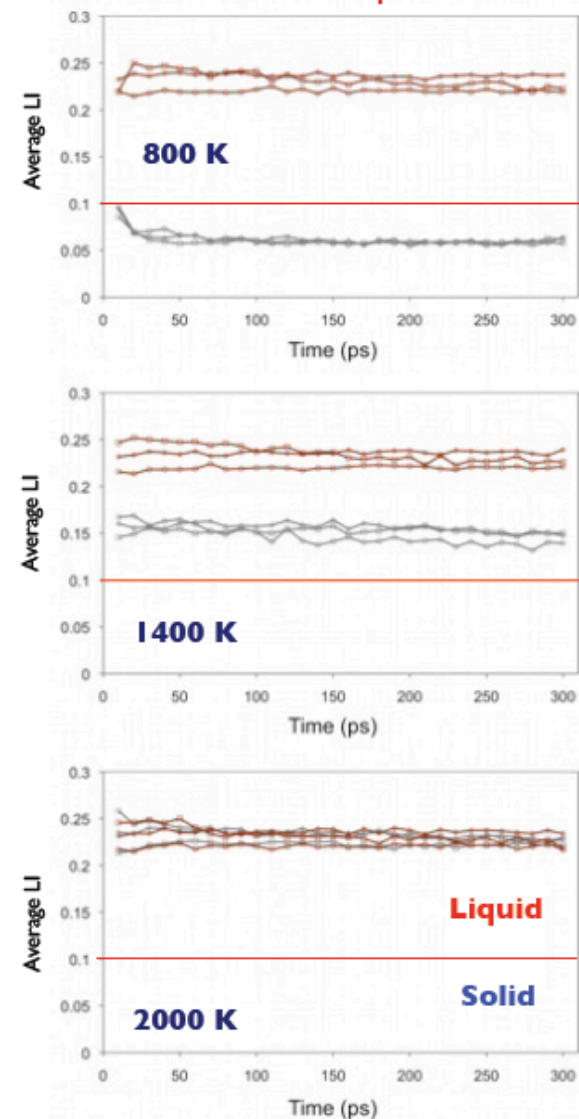
Fe: liquid > 800 K;

Ni: solid at 800 K, liquid at 1400 K.

- SWNT nucleation dynamics:
  - Driven by 'catalyst-carbon' interaction strength.
  - Catalyst-carbon interactions: Ni-C=1.06 eV; Fe-C=1.78 eV.
  - Fe-carbide: SWNT nucleation impeded (destruction of C-C bonds).
- Carbon precipitation dynamics:
  - Determined by catalyst-carbon interaction & phase of catalyst.



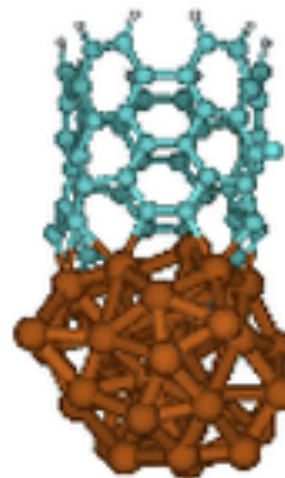
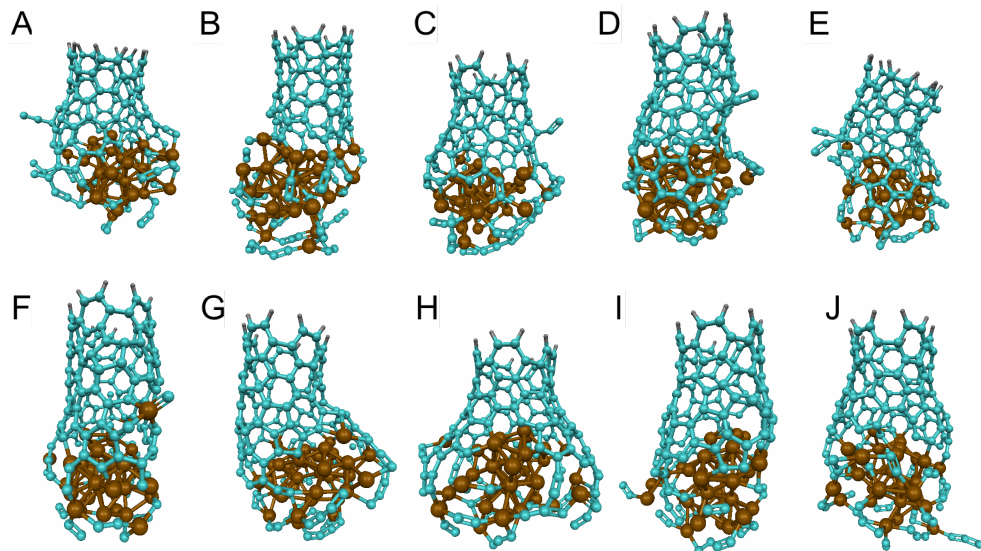
Repeated formation and destruction of first pentagon  
(Fe<sub>58</sub>C<sub>58</sub> @ 2000 K)



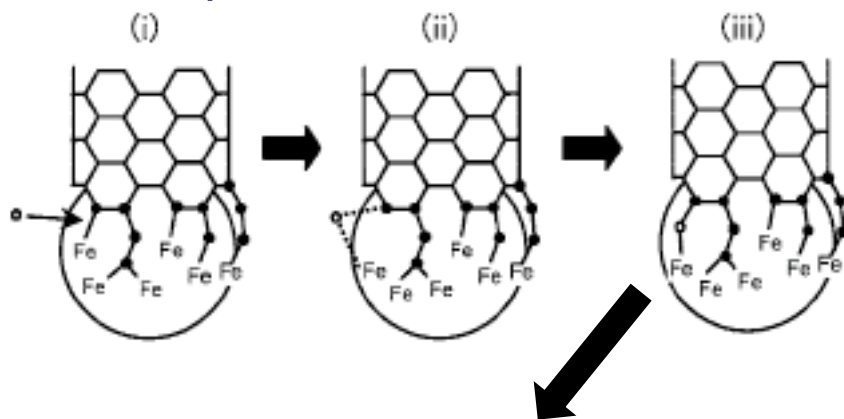


Y. Ohta, Y. Okamoto, SI, K. Morokuma,  
*ACS Nano* 2, 1437 (2008)

10 Trajectories after 45 ps C supply

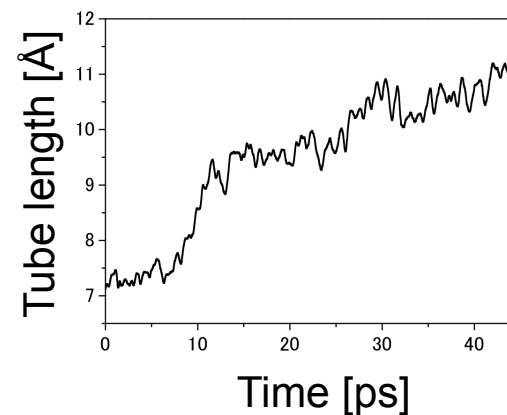


Schematic depiction of C atom insertion events



new 5-, 6-, 7-membered rings

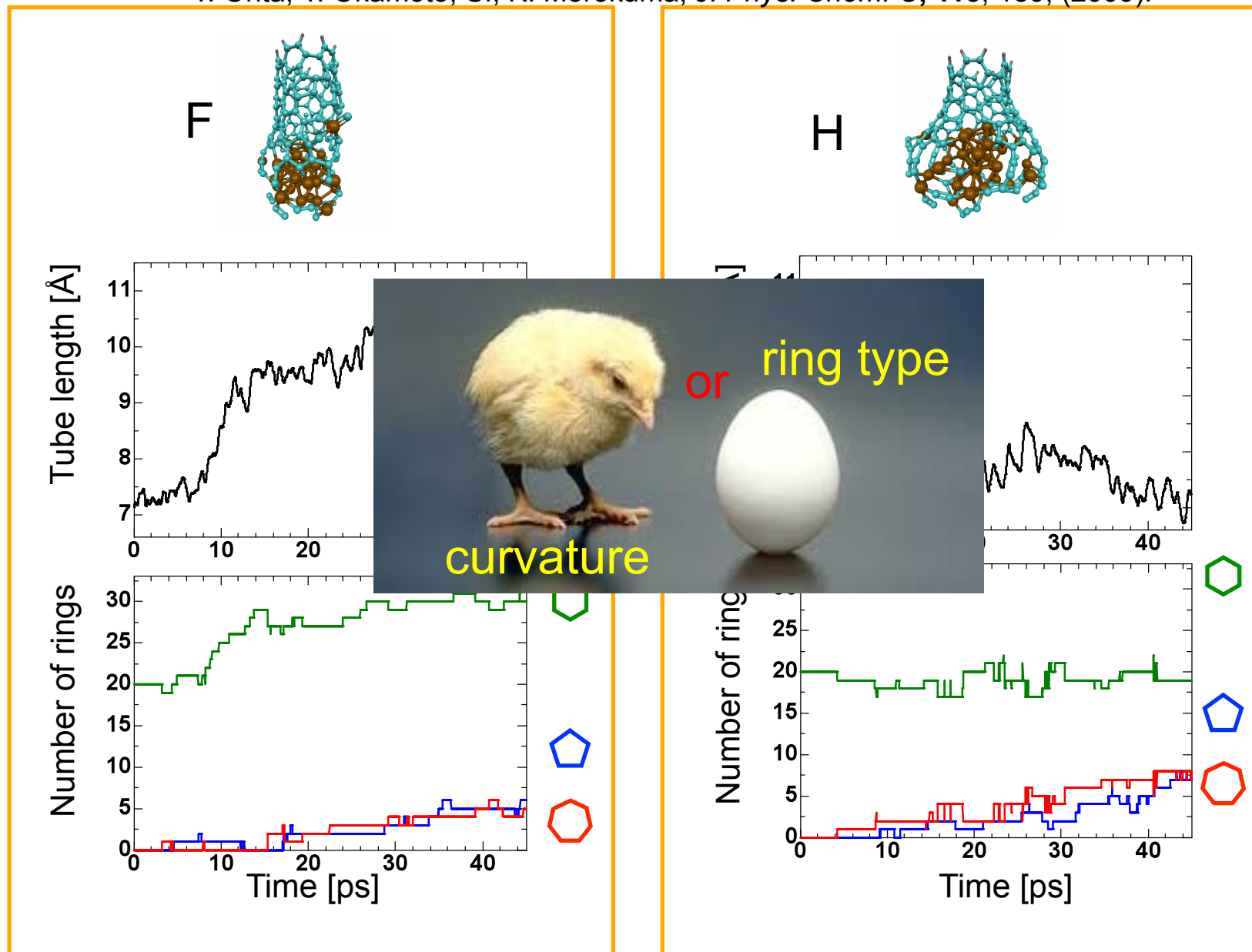
Trajectory F



Growth rate: **~10 pm/ps**

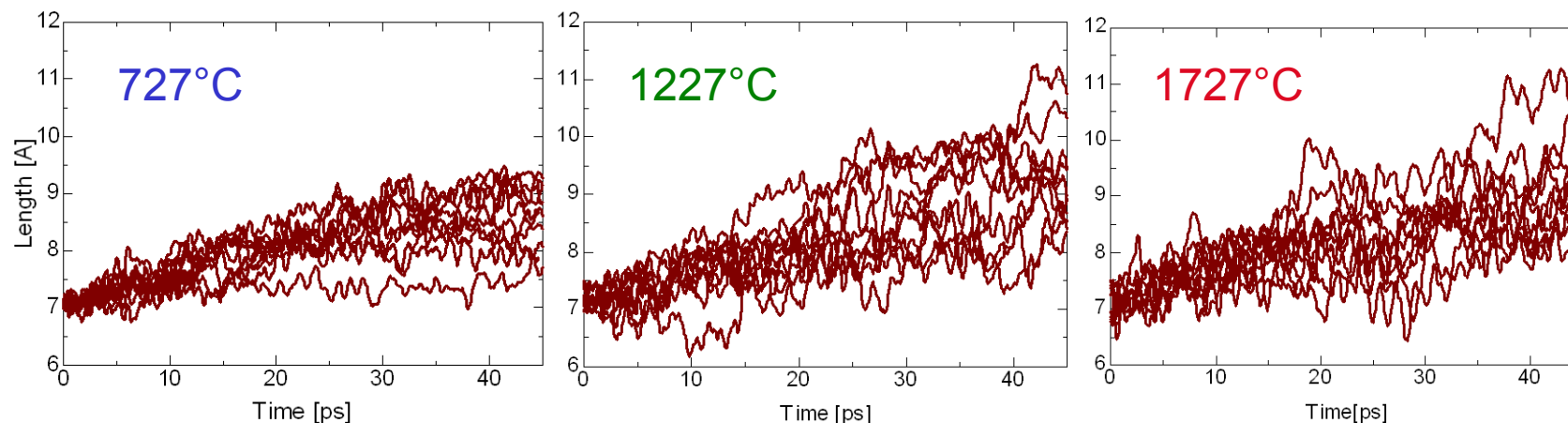
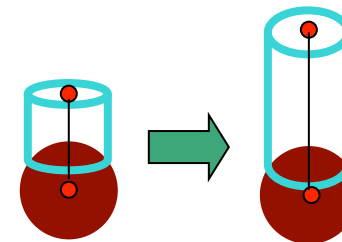
# Correlation between ring type and tube length

Y. Ohta, Y. Okamoto, SI, K. Morokuma, *J. Phys. Chem. C*, **113**, 159, (2009).



## Continued SWNT growth as function of temperature ( (5,5) armchair SWNT)

10 Trajectories for 3 temperatures



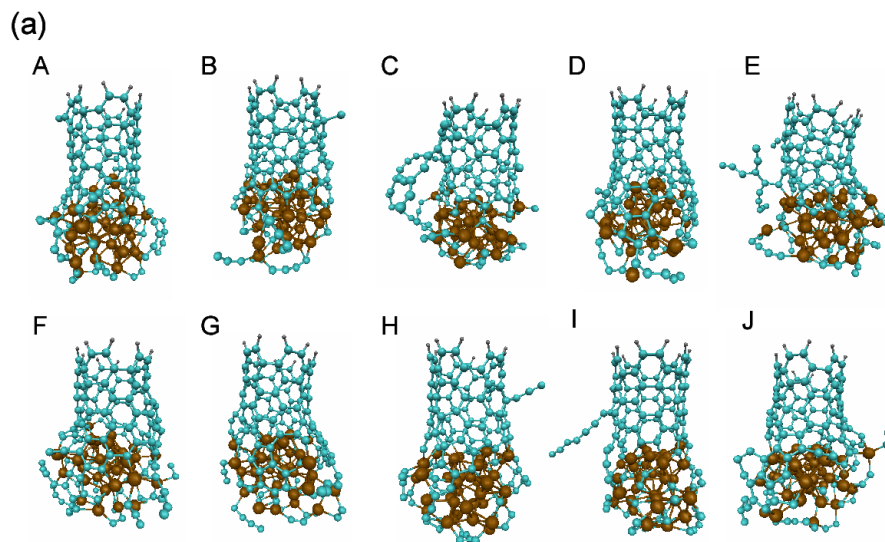
T[°C]	727	1227	1727
Growth rate [pm/ps] <sup>a</sup>	3.48	5.07	4.13
Chain carbons <sup>a</sup>	3.9	0.3	0.2
SWNT C atoms <sup>a</sup>	112.9	110.1	102.7

<sup>a</sup>averaged over 10 trajectories/T

Y. Ohta, Y. Okamoto, SI, K. Morokuma, *J. Phys. Chem. C*, **113**, 159, (2009).

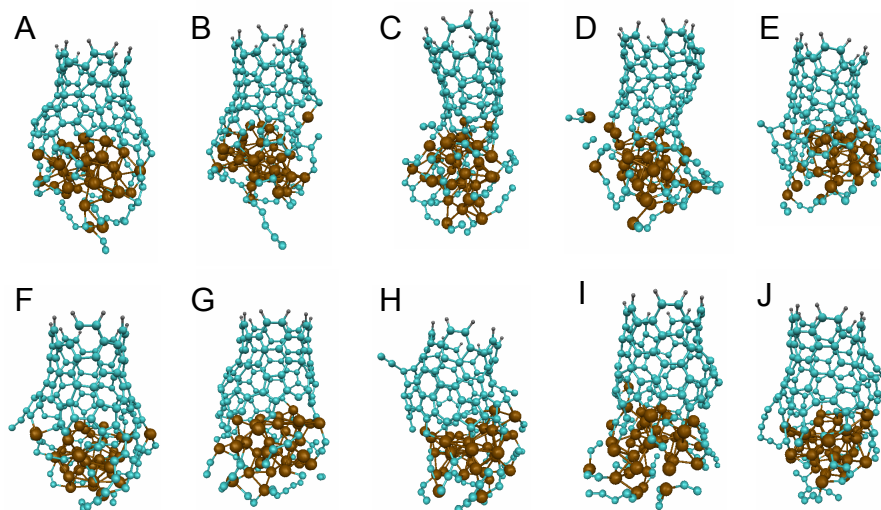
T=727°C

10 Trajectories after 45 ps

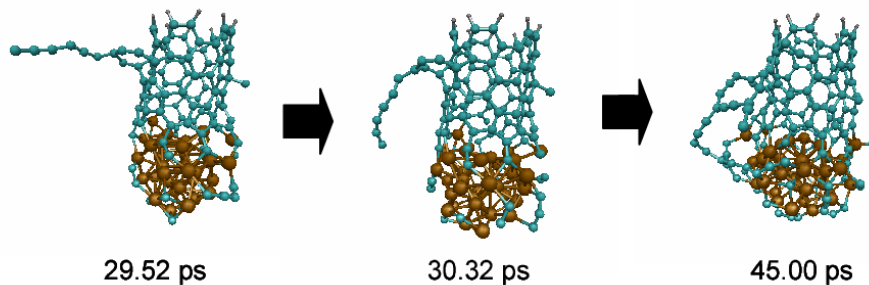


T=1727°C

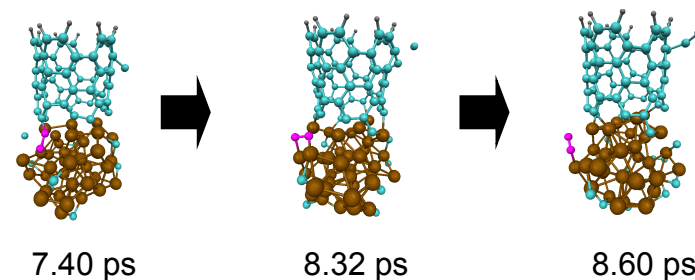
(a) 10 Trajectories after 45 ps



(b) Encapsulation of Fe by polyyne



Trajectory C

(b) Dissociation of C<sub>2</sub> from Fe/C

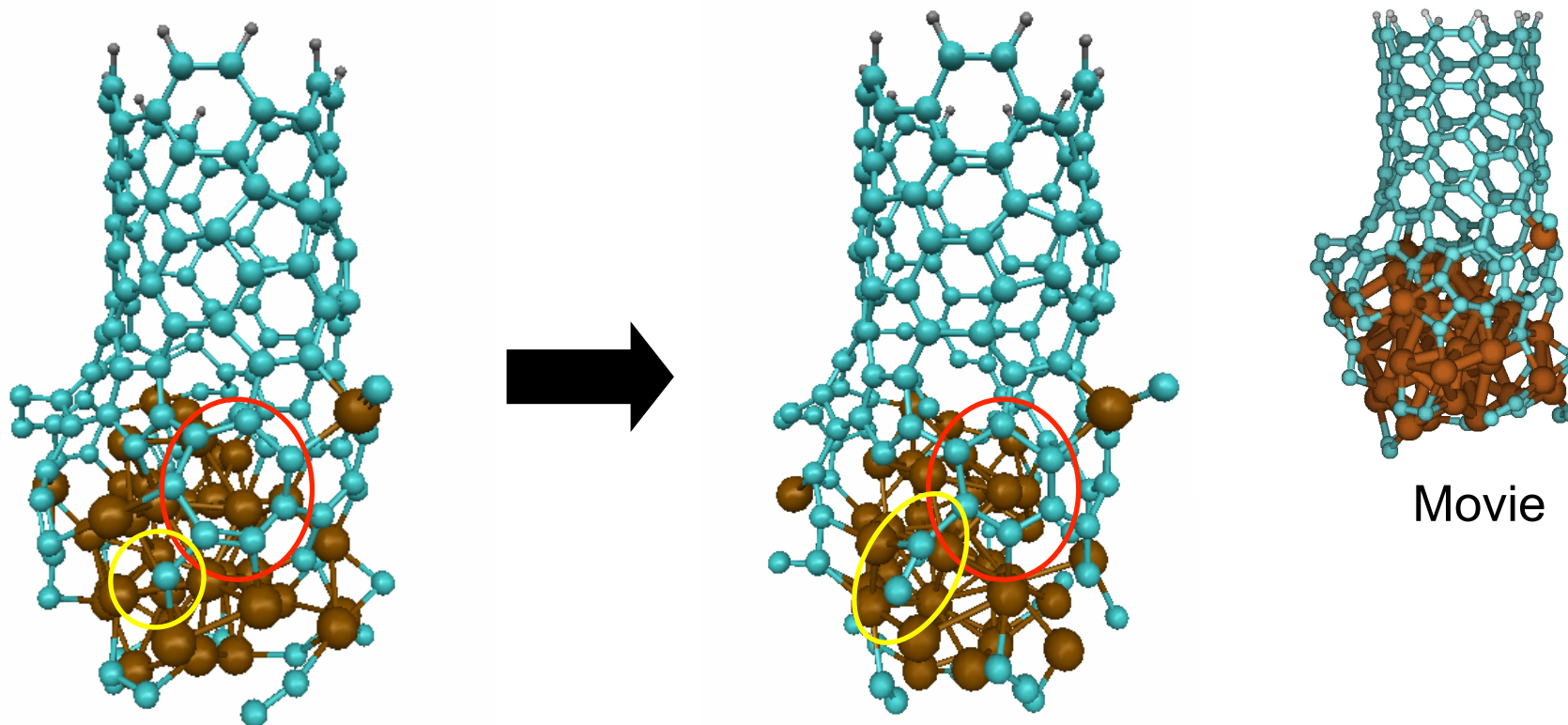
Trajectory G

Y. Ohta, Y. Okamoto, SI, K. Morokuma,  
*J. Phys. Chem. C*, **113**, 159, (2009).

# Self-healing process of sidewall (annealing)

**Fe-Carbon mobility at interface important!**

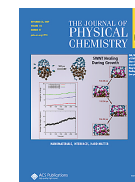
Trajectory 6:  $T_n = 1500$  K,  $T_e = 10$  k K,  $C_{int} = 1500$  K



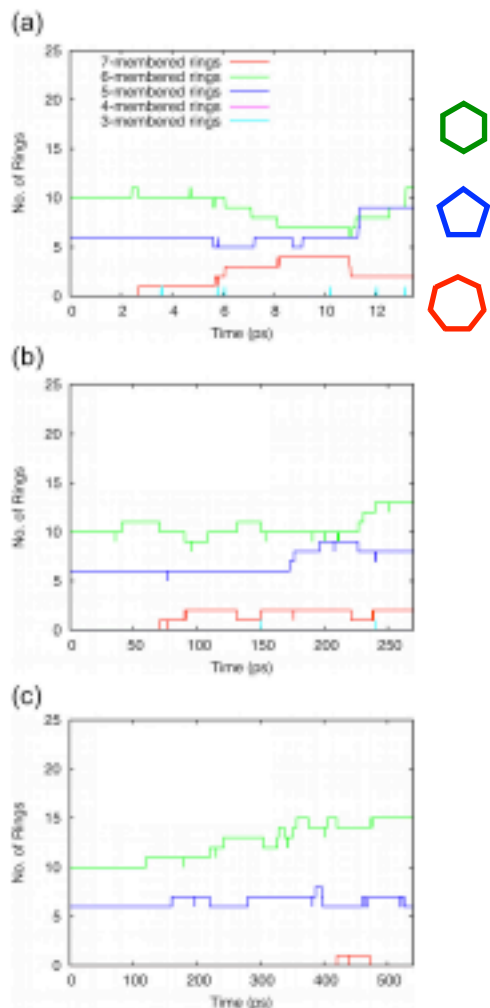
24.5 ps - 27.5 ps

**Heptagon** + **C** changes into **hexagon** + **C<sub>2</sub>**

A. Page, Y. Ohta, Y. Okamoto, SI,  
K. Morokuma, *J. Phys. Chem. C*,  
**113**, 20198, (2009)



# Carbon Feeding Rate Effect: $M_{38}C_{40}+nC$

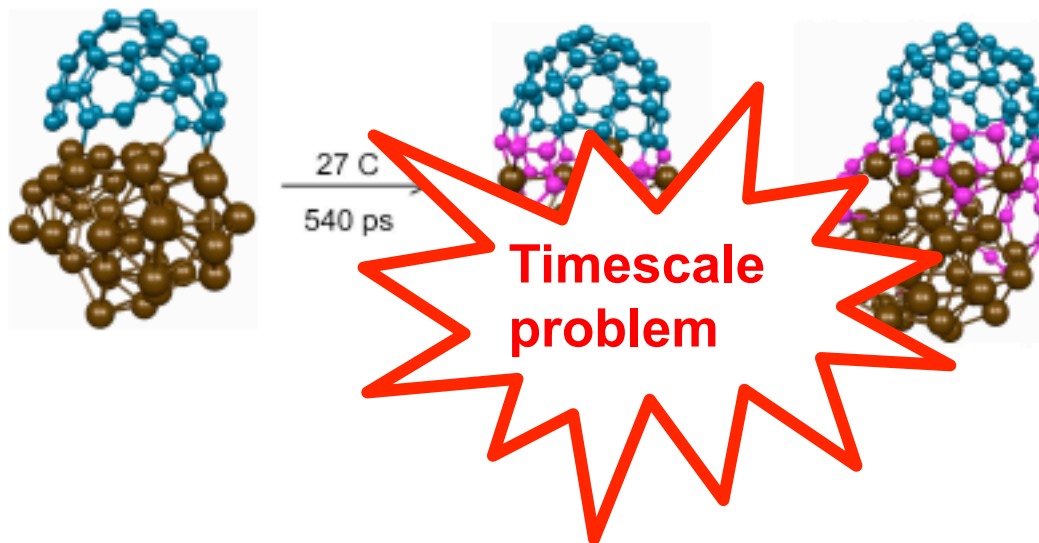


(a) fast (1 C / 0.5 ps)  
 (b) slow (1 C / 10 ps)  
 (c) very slow (1 C / 20 ps)

Comparison of "fast", "slow" & "very slow" SWNT growth:

Near-perfect extension of (5,5)  $sp^2$  network obtained with 1 C / 10 ps supply rate.

Even better using 1 C / 20 ps!!



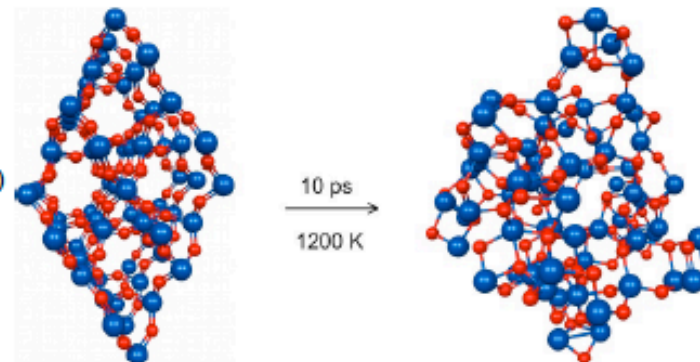
## Simulation of CH<sub>4</sub> CVD and SWNT Nucleation on SiO<sub>2</sub>-Nanoparticles

A. J. Page, KRS Chandrakumar, SI, K. Morokuma,  
*J. Am. Chem. Soc.* **133**, 621 (2011).

### Computational Details

#### Catalyst:

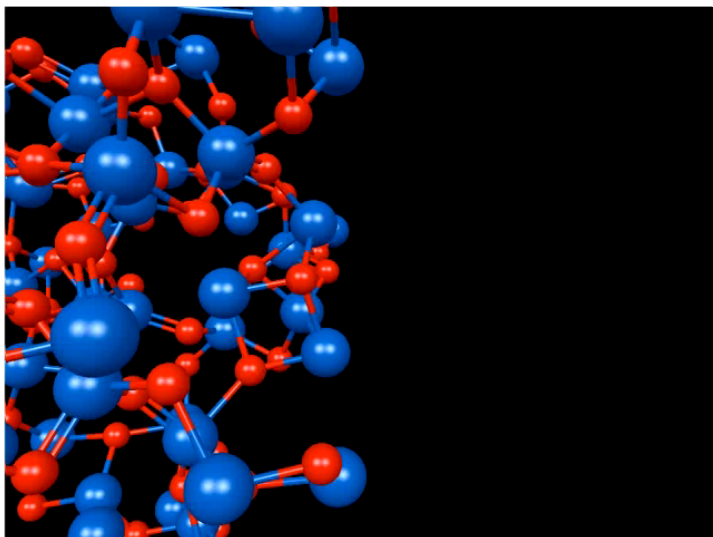
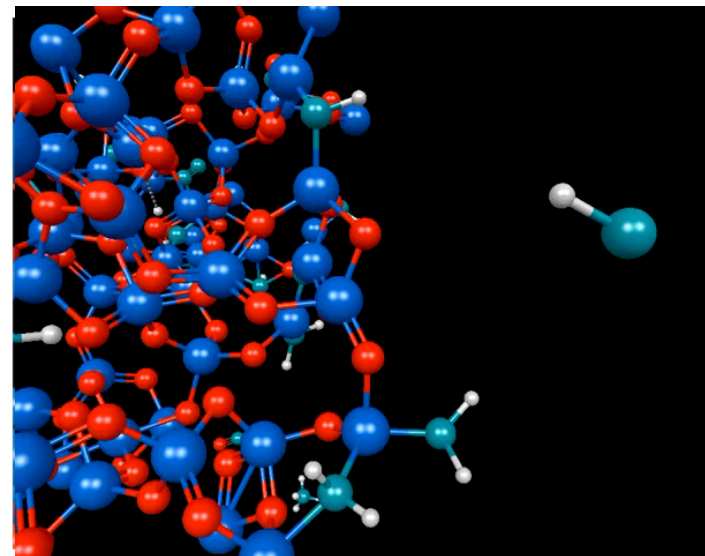
- Si-terminated Si<sub>63</sub>O<sub>88</sub> nanoparticle.
- Truncated β-SiO<sub>2</sub> structure @ 1078 K. (Kihara *Eur. J. Miner.*, 2 (1990) 63.)
- Dimensions: 1.8 × 1.5 × 1.1 nm<sup>3</sup>.



#### CVD Simulation:

- SCC-DFTB/MD:  $T_n = 1,200$  K;  $T_e = 1,500$  K;  $\Delta t = 1$  fs; Velocity-Verlet integration; Nosé-Hoover Chain thermostat (Ohta-san's Paderborn code); slko.5425 Slater-Koster files.
- 60×60×60 Å<sup>3</sup> box.
- × 10 replication.
- Assumption: CH<sub>4</sub> decomposes pyrolytically before adsorption on SiO<sub>2</sub>. (Cheng *et al.*, *ACS Nano*, 3, 3421, (2009)).
- CH<sub>x</sub> ( $x = 0 - 3$ ) shooting (chosen with weighted Poisson distribution) @ rate of 2/1.0ps.
- Random H removal @ rate of 4/1.0 ps, after first 10 ps of simulation.
- 'Target concentration' of carbon on SiO<sub>2</sub> nanoparticle = 60.
- Anneal at constant temperature once target CH<sub>x</sub> concentration reached (up to 250 ps).

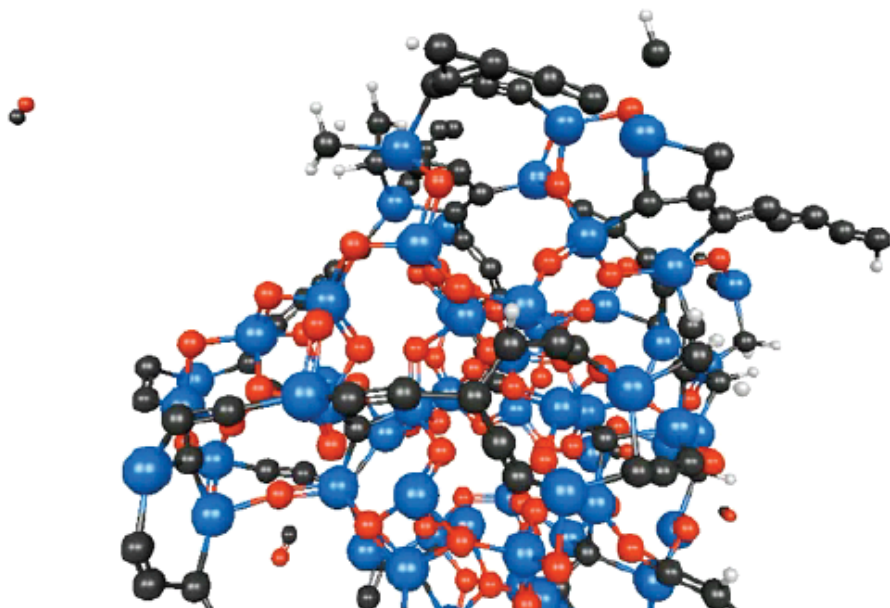
(1) Run 0.5 ps MD. (2) analyse structure. (3) Remove H. (4) Shoot CH<sub>x</sub> if # C on SiO<sub>2</sub>-np < 60, else goto (1).

CH<sub>4</sub> CVD on SiO<sub>2</sub> Nanoparticles**H-Abstraction by SiO<sub>2</sub> catalyst****H-Abstraction by surface carbon****H Abstraction/CO Formation Mechanism**

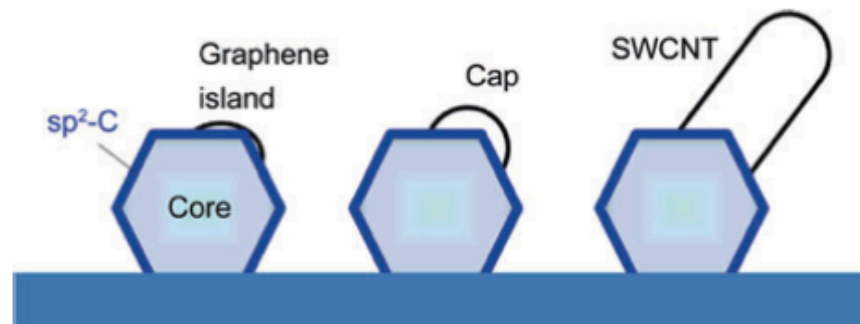
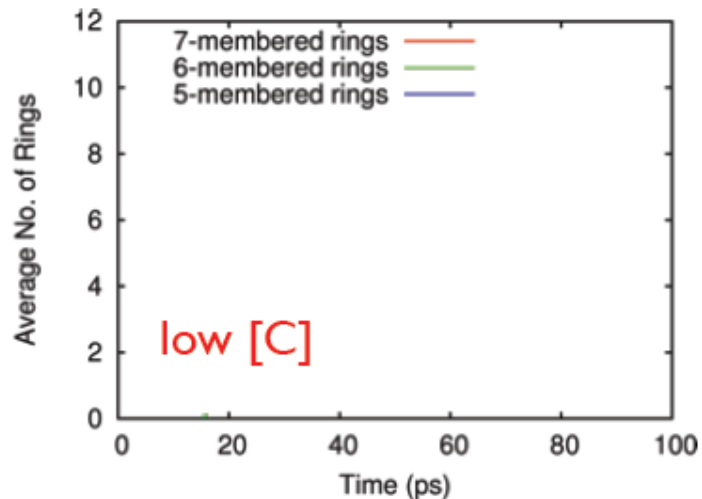
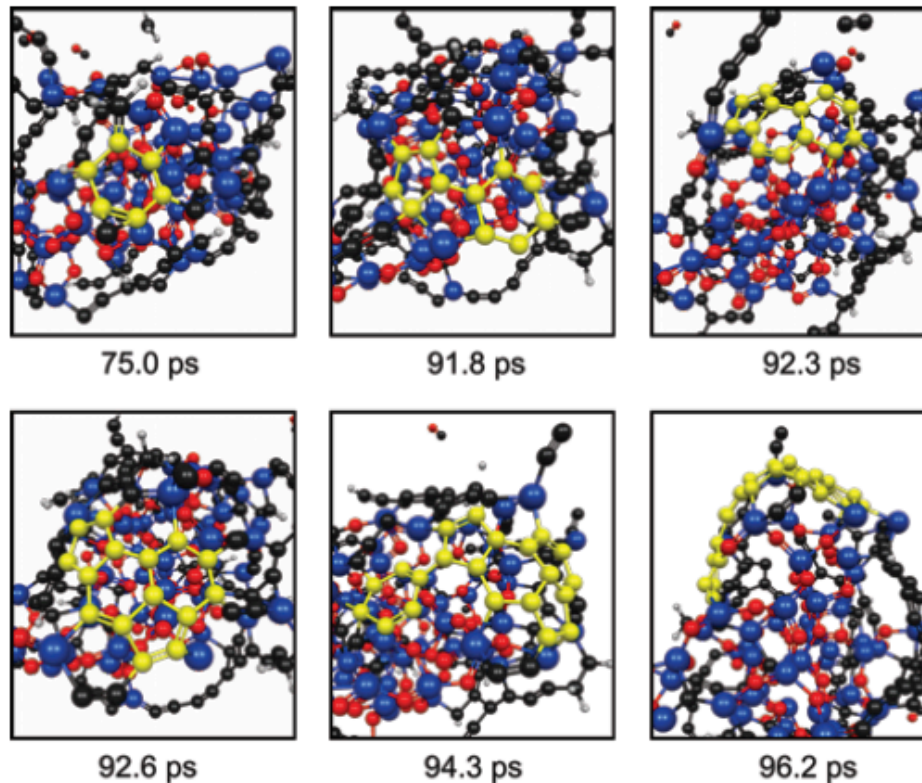
- CO production *always* follows H abstraction from CO carbon.
- H-abstraction mediated by SiO<sub>2</sub> and surface carbon.
- Natural H-removal mechanism observed!
  - H-abstraction from carbon necessary for SWNT nucleation.
  - Mechanism still unknown for transition-metal catalysts...



# SWNT Nucleation on SiO<sub>2</sub> Nanoparticles



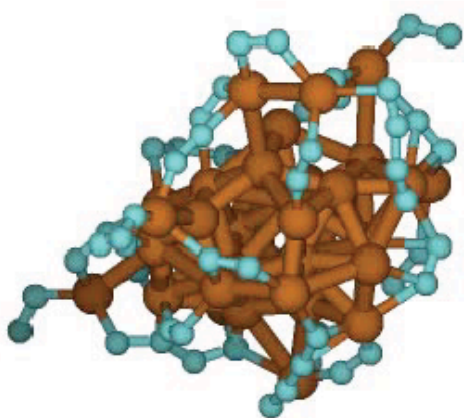
SWNT nucleation:  
Requires carbon-saturated SiO<sub>2</sub> surface!



Homma et al., Nano. Res. (2009)

## Traditional vs. Non-Traditional Catalysts

## Fe/Ni-Catalyzed SWNT Nucleation (VLS)

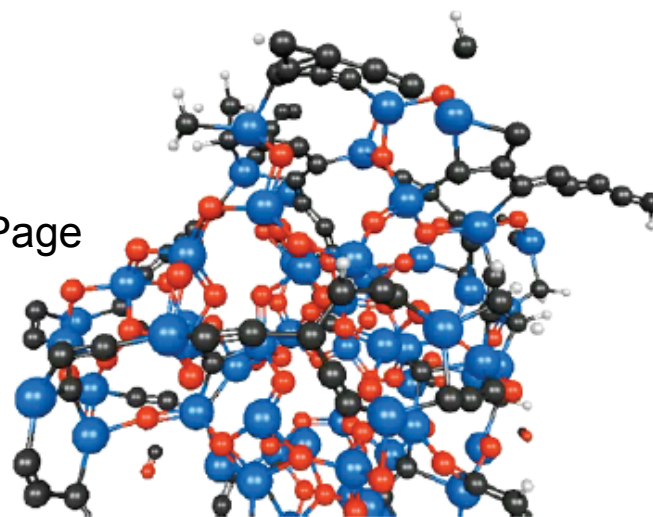


Ohta et al., *ACS Nano*, (2009);  
Page et al. *J. Phys. Chem. C* (2010)



Poster:  
Alister J. Page

1. **Bulk carbide**, catalyst can be **liquid**.
2. C<sub>n</sub> chains coalesce on catalyst surface.
3. C<sub>n</sub> chains exhibit **high** mobility.
4. **Pentagon always** formed first.
5. Further ring condensation **independent of [C]**.
6. Cap-structure formed within **50-400 ps**.

SiO<sub>2</sub>-Catalyzed SWNT Nucleation (VSS)

A. J. Page, KRS Chandrakumar, SI, K. Morokuma,  
*J. Am. Chem. Soc.* **133**, 621 (2011).

1. **Surface carbide**, catalyst is **solid**.
2. C<sub>n</sub> chains coalesce on the catalyst surface.
3. C<sub>n</sub> chains exhibit **low** mobility.
4. **Pentagon or hexagon** formed first.
5. Further ring condensation **requires high [C]**.
6. Cap-structure formed over **ns timescales**.

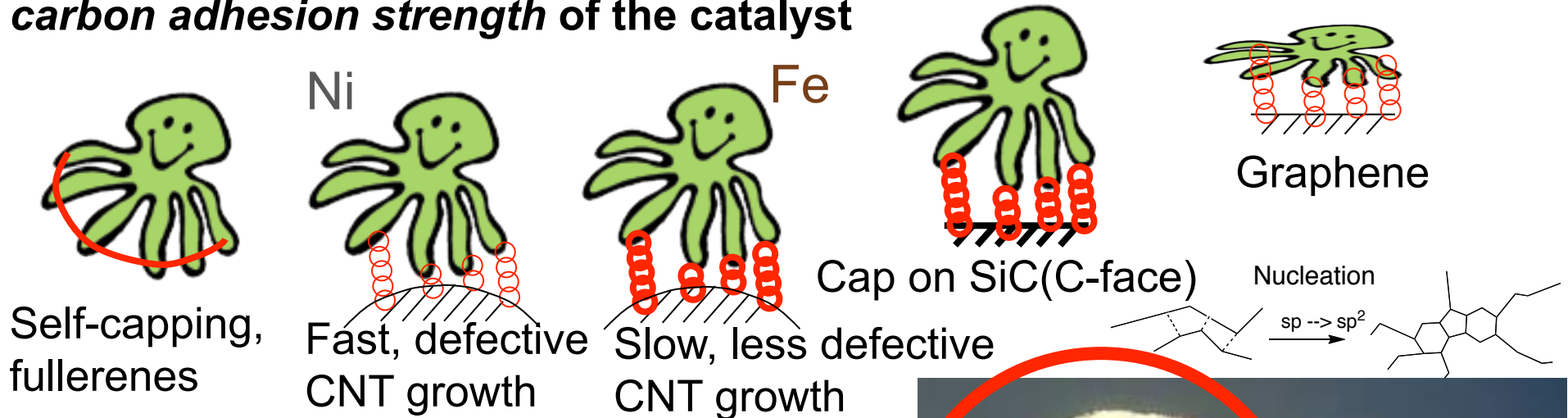
# Overview

- Overview: What are MD simulations up against?
- Density-functional tight-binding (DFTB)-based MD
- DFTB/MD Simulations: Acetylene feedstock, carbon-only feedstock, catalytic CVD, catalyst-free CVD
- **Key points: What did we learn?**
- Comparison with thermodynamics and selected experiments
- What is next?

# Key points learned

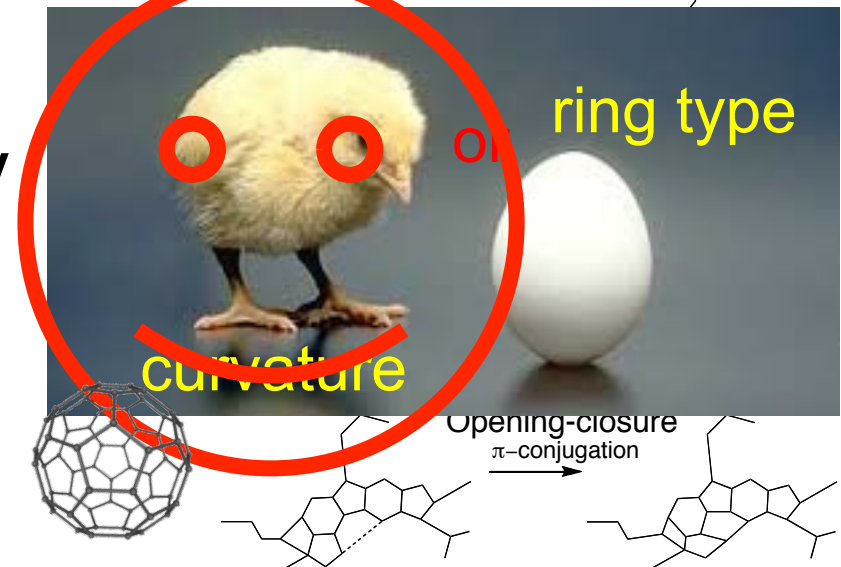
# Chicken or egg? Solved.

- Nanocarbons grow as  $C \rightarrow C(sp) \rightarrow C(sp^2)$ , via **pentagon-first** mechanism
- What (fullerene, tube, graphene) we grow depends on the *shape* and *carbon adhesion strength* of the catalyst



- Carbon nanostructures grow dynamically in **simultaneous** processes of chaotic **growth** and defect **healing**

- **Pentagons in nanocarbons are “fossils” from pentagon-first mechanism, “frozen” by shape of carbon superstructure on surface**



# Overview

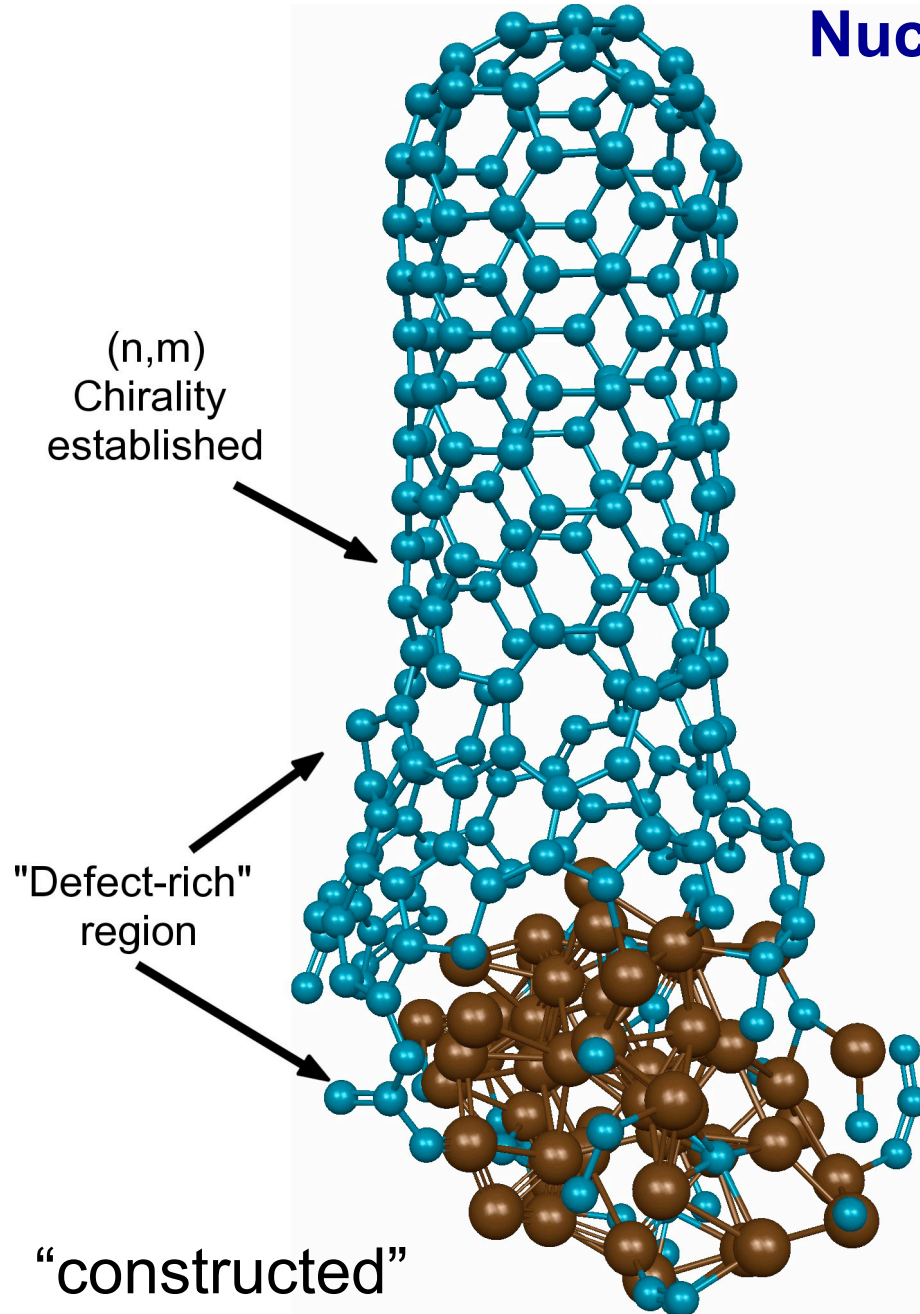
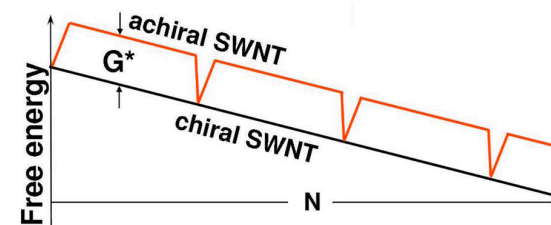
- Overview: What are MD simulations up against?
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- DFTB/MD Simulations: Acetylene feedstock, carbon-only feedstock, catalytic CVD, catalyst-free CVD
- Key points: What did we learn?
- **Comparison with thermodynamics and selected experiments**
- What is next?

### Nucleation and growth hypothesis:

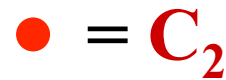
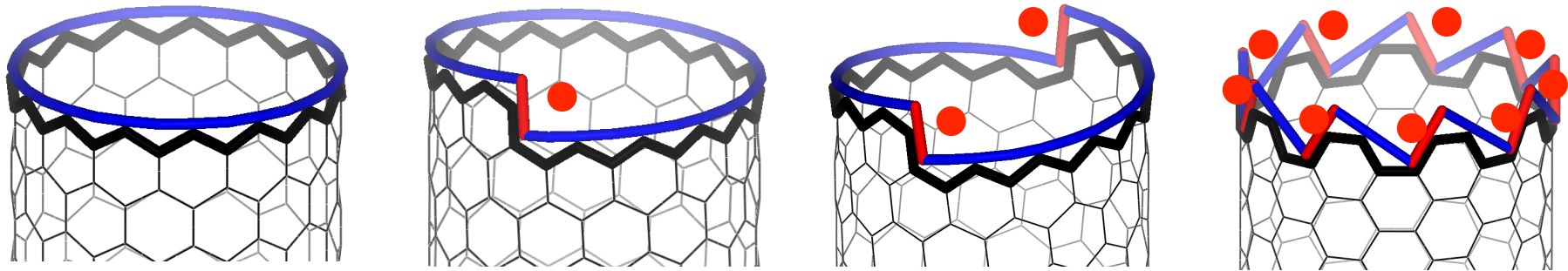
In sharp contrast to:



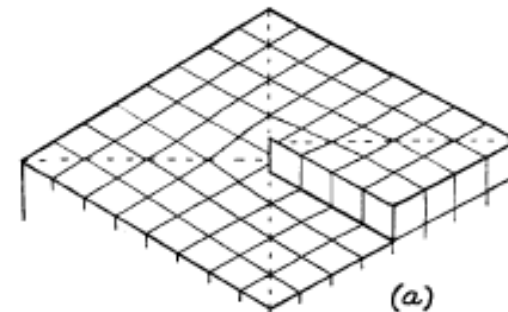
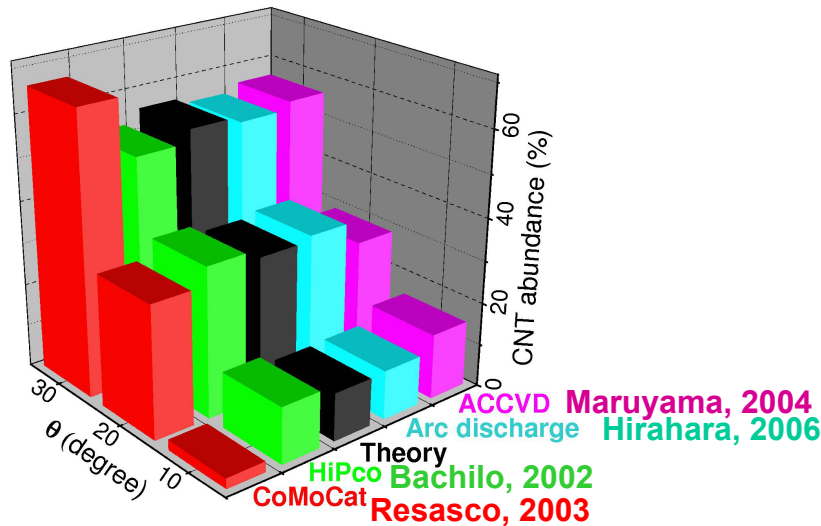
F. Ding, A. Harutyunyan, B. I. Yakobson,  
*Proc. Natl. Acad. Sci.* **106**, 2506 (2009)



# Ding & Jacobsons Nucleation and Growth Hypothesis:



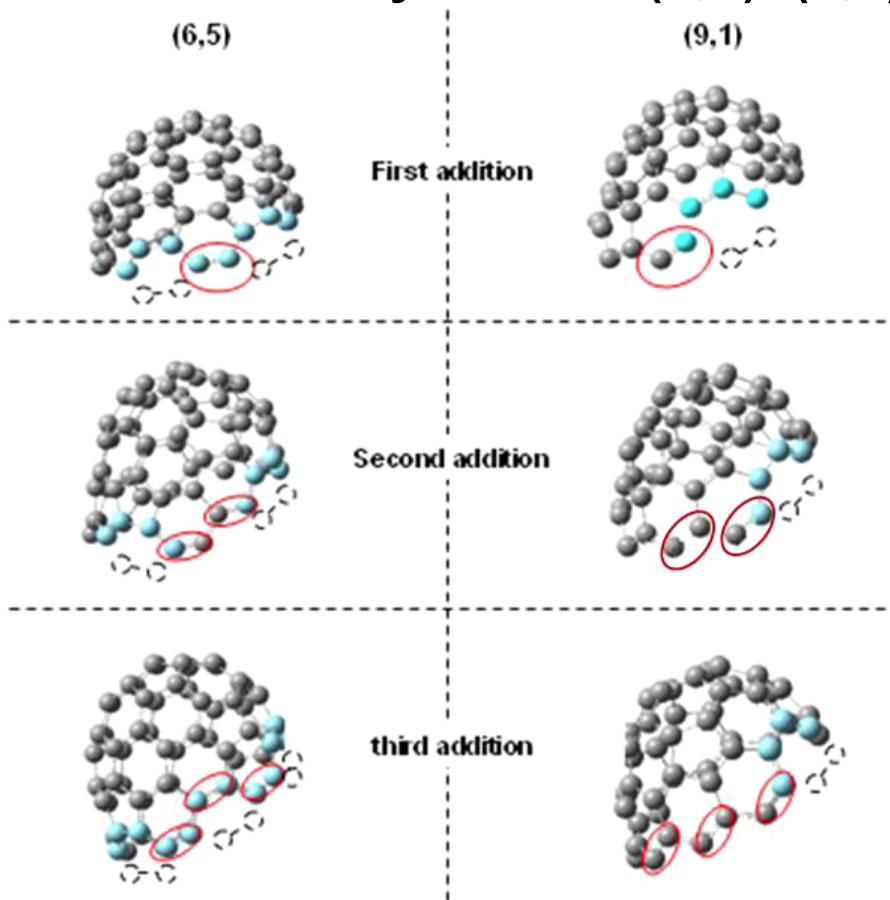
For (n,m) tube, **m** kinks serve as active sites for C<sub>2</sub> accretion,  
 Growth rate  $K \sim m/d \sim \sin(\theta) \sim \theta$ ,  $0 < \theta < 30^\circ$



Frank 1949  
 "cozy corners" J Watson 1950

## Earlier Theoretical Studies Predicting $(n,n) > (n,0)$

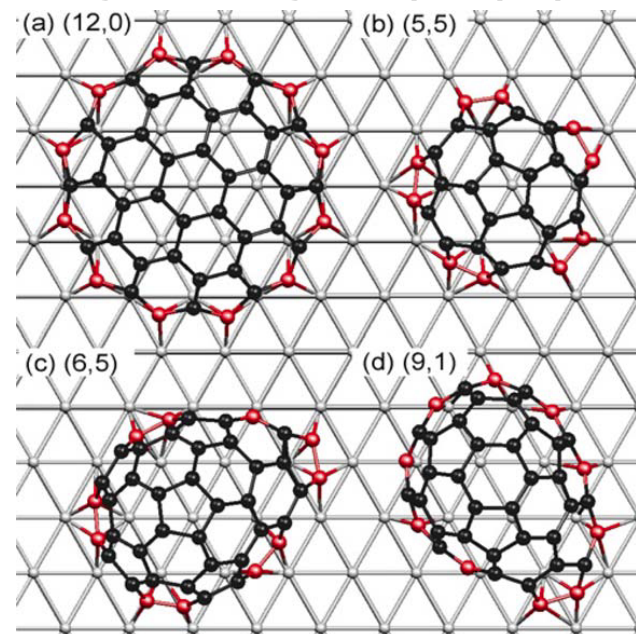
Number of cozy corners  $(n,n) > (n,0)$



Red circled: previously added  $C_2$   
 Blue spheres: favorable  $C_2$  addition sites  
 Dashed spheres: possible new  $C_2$ s

D. A. Gomez-Gualdron, P. B. Balbuena, Nanotechnology **19**, 485604 (2008)

Edge energies  $(n,0) > (n,n)$



	$E_{cap}$	$E_{CM}$	(excess energies/C [eV])
(12,0)	0.33	0.01	( <i>lower is more stable</i> )
(5,5)	0.42	0.00	
(6,5)	0.33	0.10	
(9,1)	0.35	0.22	

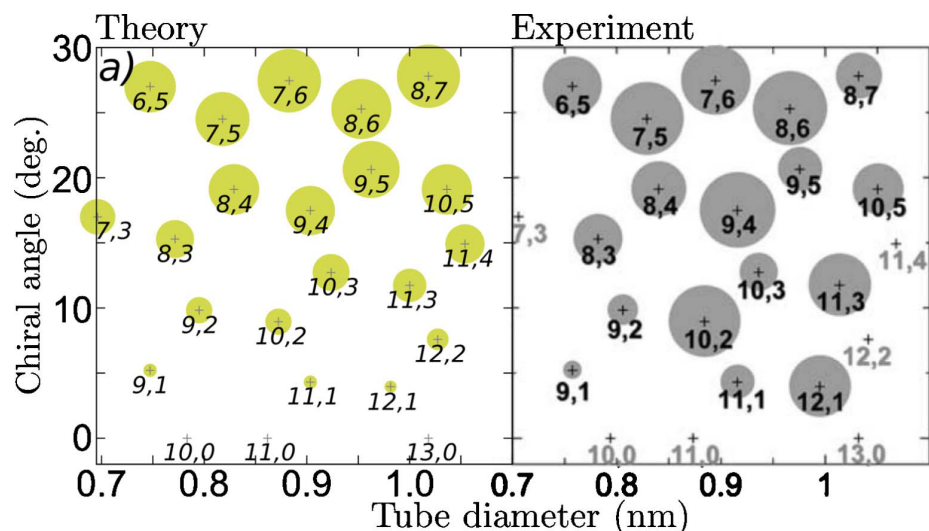
Both (9,1) and (6,5) caps are matching the Ni(111) lattice, but (6,5) has greater thermodynamic stability!

S. Reich, L. Li, J. Robertson, Chem. Phys. Lett. **421**, 469 (2006)

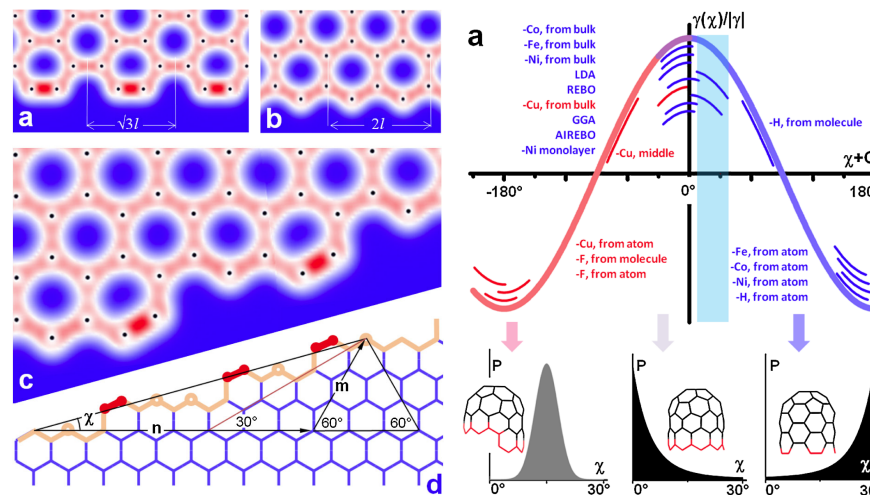


## Later Theoretical Studies Predicting $(n,n) > (n,0)$

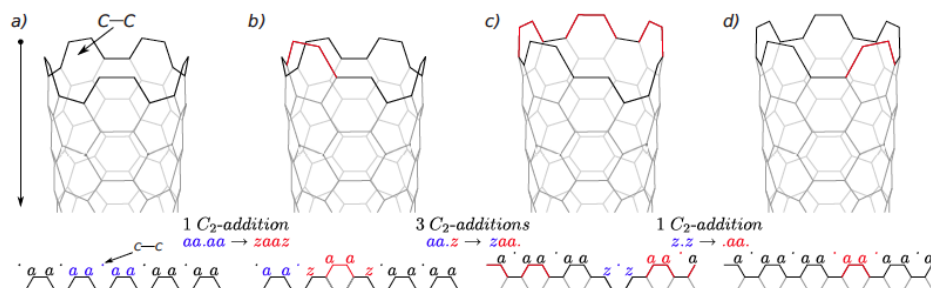
Number of cozy corners  $(n,n) > (n,0)$   
 Barriers of  $C_2$  addition  $(n,n) < (n,0)$



Edge energies  $(n,0) > (n,n)$



Y. Liu, A. Dobrinsky, B. I. Yakobson, Phys. Rev. Lett. **105**, 235502 (2010)

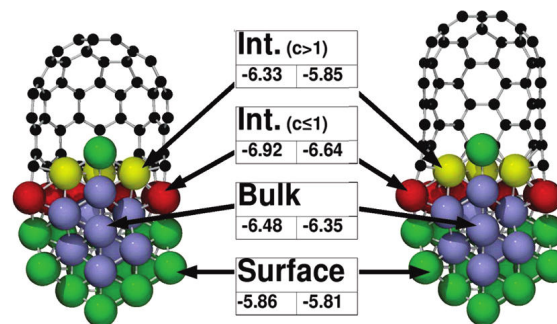


Near-armchair tubes have many addition sites, each addition in cozy corner, zero barrier addition

H. Dumlich, S. Reich, Phys. Rev. B **82**, 085421 (2010)

## Edge adhesion $(n,0) > (n,n)$

$(10,0)@Ni_{55}$        $(5,5)@Ni_{55}$



A. Borjesson, K. Bolton, ACS Nano **5**, 771 (2012)

## “Confirmation” of Ding/Yakobson Model by Experiment

nature  
materials

LETTERS

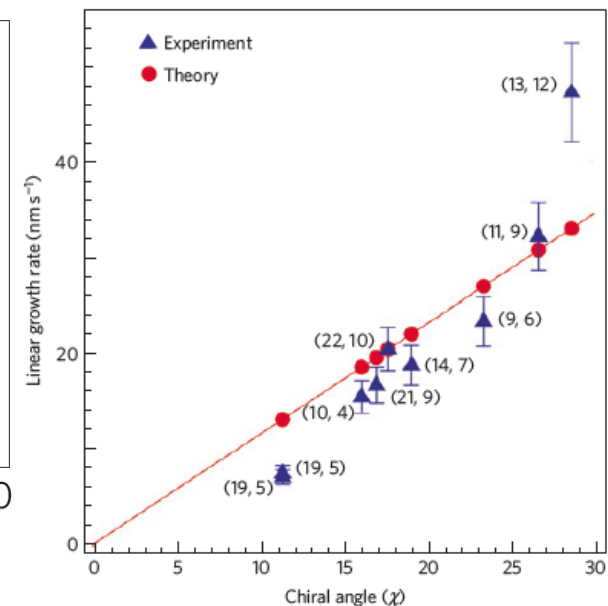
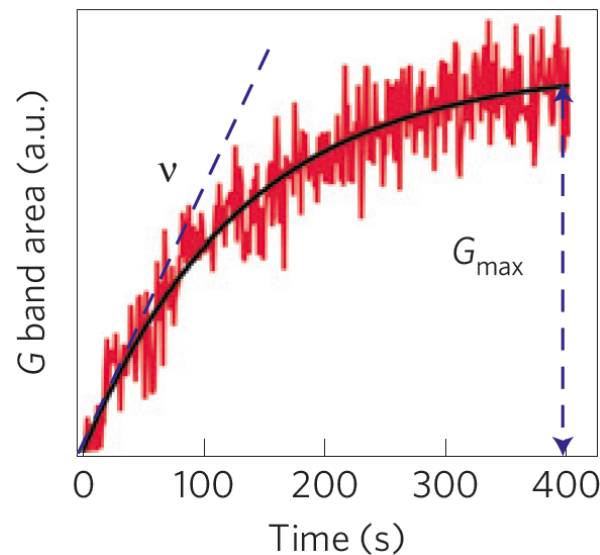
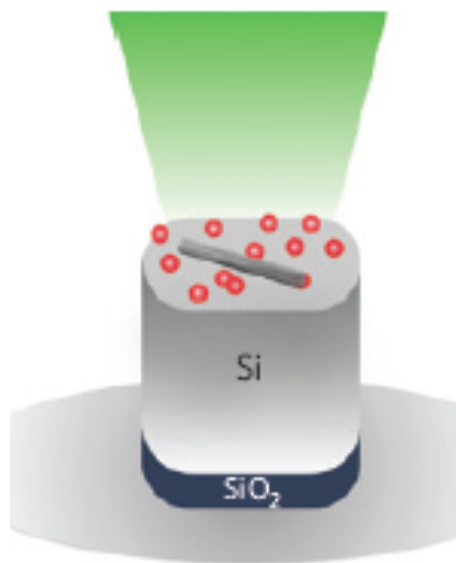
PUBLISHED ONLINE: 29 JANUARY 2012 | DOI: 10.1038/NMAT3231

Nat. Mater. **11**, 231 (2012)

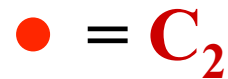
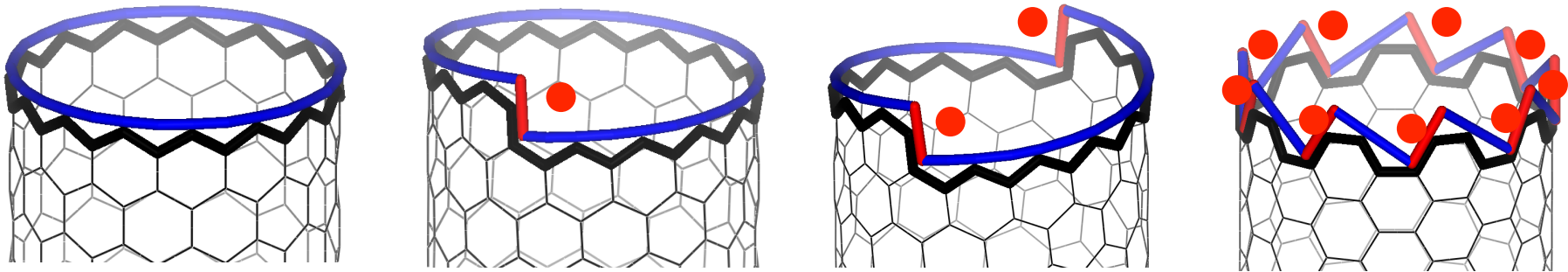
### *In situ* evidence for chirality-dependent growth rates of individual carbon nanotubes

Rahul Rao<sup>1\*†</sup>, David Liptak<sup>1,2</sup>, Tonya Cherukuri<sup>1</sup>, Boris I. Yakobson<sup>3</sup> and Benji Maruyama<sup>1\*</sup>

Measuring *growth rates*  $v$  of individual SWCNTs by Raman



## Ding & Yacobsons Nucleation and Growth Hypothesis:



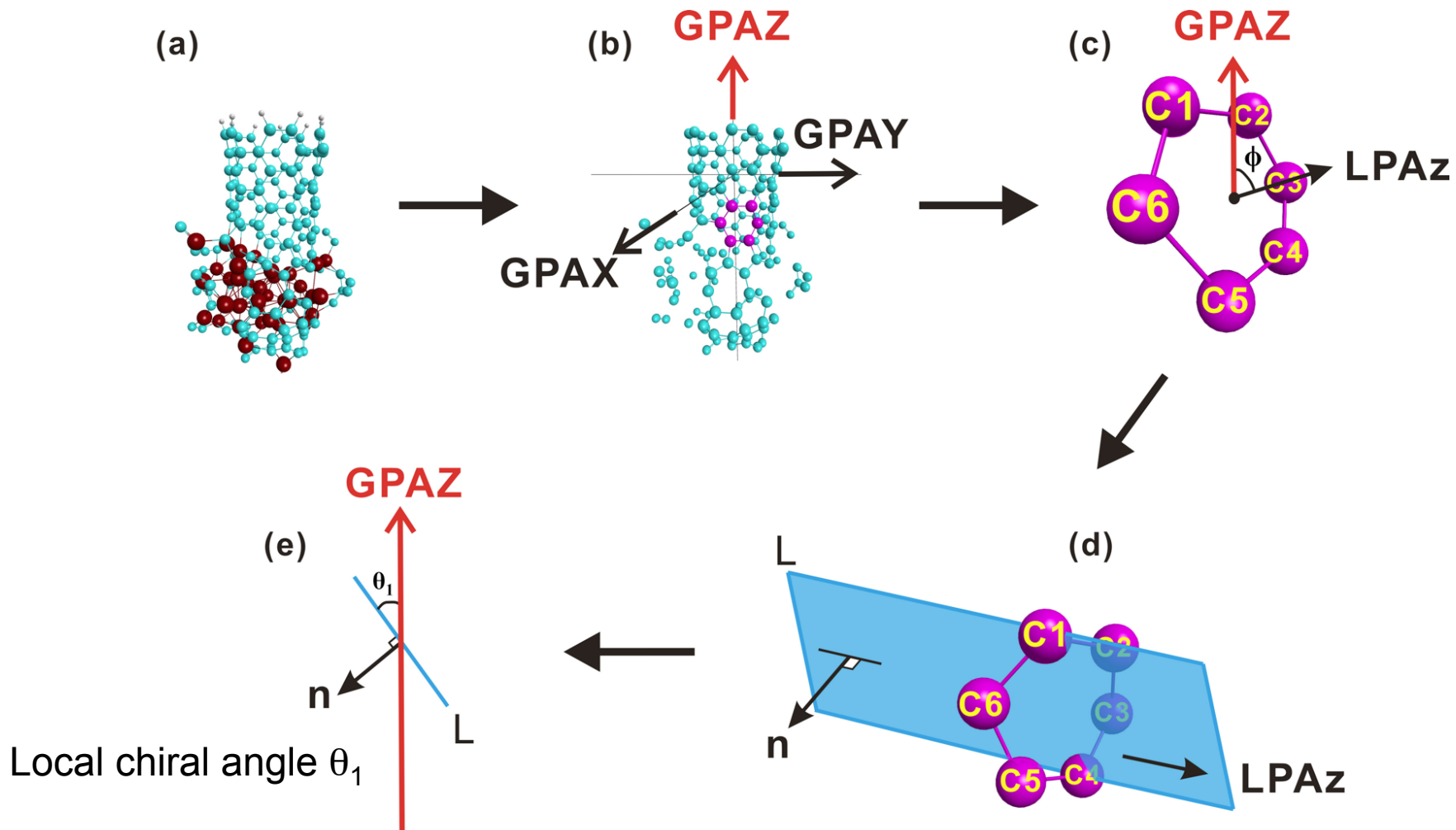
Is there anything in MD simulations, that relates to both Ding/ Yakobson's "Theory" as well as experiments?

Requirement: Need to define tube chiral angle during growth, even in the presence of defects!

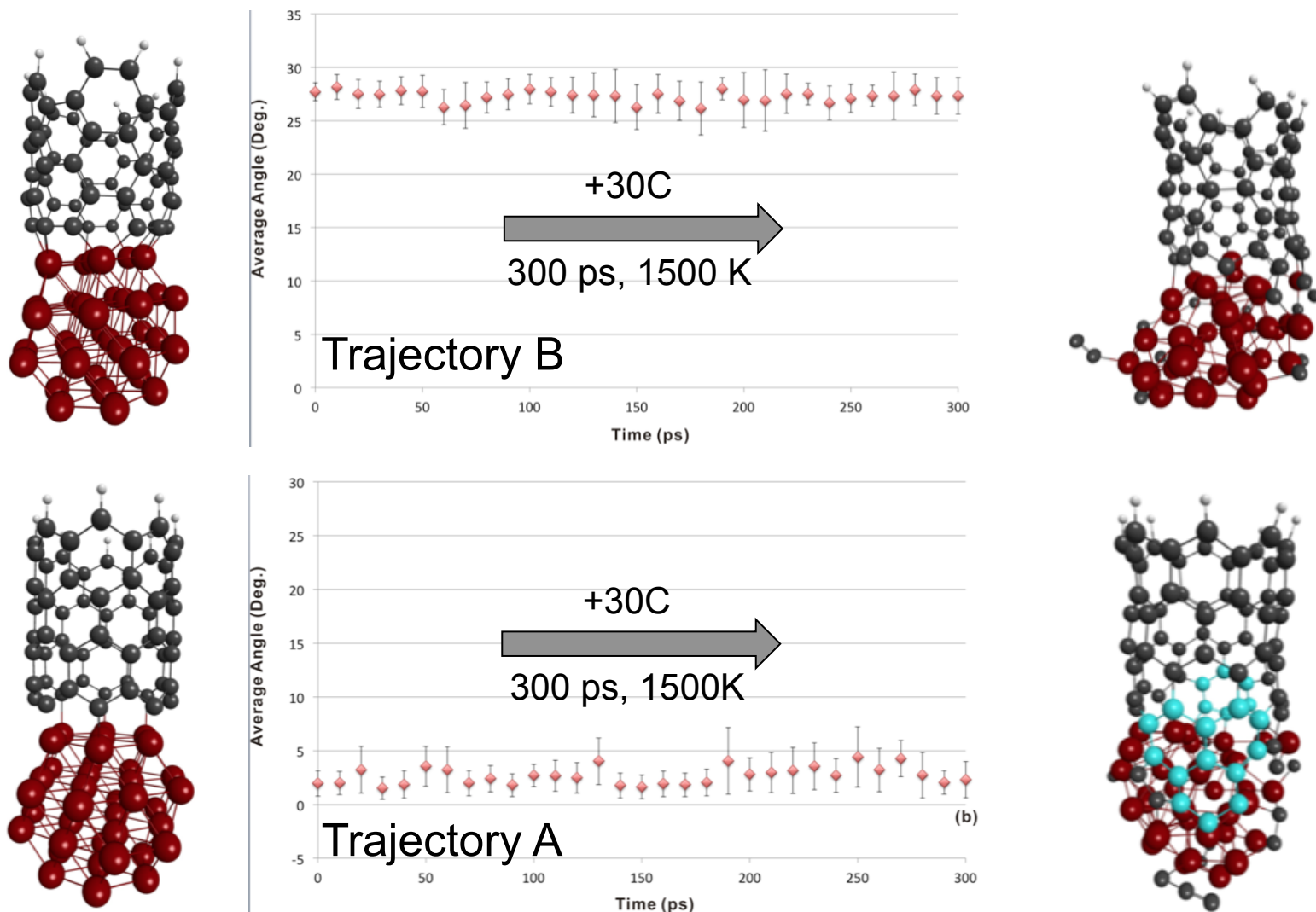
Solution: Define chiral angle for each hexagon separately.

## Local Chirality Index (LOCI): Definition

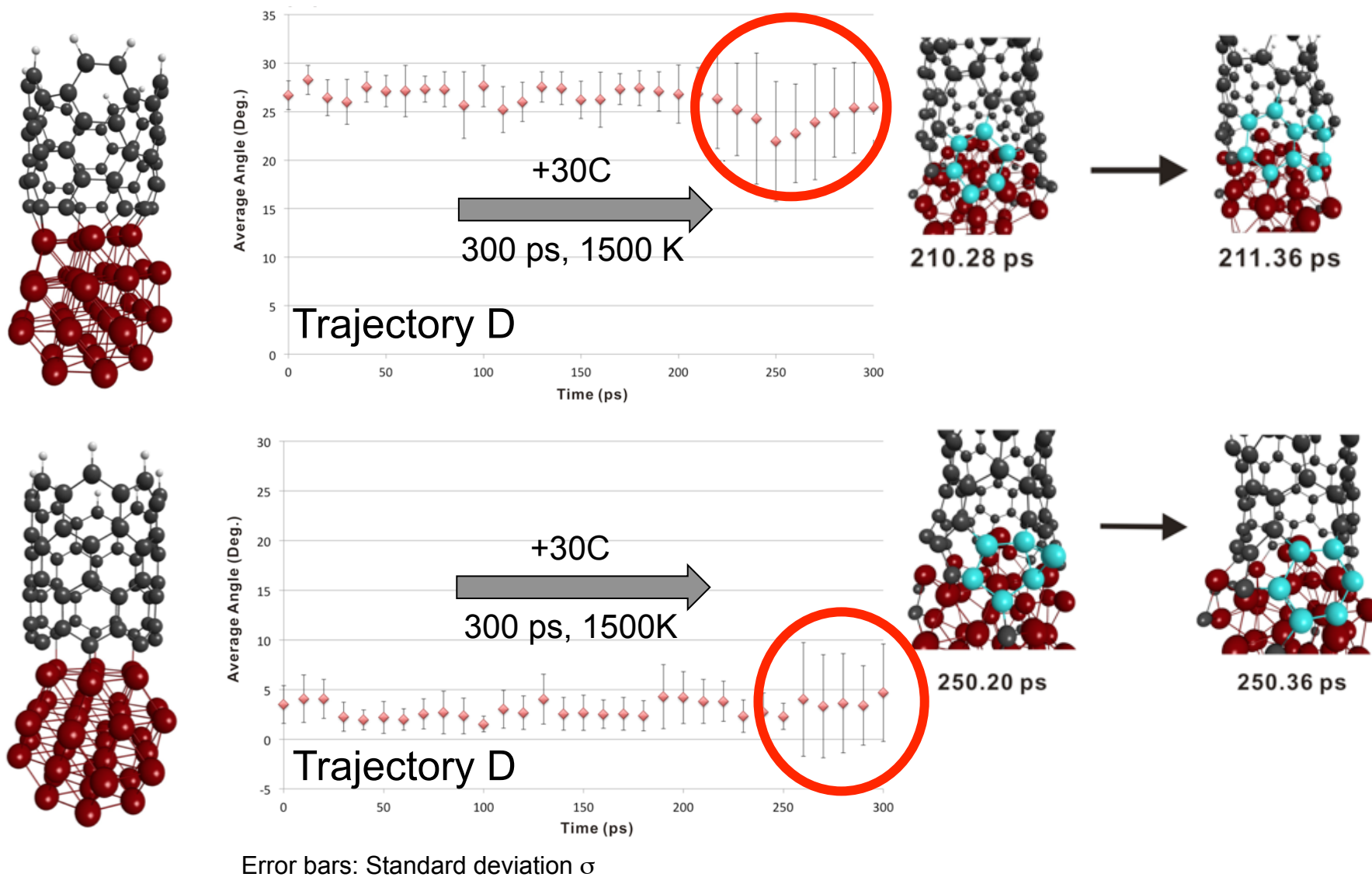
Requires: i) System's global principal axis in tube direction (GPAZ)  
ii) Hexagon's local principal axis normal to hexagon plane



J. Kim, S.I. K. Morokuma, *Phys. Rev. Lett.* **107**, 15505 (2011).

Slow simulations of (5,5) and (8,0) SWCNT growth on Fe<sub>38</sub>

Error bars: Standard deviation  $\sigma$

Slow simulations of (5,5) and (8,0) SWCNT growth on Fe<sub>38</sub>

## Slow simulations of (5,5) and (8,0) SWCNT growth on Fe<sub>38</sub>

Statistics based on 10 trajectories <sup>a</sup>		(5,5)	(8,0)
defect formation	pentagon formation	3.2	4.5
	heptagon formation	0.2	0.3
	hexagon → heptagon transformation	2.7	3.7
	hexagon → deformation	1.0	0.6
	hexagon → pentagon transformation	0.1	0.5
	total defects formed ( $\Sigma_1$ )	7.2	9.6
defect removal	hexagon formation	3.4	2.1
	heptagon → hexagon transformation	1.1	0.8
	pentagon → hexagon transformation	1.2	0.8
	total defects removed ( $\Sigma_2$ )	5.7	3.7
net healing ( $\Sigma_2 - \Sigma_1$ )		-1.5	-5.9

<sup>a</sup>All data are averaged over 10 trajectories following 300 ps of QM/MD simulation.

**Conclusions:** (5,5) grows less defects than (8,0), heals faster!

## “Confirmation” of Defect/Healing Growth by Experiment

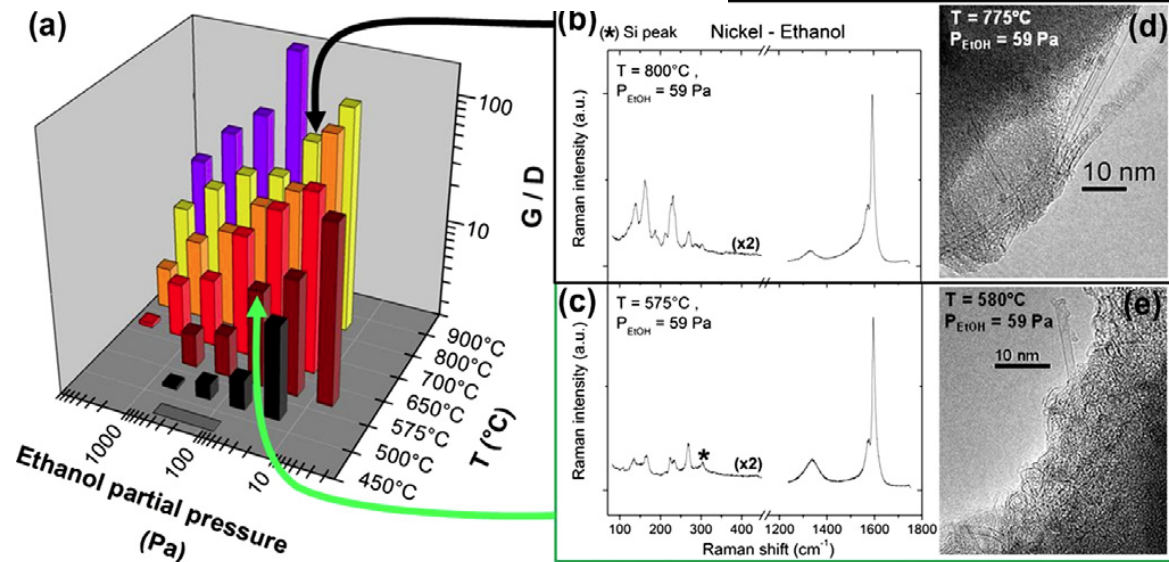
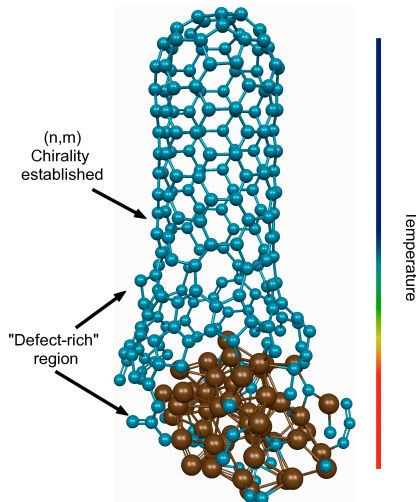
### Influence of the growth conditions on the defect density of single-walled carbon nanotubes

Carbon **50**, 2407 (2012)

Matthieu Picher <sup>a,b</sup>, Hugo Navas <sup>a,b</sup>, Raul Arenal <sup>c,d,f</sup>, Etienne Quesnel <sup>e</sup>, Eric Anglaret <sup>a,b</sup>, Vincent Jourdain <sup>a,b,\*</sup>

with reactive gas species). Generally speaking, these findings support that disordered structures at the nanotube rim are important intermediates of nanotube growth that should be explicitly considered in atomic-scale growth models.

cf: DFTB/MD growth model





# Overview

- Overview: What are MD simulations up against?
- Density-functional tight-binding (DFTB)-based MD
- DFTB/MD Simulations: Acetylene feedstock, carbon-only feedstock, catalytic CVD, catalyst-free CVD
- Key points: What did we learn?
- Comparison with thermodynamics and selected experiments
- **What is next?**

# What is next?

## We need to address the following urgent issues:

- Timescale problem in MD simulations, will allow to study:
  - Role of carbide formation
  - Role of defect healing
  - More precise mechanism
- Investigate possible mechanism for chirality control at time of nucleation
- Investigate role of hydrogen in greater detail
- Effect of various catalyst substrates
- Effect of etching gas [ $\text{NH}_3$ , cf S. Taubert, K. Laasonen, *JPCCC* **116**, 18538 (2012)]
- Effect of water  $\text{H}_2\text{O}$

