

# **Photoluminescence sidebands of carbon nanotubes below the bright singlet excitonic levels**

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## **Abstract**

We performed detailed photoluminescence (PL) spectroscopy studies of three different types of single-walled carbon nanotubes (SWNTs) by using samples that contain essentially only one chiral type of SWNT, (6,5), (7,5), or (10,5). The observed PL spectra unambiguously show the existence of an emission sideband at  $\sim 140$  meV below the lowest singlet excitonic ( $E_{11}$ ) level, whose identity and origin are now under debate. We find that the energy separation between the  $E_{11}$  level and the sideband is independent of the SWNT diameter within our experimental certainty. Based on this, we ascribe the origin of the observed sideband to coupling between  $K$ -point phonons and dipole-forbidden dark excitons, as recently suggested based on the measurement of (6,5) SWNTs.

## I. INTRODUCTION

The optical and electronic properties of one-dimensional (1-D) materials have been an important subject in the field of condensed matter physics [1,2]. The enhanced Coulomb interactions in 1-D often lead to the formation of strongly bound electron-hole ( $e-h$ ) pairs called excitons [3]. It is known that the optical properties of 1-D semiconductors are distinctly different from higher dimensional materials, being inherently dominated by excitons [4,5]. The sharp spatial localization of strongly bound excitons often makes the exciton-phonon ( $ex-ph$ ) interaction important [6].

Single-walled carbon nanotubes (SWNTs) [7] are novel 1-D materials that possess various unique properties [8]. The strong confinement in the radial direction ( $\sim 1$  nm) and the weak dielectric screening inside SWNTs give rise to very large exciton binding energies of  $\sim 0.5$  eV [9-13], which is much larger than those of InGaAs quantum wires [5,14] and larger than or comparable to those of  $\pi$ -conjugated polymers [15,16]. So far, various groups have studied the  $ex-ph$  interactions in SWNTs both in terms of theory [17,18] and experiment [19-22], and have revealed the existence of a phonon sideband approximately 200 meV above the energy level of the singlet bright exciton (which has an  $s$ -envelope and termed a “ $1u$ ” state based on symmetry [12,13] but we simply call it “ $E_{ii}$ ” hereafter for the  $i$ th single-particle subband) [17-22].

Techniques for preparing SWNT samples for optical studies have been rapidly improving recently. A technique that utilizes fluorene polymers to disperse SWNTs in organic solvents reported by Nish et al. [23] is considered to be particularly important because of the strong selectivity to specific chiral types of SWNTs. The density gradient separation method reported by Arnold et al. [24,25] is another important technique that

separates SWNTs according to their diameters as well as to their metallic/semiconducting property.

In this report, we performed detailed photoluminescence (PL) spectroscopy studies of three different types of SWNTs [(6,5), (7,5), and (10,5)] using samples containing virtually only one type of SWNT, and unambiguously show the existence of emission sidebands at approximately 140 meV below the  $E_{11}$  level for all of these SWNT types. Currently, the physical origin of this sideband is under debate: This sideband was initially discovered by Kiowski et al. [26], who explained its origin as “deep dark excitonic states”. They ruled out the possibility of a phonon-dissipating emission mechanism based on their experimental observation that the energy separation between the  $E_{11}$  level and the sideband ( $\delta$ ) is remarkably dependent on SWNT diameter ( $d_{\text{SWNT}}$ ). On the other hand, Torrens et al. [27] recently proposed that this sideband originates from dipole-forbidden “dark” excitons coupled with  $K$ -point phonons [i.e., the mechanism that was ruled out in Ref. (26)], based on their experimental measurement limited only to (6,5) SWNTs. Apparently, the dependence of  $\delta$  on  $d_{\text{SWNT}}$  is a key issue to resolve this conflict, which is essential for correctly understanding the properties of the weak photoemission found below the  $E_{11}$  states.

## II. EXPERIMENTAL RESULTS AND ANALYSIS

We prepared three types of samples, denoted as “DG”, “PFO”, and “PFO-BT”. In essence, the first sample was prepared based on the density-gradient separation method [25,28], and the latter two samples utilized fluorene polymers to individually disperse SWNTs in toluene [23]. Details of the sample preparation procedures are described

separately [29]. Although our samples may contain some amount of metallic SWNTs, since they do not emit PL [30], the possible existence of metallic SWNTs does not affect our results and discussion presented here.

Figure 1 shows colored contour maps of the PL excitation intensities measured from the (a, d) DG, (b, e) PFO, and (c, f) PFO-BT samples. Panels (d) - (f) are the same as panels (a) - (c), but the intensities are presented in log-scale. This figure shows that the samples contained virtually only one chiral type of SWNTs while the amounts of other types of SWNTs were highly suppressed. Panels (d) - (f) clearly show the existence of sidebands (indicated by the arrows) associated with the PL features of (6,5), (7,5), and (10,5) SWNTs, respectively.

Figures 2(a)-2(c) show PL spectra measured from the DG, PFO, and PFO-BT samples, obtained by resonantly exciting  $E_{22}$  levels of the dominant SWNT species with excitation wavelengths 570, 655, and 800 nm, respectively. The abscissa denotes energy relative to the PL emission maxima from respective  $E_{11}$  levels. We performed spectral decomposition analysis in order to obtain the positions and widths of the observed peaks. Specifically, we fit these spectra with an  $E_{11}$  PL peak, a shoulder at  $\sim 45$  meV below the  $E_{11}$  level [see Fig. S3 in Ref. (29)], and the PL sideband shown in Fig. 1. As for Fig. 2(c), additional peaks for (9,7) and (11,4) tubes were taken into account. We assumed a 50 % Lorentzian + 50 % Gaussian lineshape for all the peaks, and optimized both the positions and widths of the peaks to best reproduce the original spectra. In these figures, the blue dash curves show the summation of all the components, which overlap the experimental spectra shown by the black solid curves. Uncertainties or the possible ranges of the peak-maximum position of the sidebands obtained from the decomposition analysis are

indicated by horizontal bars shown in Figs. 2(a)-2(c), whose magnitudes are approximately 10 meV.

Figure 3(a) shows the peak widths (FWHM) of the observed  $E_{11}$  PL emission features (solid circles) and sideband features (solid squares), which were obtained from the above fitting analysis, plotted as a function of  $d_{\text{SWNT}}$ . The decrease of the widths of the  $E_{11}$  PL emission features with the increase of  $d_{\text{SWNT}}$  agrees with the behavior reported by Inoue et al. [31]. Although the samples measured in this study were ensembles of SWNTs, the clear dependence of the  $E_{11}$  emission widths on  $d_{\text{SWNT}}$  indicates that these peaks were not completely smeared out by the ensemble effect. In fact, the widths (15 - 30 meV) are approximately twice those measured from a single, isolated SWNT at room temperature [31]. It is noted that the widths of the sideband features show a similar inverse dependence on  $d_{\text{SWNT}}$  and are always larger than those of the  $E_{11}$  features, which indicates that these features are not artifacts due to  $E_{11}$  PL emissions from other SWNTs with larger diameters.

The filled squares plotted in Fig. 3(b) represent the dependence of  $\delta$  on  $d_{\text{SWNT}}$ , which shows that the observed  $\delta$  is independent of  $d_{\text{SWNT}}$  ( $\sim 140$  meV, in the range of  $0.75 \leq d_{\text{SWNT}} \leq 1.05$  nm) within the uncertainties indicated in Figs. 2(a)-2(c) [shown by error bars in Fig. 3(b)]. For comparison, the values of  $\delta$  reported for the similar sidebands in Ref. (26) are plotted as open triangles in the same figure, with the experimental uncertainty of  $\pm 5$  meV represented by the error bars. As described by the authors, their  $\delta$  shows a remarkable dependence on  $d_{\text{SWNT}}$ , which is qualitatively different from our experimental observation, i.e., there is a clear difference between these two datasets that exceeds the uncertainties in both experiments. Kiowski et al. [26] explained that the

observed PL sidebands were weak PL emission from “deep dark excitonic states” below the  $E_{11}$  levels, even lower than the energy level of the singlet dark exciton with zero angular momentum and an  $s$ -envelope (termed the “1g” exciton [12,13] and has energy  $\sim 5$  meV lower than the  $E_{11}$  (or “1u”) level [32-34]). It is noted that these authors have ruled out the possibility of phonon-involved processes regarding the origin of these sidebands based on the apparent dependence of  $\delta$  on  $d_{\text{SWNT}}$  [26]. In contrast, the independence of  $\delta$  on  $d_{\text{SWNT}}$  observed in this study suggests an involvement of phonons in the origin of these sidebands, particularly the involvement of higher-frequency ( $> 1000$   $\text{cm}^{-1}$ ) phonons that arise from the phonon dispersion relations of graphite [35], and hence is essentially independent of  $d_{\text{SWNT}}$ . So far, the phonon sideband at  $\sim 200$  meV above the  $E_{ii}$  levels has been well recognized and studied [17-22]. This phonon sideband was first predicted by Perebeinos et al. [17] as a result of strong coupling between dipole-forbidden excitons above the  $E_{11}$  level and  $K$ -point phonons ( $\sim 170$  meV). This phonon is known to possess an in-plane transverse optical (TO) mode, and is responsible for the D-band Raman feature in graphite and carbon nanotubes through a one-phonon emission double-resonance Raman process [35-37].

### III. DISCUSSIONS

Figure 4 shows a schematic diagram that describes the four lowest-energy states of singlet excitons in SWNTs [32]. The abscissa denotes the momentum  $q$  of the excitons. The solid (dashed) curve represents the dipole-allowed (dipole-forbidden) excitonic state with zero angular momentum  $E_{11}$  ( $E_{1g}$ ). The dot-dashed curve denotes the dipole-forbidden exciton band with finite angular momentum, whose energy has been predicted

to be approximately 20–30 meV higher than the  $E_{11}$  level for  $q = 0$  [32]. We denote this energy separation by  $\Delta$  as shown in Fig. 4. Only the  $q \approx 0$  excitons in the  $E_{11}$  level can directly interact with photons. For simplicity, we have shown here the diagram for zigzag SWNTs [32,38], but the generality in the following discussion is not affected by this simplification. Based on this schematic, the phonon sideband predicted by Perebeinos et al. corresponds to the point ‘A’, emerging as a result of the scattering of the dark exciton at  $q = q_0$  (point ‘X’) by  $K$ -point TO phonons with  $q = -q_0$  [17].

We explain the origin of the observed sideband at  $\sim 140$  meV below  $E_{11}$  as follows, based on the same model recently proposed by Torrens et al. [27]. The strong coupling between dark excitons with finite angular momentum and  $K$ -point phonons ( $\sim 170$  meV  $\equiv E_{\text{ph}}$ ) predicted by Perebeinos et al. [17] also causes the scattering of dark excitons at  $q = q_0$  (at ‘X’ in Fig. 4) into the bright excitonic state at  $q = 0$  (‘B’ in Fig. 4), reducing their energy by  $E_{\text{ph}}$  through emission of a  $K$ -point TO phonon of wavevector  $q_0$ , *satisfying both the energy and momentum conservation requirements simultaneously*. In this process, the phonon sideband is expected to appear at approximately 140 meV ( $\cong 170 - 30$  meV) below the  $E_{11}$  level, which agrees well with our experimental results. We note that the sidebands disappeared at 6 K according to the results shown by Kiowski et al. [26], and this seems to support the above phonon-mediated interpretation.

Here, we briefly describe the values of  $\Delta$  for (6,5) and (7,5) tubes based on the values obtained for  $\delta$ . To do this we need to know the energy differences between  $E_{11}$  levels and their PLE sidebands, denoted by  $\delta_{\text{PLE}}$ . We obtained  $\delta_{\text{PLE}}$  for (6,5) and (7,5) from Fig. 2A in Ref. (30), which are approximately 212 and 209 meV, respectively. Using the



relationship  $\Delta = (\delta_{\text{PLE}} - \delta)/2$  [27], we obtained  $\Delta = 35 \pm 5$  meV for both (6,5) and (7,5) SWNTs.

Finally, we estimate the possible effect of environmental difference in the three types of samples used in this study. As shown in Figure S1 [29], the  $E_{11}$  emission energies of (6,5) tubes in the “PFO” and “DG” samples differ by  $\sim 9$  meV. (Our unpublished data show that the  $E_{11}$  energy difference of the same chirality tubes between the “PFO” and “PFO-BT” samples is much smaller.) The exciton binding energy, the energy difference between the band gap and the  $E_{11}$  level, of (6,5) tubes is known to be  $\sim 400$  meV [13]. This means that the overall Coulomb interaction that determines the magnitude of the  $e$ - $h$  interaction is changed by  $\sim 2\%$  due to the environment. By a first approximation, the magnitude of  $\Delta$  is considered to be modified by a similar proportion. 2% of  $\Delta$  ( $\sim 35$  meV) is 0.7 meV, which is the estimated difference in the value of  $\Delta$  due to the environment. This is negligible compared to the magnitude of the error bars ( $\sim 10$  meV) shown in Fig. 3(b).

#### IV. SUMMARY

We have performed detailed PL studies of (6,5), (7,5), and (10,5) SWNTs by using samples that contain essentially only one chiral type of SWNT. Their PL spectra unambiguously show sideband features at  $\sim 140$  meV below the  $E_{11}$  levels for all of these SWNT types. The experimental results showed that  $\delta$  was almost independent of  $d_{\text{SWNT}}$  within the resolution of our data ( $\pm 5$  meV). This result suggests that the observed sidebands emerge as a result of strong coupling between dark excitons with finite angular

momentum and  $K$ -point TO phonons, in agreement with the recent suggestion by Torrens et al. [27] based on measurements of (6,5) SWNTs.

## ACKNOWLEDGEMENTS

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## Figure Captions

FIG. 1: (Color online) Contour maps of PL excitation intensities measured from the (a, d) DG, (b, e) PFO, and (c, f) PFO-BT samples. Intensity scale-bars are attached to the right of each panel, where the unit is photon count. Panels (d) - (f) are the same as panels (a) - (c), but the intensities are shown in log scale. Arrows indicate the locations of the sidebands.

FIG. 2: (Color online) PL spectra measured from the (a) DG, (b) PFO, and (c) PFO-BT samples, obtained by resonantly exciting the  $E_{22}$  levels of the dominant SWNTs with excitation wavelengths of 570, 655, and 800 nm, respectively. The abscissa represents the energy relative to the  $E_{11}$  levels of (6,5), (7,5), and (10,5) SWNTs. The original spectra, shown by black solid curves, were decomposed into multiple peaks, and the summation is shown by blue dashed curves. The gray short-dash curves in (b) and (c) are spectral baselines assumed in the analysis. The uncertainties in the peak-maximum positions of the PL sidebands are indicated by the horizontal bars.

FIG. 3: (Color online) (a) Dependence of the peak widths (FWHM) of the  $E_{11}$  PL emissions (solid circles) and the observed sidebands (solid squares) on  $d_{\text{SWNT}}$ . The widths were obtained from the fitting analysis shown in Fig. 2. (b) Solid squares: The relationship between  $\delta$  and  $d_{\text{SWNT}}$  measured in this study. Magnitudes of the error bars are the same as widths of the horizontal bars shown in Figs. 2(a)-2(c). Open triangles: The relationship between  $\delta$  and  $d_{\text{SWNT}}$  for

similar PL sidebands reported in Ref. (26), where the error bars denote  $\pm 5$  meV experimental accuracy reported in the literature.

FIG. 4: (Color online) Schematic diagram showing the four lowest-energy singlet exciton states in SWNTs. The abscissa denotes the exciton momentum. The solid and dashed curves denote bright ( $E_{11}$ ) and dark ( $E_{1g}$ ) exciton bands with zero angular momentum, respectively. The dot-dashed curve denotes the dark exciton band with non-zero angular momentum. The arrow connecting the points 'X' and 'B' shows the process suggested for the PL sidebands observed in this study.

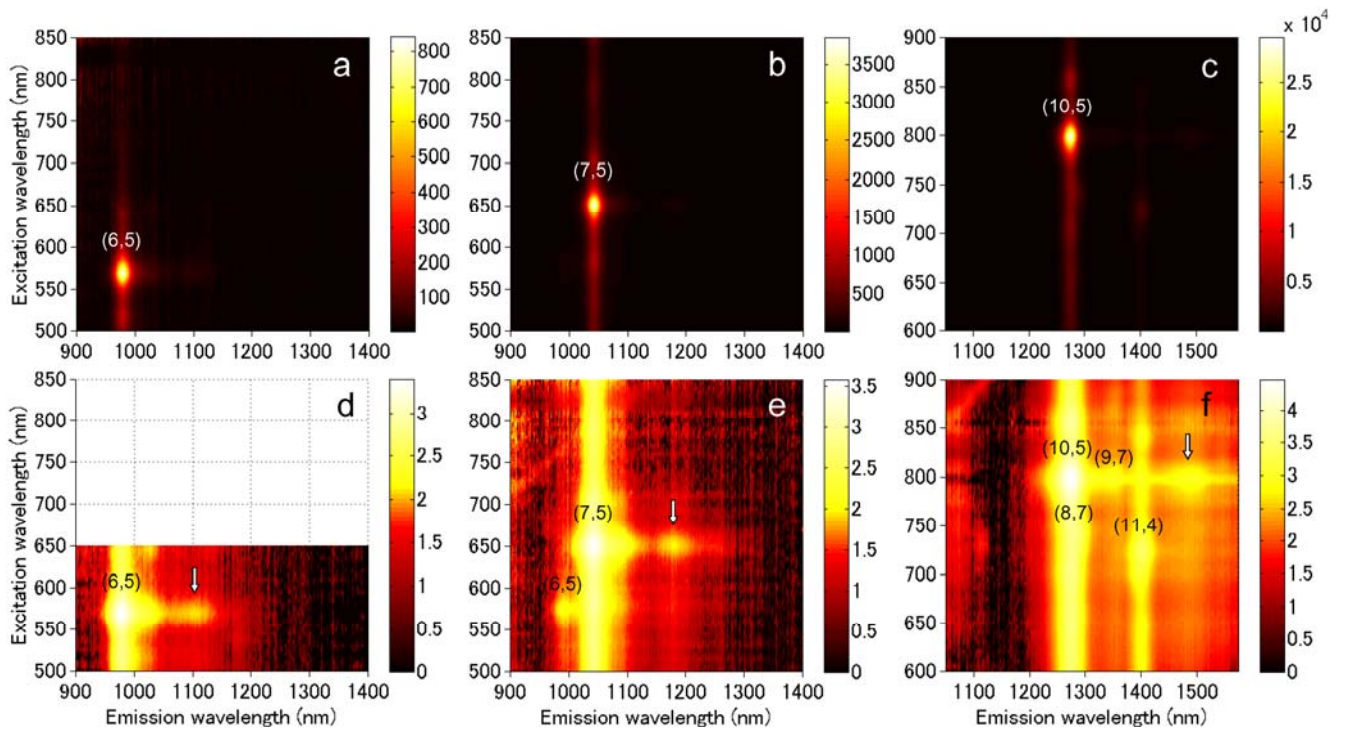


Figure 1



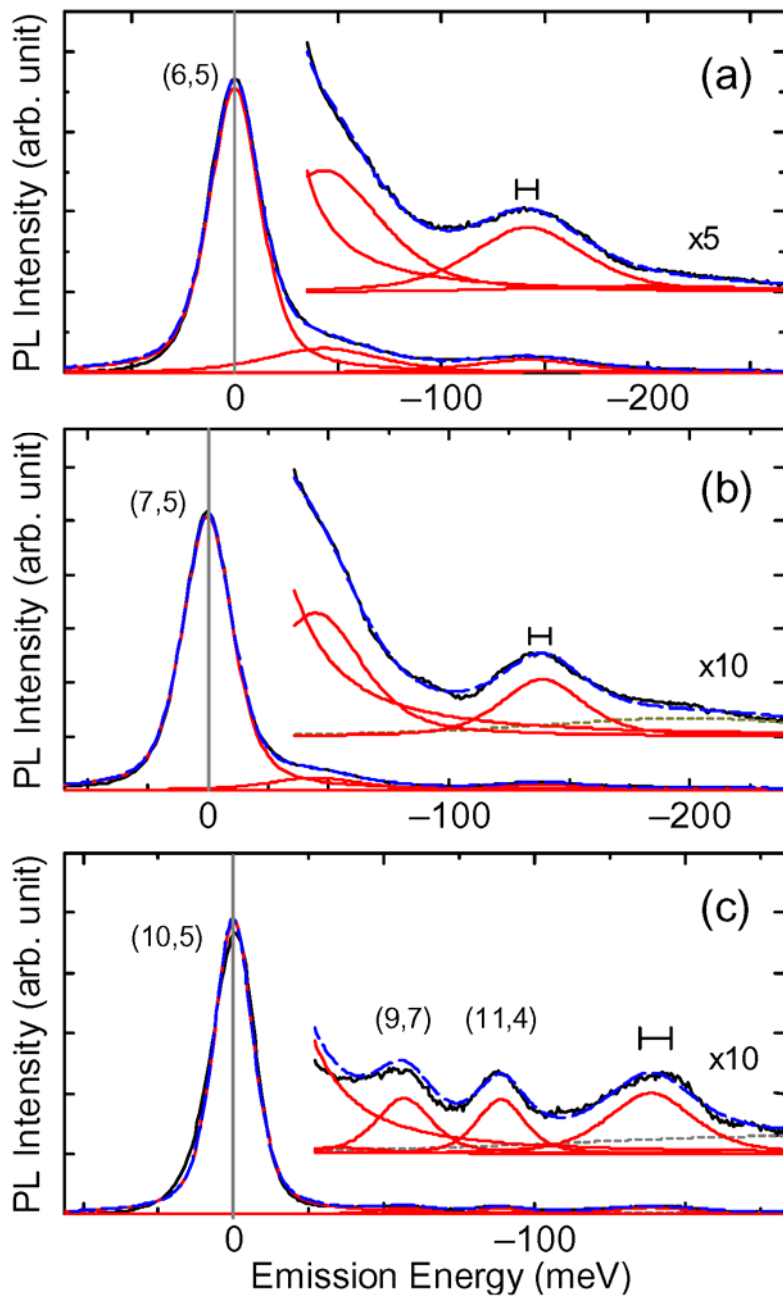


Figure 2

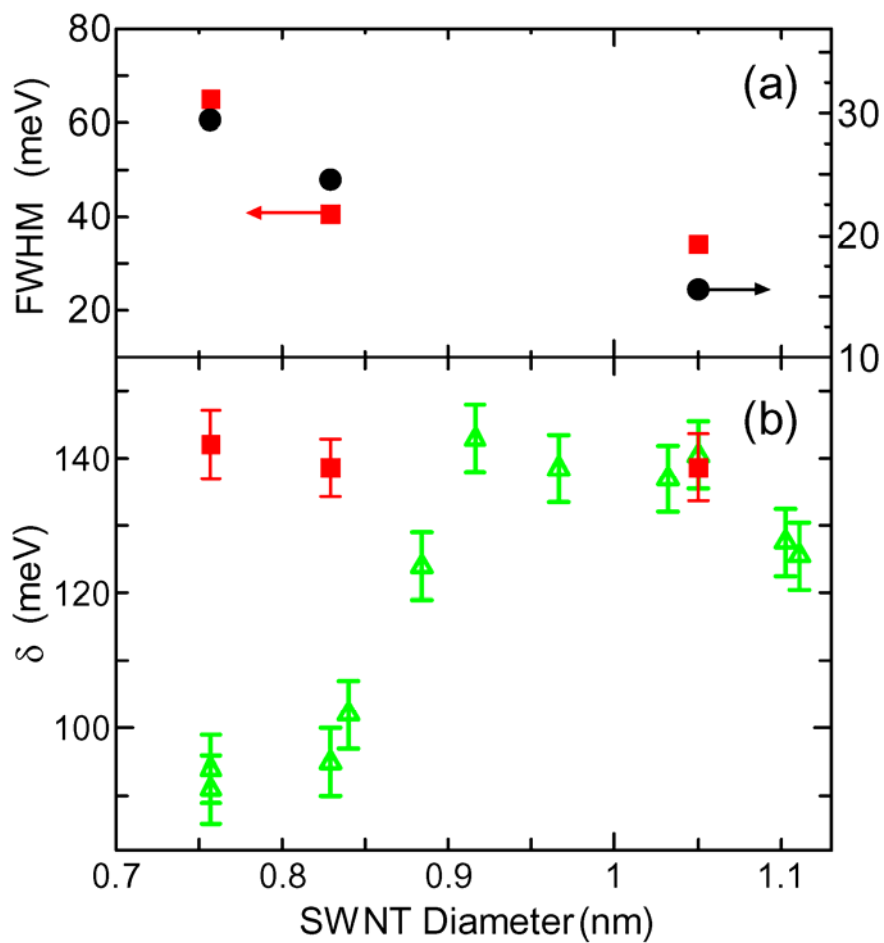


Figure 3

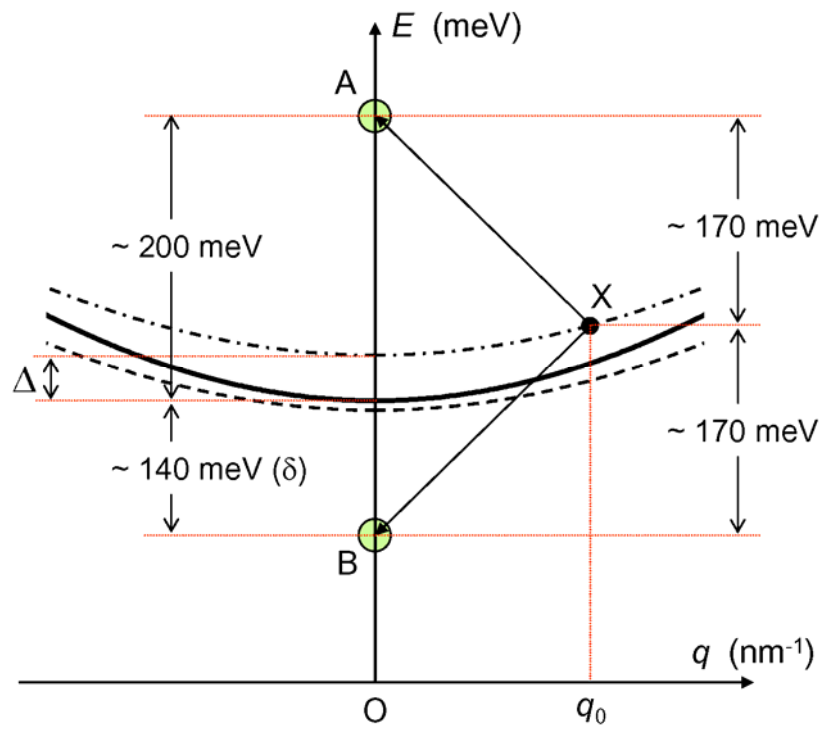


Figure 4