

MD Simulation for Microscale Heat Transfer

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1. Microscale Heat Transfer

- 1.1 Why do we deal with Molecular Dynamics?
- 1.2 Molecular Dynamics Method and Monte Carlo Method
- 1.3 Quantum Dynamics, *ab initio* Calculations

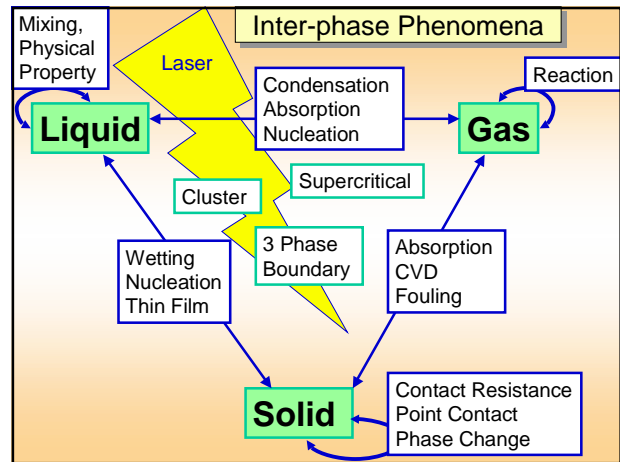
1. Microscale Heat Transfer and MD Simulation?

Fields of Applications of Molecular Heat Transfer

- Heat and Mass Transfer through **Interphase** (Phase Change, Ablation)
- Stress at **Composite Materials**
- Seeking for a **New Materials** (Especially Thermal Properties)
- Manufacturing Process of **Thin Film** (CVD, etc)
- Physical Properties of **Thin Film**
- Faulting** of Solid Materials
- Numerical Prediction of **Physical Properties**
- High Speed and High Flux** Energy Transfer
- Control of **Cluster**

Thermal Phenomena including **Chemical Reactions**
Manufacturing and Control with **Laser**,
Electron Beam and **Molecular Beam**

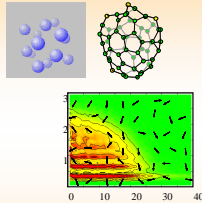
Quantum
Effectn &
State of
Electron



Phase change phenomena

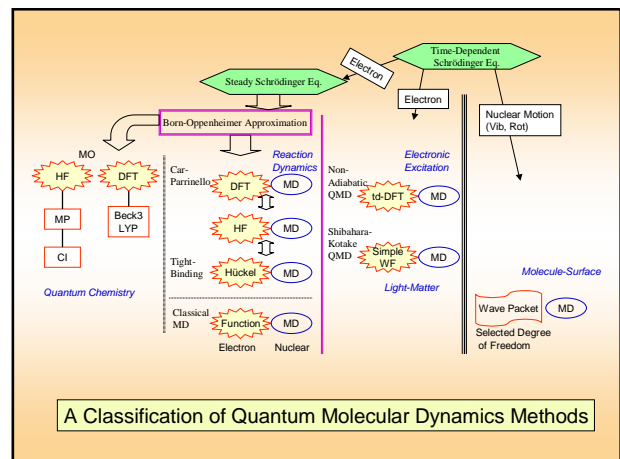
Microscopic Problems

- Clustering
- Ultra-super cooling/heating
- Uniform phase change
- Ultra-fast phase change



Macroscopic Problems

- Nucleation (homogeneous & heterogeneous)
- Maximum heat flux
- Condensation coefficient



Time-Dependent Schrödinger Eq. $i\hbar \frac{\partial \psi}{\partial t} = H\psi$ $H = H_0 + \left\{ -\sum_i e\phi_i + \sum_k Z_k e\mathbf{R}_k \right\} \cdot \mathbf{E}$

Electron

$$H_0 = -\sum_k \frac{\hbar^2}{2M_k} \nabla_k^2 - \sum_i \frac{\hbar^2}{2m} \nabla_i^2 + \sum_{k,l} \frac{Z_k Z_l e^2}{|\mathbf{R}_k - \mathbf{R}_l|} - \sum_{k,j} \frac{Z_k e^2}{|\mathbf{R}_k - \mathbf{r}_j|} + \sum_{i,j} \frac{e^2}{|\mathbf{r}_i - \mathbf{r}_j|}$$

Steady Schrödinger Eq.

$$\psi(\vec{r}, t) = \psi_0(\vec{r}) e^{\frac{E}{\hbar} t}$$

$$E\psi_0 = H\psi_0$$

electrons \mathbf{r}_i

nuclei \mathbf{R}_k

Schrödinger Equation

Steady Schrödinger Eq. $H\Psi = E\Psi$

Electron

Time-Dependent Schrödinger Eq.

$$H = -\sum_k \frac{\hbar^2}{2M_k} \nabla_k^2 - \sum_i \frac{\hbar^2}{2m} \nabla_i^2 + \sum_{k,l} \frac{Z_k Z_l e^2}{|\mathbf{R}_k - \mathbf{R}_l|} - \sum_{k,j} \frac{Z_k e^2}{|\mathbf{R}_k - \mathbf{r}_j|} + \sum_{i,j} \frac{e^2}{|\mathbf{r}_i - \mathbf{r}_j|}$$

Born-Oppenheimer Approximation

$\Psi_{mol} = \psi_e(\mathbf{r}; \mathbf{R}) \chi_N(\mathbf{R})$ *Electrons moves much slowly than nuclei*

$$H_e \psi_e = \left\{ \sum_i \frac{\hbar^2}{2m} \nabla_i^2 - \sum_{k,j} \frac{Z_k e^2}{|\mathbf{r}_j - \mathbf{R}_k|} + \sum_{i,j} \frac{e^2}{|\mathbf{r}_i - \mathbf{r}_j|} \right\} \psi_e = E_e(\mathbf{R}_{AB}) \psi_e$$

$$H_N \chi_N = \left\{ -\sum_{k=A,B} \frac{\hbar^2}{2M_k} \nabla_k^2 - E_e(\mathbf{R}_{AB}) + \frac{Z_A Z_B e^2}{R_{AB}} \right\} \chi_N = E_{Total} \chi_N$$

The Born-Oppenheimer Approximation

Steady Schrödinger Eq. \downarrow Born-Oppenheimer Approximation \downarrow Time-Dependent Schrödinger Eq.

Electron

Molecular Orbital Method

LCMO(linear combination of atomic orbitals)

HF: Hartree-Fock Theory

Basis Sets

Polarized, Diffuse: 6-31G(d), 6-311+G(d,p), 6-311++G(3df, 3pd)

Electron Correlations

MP: Moller-Plesset Perturbation Theory, MP2, MP3, MP4

CI: Configuration Interaction

cf. Gaussian94

Molecular Orbital Calculations - Quantum Chemistry

Steady Schrödinger Eq. \downarrow Born-Oppenheimer Approximation \downarrow Time-Dependent Schrödinger Eq.

Electron

DFT: Density Functional Theory

$$\left[-\frac{1}{2} \nabla_i^2 + V(\mathbf{r}) \right] \psi_i(\mathbf{r}) = \epsilon_i \psi_i(\mathbf{r})$$

$$V(\mathbf{r}) = -\sum_{a=1}^N \frac{Z_a}{|\mathbf{r} - \mathbf{r}_a|} + \int \frac{\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + V_{xc}(\mathbf{r})$$

Exchange-Correlation

B3LYP: Beck's 3 parameter Exchange Functional with Lee-Yang-Parr Correlation

cf. Gaussian94

Density Functional Theory - Quantum Chemistry

Steady Schrödinger Eq. \downarrow Born-Oppenheimer Approximation \downarrow Time-Dependent Schrödinger Eq.

Electron

Molecular Dynamics for Nuclei

Position of Nuclei

Hellmann-Feynman Force

DFT for Electronic Wave Function

Fictitious mass of electronic degree

Time

Time

Car-Parrinello Method